

# Logiweb codex of rapport

## Up Help

rapport, , LEMMA3.2(a), LEMMA3.2(b), LEMMA3.2(c), LEMMA3.2(d), LEMMA3.2(f), LEMMA3.2(f)base, LEMMA3.2(f)induction, LEMMA3.2(g), LEMMA3.2(g)base, LEMMA3.2(g)induction, LEMMA3.2(h), LEMMA3.2(h)base, LEMMA3.2(h)induction, IMV, CImp, TImp,

## rapport

[rapport  $\xrightarrow{\text{pyk}}$  “rapport”]

[ $\xrightarrow{\text{tex}}$  “”]

[ $\xrightarrow{\text{pyk}}$  “blank space”]

## LEMMA3.2(a)

[LEMMA3.2(a)  $\xrightarrow{\text{proof}}$   $\lambda c. \lambda x. \mathcal{P}(\lceil S' \vdash \forall t: [ [ S5' \gg [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] ] ; [ [ S1' \gg [ [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] \Rightarrow [ [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] \Rightarrow [ \underline{t} \stackrel{p}{=} \underline{t} ] ] ] ] ; [ [ [ [ MP' \triangleright [ [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] \Rightarrow [ [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] \Rightarrow [ \underline{t} \stackrel{p}{=} \underline{t} ] ] ] ] \triangleright [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] ] \gg [ [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] \Rightarrow [ \underline{t} \stackrel{p}{=} \underline{t} ] ] ] ; [ [ [ MP' \triangleright [ [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] \Rightarrow [ \underline{t} \stackrel{p}{=} \underline{t} ] ] ] \triangleright [ [ \underline{t} \dot{+} \dot{0} ] \stackrel{p}{=} \underline{t} ] ] \gg [ \underline{t} \stackrel{p}{=} \underline{t} ] ] ] ] \rceil, p_0, c)$ ]

[LEMMA3.2(a)  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall t: [ \underline{t} \stackrel{p}{=} \underline{t} ]$ ]

[LEMMA3.2(a)  $\xrightarrow{\text{tex}}$  “LEMMA 3.2(a)”]

[LEMMA3.2(a)  $\xrightarrow{\text{pyk}}$  “mendelson lemma three two a”]

## LEMMA3.2(b)

[LEMMA3.2(b)  $\xrightarrow{\text{proof}}$   $\lambda c. \lambda x. \mathcal{P}(\lceil S' \vdash \forall t: \forall r: [ [ S1' \gg [ [ \underline{t} \stackrel{p}{=} \underline{r} ] \Rightarrow [ [ \underline{t} \stackrel{p}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{p}{=} \underline{t} ] ] ] ] ; [ [ [ CImp \triangleright [ [ \underline{t} \stackrel{p}{=} \underline{r} ] \Rightarrow [ [ \underline{t} \stackrel{p}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{p}{=} \underline{t} ] ] ] ] \gg [ [ \underline{t} \stackrel{p}{=} \underline{t} ] \Rightarrow [ [ \underline{t} \stackrel{p}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{p}{=} \underline{t} ] ] ] ] ; [ [ LEMMA3.2(a) \gg [ \underline{t} \stackrel{p}{=} \underline{t} ] ] ] \rceil$ ]

$] ; [ [ [ MP' \triangleright [ [ \underline{t} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{t} ] ] ] ] \triangleright [ \underline{t} \stackrel{P}{=} \underline{t} ] ] \gg [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{t} ] ] ] ] ] , p_0, c ]$

[LEMMA3.2(b)  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{t}. \forall \underline{r}. [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{t} ] ] ]$

[LEMMA3.2(b)  $\xrightarrow{\text{tex}}$  “LEMMA 3.2(b)”]

[LEMMA3.2(b)  $\xrightarrow{\text{pyk}}$  “mendelson lemma three two b”]

## LEMMA3.2(c)

[LEMMA3.2(c)  $\xrightarrow{\text{proof}}$   $\lambda c. \lambda x. \mathcal{P}([S' \vdash \forall \underline{t}. \forall \underline{r}. \forall \underline{s}. [ [ S1' \gg [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] ; [ [ \text{LEMMA3.2(b)} \gg [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{t} ] ] ] ] ; [ [ [ \text{TImp} \triangleright [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{t} ] ] ] \triangleright [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] \gg [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] ] , p_0, c )]$

[LEMMA3.2(c)  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{t}. \forall \underline{r}. \forall \underline{s}. [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ]$

[LEMMA3.2(c)  $\xrightarrow{\text{tex}}$  “LEMMA 3.2(c)”]

[LEMMA3.2(c)  $\xrightarrow{\text{pyk}}$  “mendelson lemma three two c”]

## LEMMA3.2(d)

[LEMMA3.2(d)  $\xrightarrow{\text{proof}}$   $\lambda c. \lambda x. \mathcal{P}([S' \vdash \forall \underline{t}. \forall \underline{r}. \forall \underline{s}. [ [ \text{LEMMA3.2(c)} \gg [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{t} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ; [ [ [ \text{CImp} \triangleright [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{t} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] \gg [ [ \underline{t} \stackrel{P}{=} \underline{s} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ; [ [ \text{LEMMA3.2(b)} \gg [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ; [ [ [ [ \text{TImp} \triangleright [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] \triangleright [ [ \underline{t} \stackrel{P}{=} \underline{s} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] \gg [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ; [ [ \text{CImp} \triangleright [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] \gg [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] , p_0, c )]$

[LEMMA3.2(d)  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{t}. \forall \underline{r}. \forall \underline{s}. [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ]$

[LEMMA3.2(d)  $\xrightarrow{\text{tex}}$  “LEMMA 3.2(d)”]

[LEMMA3.2(d)  $\xrightarrow{\text{pyk}}$  “mendelson lemma three two d”]

## LEMMA3.2(f)

[LEMMA3.2(f)  $\xrightarrow{\text{proof}}$   $\lambda c. \lambda x. \mathcal{P}([S' \vdash [ [ S9' \gg [ [ \dot{0} \stackrel{P}{=} [ \dot{0} \dot{+} \dot{0} ] ] \Rightarrow [ [ \dot{\forall} \underline{t}. [ [ \dot{t} \stackrel{P}{=} [ \dot{0} \dot{+} [ \dot{t} ] ] ] ] \Rightarrow [ \dot{t}' \stackrel{P}{=} [ \dot{0} \dot{+} [ \dot{t}' ] ] ] ] ] \Rightarrow \dot{\forall} \underline{t}. [ \dot{t} \stackrel{P}{=} [ \dot{0} \dot{+} [ \dot{t} ] ] ] ] ] ] ; [ [ \text{LEMMA3.2(f)base} \gg [ \dot{0} \stackrel{P}{=} [ \dot{0} \dot{+} \dot{0} ] ] ] ; [ [ [ [ MP' \triangleright [ [ \dot{0} \stackrel{P}{=} [$



$$\begin{aligned}
& [\dot{t}'] \stackrel{p}{=} [\dot{0} \dot{+} [\dot{t}]]' \Rightarrow [\dot{t}' \stackrel{p}{=} [\dot{0} \dot{+} [\dot{t}']]] \gg [[[\dot{0} \dot{+} [\dot{t}']]] \stackrel{p}{=} [[[\dot{0} \dot{+} [\dot{t}]]']]] \Rightarrow [[[\dot{t}' \stackrel{p}{=} [\dot{0} \dot{+} [\dot{t}']]]] \stackrel{p}{=} [[[\dot{0} \dot{+} [\dot{t}]]']]]]; \\
& [[[\text{MP}' \triangleright [[[\dot{0} \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{0} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{t}' \stackrel{p}{=} [\dot{0} \dot{+} [\dot{t}]]]]] \triangleright [[[\dot{0} \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{0} \dot{+} [\dot{t}]]']]]]] \gg [[[\dot{t}' \stackrel{p}{=} [\dot{0} \dot{+} [\dot{t}]]] \Rightarrow [\dot{t}' \stackrel{p}{=} [\dot{0} \dot{+} [\dot{t}']]]]]], p_0, c)]
\end{aligned}$$

$$[\text{LEMMA3.2(f)induction} \xrightarrow{\text{stmt}} S' \vdash [[[\dot{t}' \stackrel{p}{=} [\dot{0} \dot{+} [\dot{t}]]] \Rightarrow [\dot{t}' \stackrel{p}{=} [\dot{0} \dot{+} [\dot{t}']]]]]]$$

$$[\text{LEMMA3.2(f)induction} \xrightarrow{\text{tex}} \text{"LEMMA 3.2(f) induction"}]$$

$$[\text{LEMMA3.2(f)induction} \xrightarrow{\text{pyk}} \text{"mendelson lemma three two f induction"}]$$

## LEMMA3.2(g)

$$\begin{aligned}
& [\text{LEMMA3.2(g)} \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash [[S9' \gg [[[\dot{r}' \dot{+} \dot{0}] \stackrel{p}{=} [[[\dot{r} \dot{+} \dot{0}]]']]]] \Rightarrow [[[\dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \Rightarrow \dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]]; \\
& \text{LEMMA3.2(g)base} \gg [[[\dot{r}' \dot{+} \dot{0}] \stackrel{p}{=} [[[\dot{r} \dot{+} \dot{0}]]']]]]; [[[\text{MP}' \triangleright [[[\dot{r}' \dot{+} \dot{0}] \stackrel{p}{=} [[[\dot{r} \dot{+} \dot{0}]]']]] \Rightarrow [[[\dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \Rightarrow \dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \triangleright [[[\dot{r}' \dot{+} \dot{0}] \stackrel{p}{=} [[[\dot{r} \dot{+} \dot{0}]]']]]] \gg [[[\dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \Rightarrow \dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]; \\
& [[[\text{LEMMA3.2(g)induction} \gg [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]]; [[[\text{Gen}' \triangleright [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \gg \dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]]; [[[\text{MP}' \triangleright [[[\dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \Rightarrow \dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \triangleright \dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}']] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \gg \dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]; \\
& [[[\text{A4'@} [\dot{t}]] \gg [[[\dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]]; [[[\text{MP}' \triangleright [[[\dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \Rightarrow [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]] \triangleright \dot{v}\dot{t}: [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]] \gg [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]]], p_0, c)]
\end{aligned}$$

$$[\text{LEMMA3.2(g)} \xrightarrow{\text{stmt}} S' \vdash [[[\dot{r}' \dot{+} [\dot{t}]]] \stackrel{p}{=} [[[\dot{r} \dot{+} [\dot{t}]]']]]]$$

$$[\text{LEMMA3.2(g)} \xrightarrow{\text{tex}} \text{"LEMMA 3.2(g)"}]$$

$$[\text{LEMMA3.2(g)} \xrightarrow{\text{pyk}} \text{"mendelson lemma three two g"}]$$