

[propositional calculus $\xrightarrow{\text{pyk}}$ “propositional calculus”]

[$T_{PC} \xrightarrow{\text{stmt}} \forall \underline{b}: \forall \underline{c}: \forall \underline{d}: \underline{b} \Rightarrow \underline{c} \Rightarrow \underline{d} \Rightarrow \underline{b} \Rightarrow \underline{c} \Rightarrow \underline{b} \Rightarrow \underline{d} \oplus \forall \underline{b}: \forall \underline{c}: \underline{b} \vdash \underline{b} \Rightarrow \underline{c} \vdash \underline{c}$ \oplus
 $\forall \underline{b}: \forall \underline{c}: \underline{b} \Rightarrow \underline{c} \Rightarrow \underline{b} \oplus \forall \underline{b}: \forall \underline{c}: \neg \underline{c} \Rightarrow \neg \underline{b} \Rightarrow \neg \underline{c} \Rightarrow \underline{b} \Rightarrow \underline{c}$]

[$T_{PC} \xrightarrow{\text{pyk}}$ “propositional theory”]

[$x \Rightarrow y \xrightarrow{\text{pyk}}$ “* imply *”]

[$x \Rightarrow y \xrightarrow{\text{val}}$ $\neg x \vee y$]

[$T \Rightarrow T$] \cdot

[$T \Rightarrow F$] $-$

[$F \Rightarrow T$] \cdot

[$F \Rightarrow F$] \cdot

[A1 $\xrightarrow{\text{pyk}}$ “axiom one”]

[A2 $\xrightarrow{\text{pyk}}$ “axiom two”]

[A3 $\xrightarrow{\text{pyk}}$ “axiom three”]

[MP $\xrightarrow{\text{pyk}}$ “mp”]

[$A1 \xrightarrow{\text{stmt}} T_{PC} \vdash \forall \underline{b}: \forall \underline{c}: \underline{b} \Rightarrow \underline{c} \Rightarrow \underline{b}$][A1 $\xrightarrow{\text{proof}}$ Rule tactic]

[$A2 \xrightarrow{\text{stmt}} T_{PC} \vdash \forall \underline{b}: \forall \underline{c}: \forall \underline{d}: \underline{b} \Rightarrow \underline{c} \Rightarrow \underline{d} \Rightarrow \underline{b} \Rightarrow \underline{c} \Rightarrow \underline{b} \Rightarrow \underline{d}$][A2 $\xrightarrow{\text{proof}}$ Rule tactic]

[A3 $\xrightarrow{\text{stmt}} T_{PC} \vdash \forall \underline{b}: \forall \underline{c}: \neg \underline{c} \Rightarrow \neg \underline{b} \Rightarrow \neg \underline{c} \Rightarrow \underline{b} \Rightarrow \underline{c}$][A3 $\xrightarrow{\text{proof}}$ Rule tactic]

[MP $\xrightarrow{\text{stmt}} T_{PC} \vdash \forall \underline{b}: \forall \underline{c}: \underline{b} \vdash \underline{c} \vdash \underline{c}$][MP $\xrightarrow{\text{proof}}$ Rule tactic]

[LEMMA1.8 $\xrightarrow{\text{pyk}}$ “mendelson lemma one eight”]

[LEMMA1.8 $\xrightarrow{\text{stmt}}$ $T_{PC} \vdash \forall \underline{b}: \underline{b} \Rightarrow \underline{b}$]

[LEMMA1.8 $\xrightarrow{\text{proof}}$ $\lambda c. \lambda x. P(T_{PC} \vdash \forall \underline{b}: A2 \gg \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b}; A1 \gg \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b}; MP \triangleright \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \triangleright \underline{b} \Rightarrow \underline{b} \gg \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b}; A1 \gg \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b}; MP \triangleright \underline{b} \Rightarrow \underline{b} \Rightarrow \underline{b} \triangleright \underline{b} \Rightarrow \underline{b} \gg \underline{b} \Rightarrow \underline{b}]$, p0, c]

A \TeX definitions

[$T_{PC} \xrightarrow{\text{tex}}$ “T_{\{-PC\}}”]

[$x \Rightarrow y \xrightarrow{\text{tex}}$ “#1.
 \Rightarrow #2.”]

[A1 $\xrightarrow{\text{tex}}$ “A1”]

[A2 $\xrightarrow{\text{tex}}$ “A2”]

[A3 $\xrightarrow{\text{tex}}$ “A3”]

[MP $\xrightarrow{\text{tex}}$ “MP”]

[LEMMA1.8 $\xrightarrow{\text{tex}}$ “LEMMA 1.8”]