

(*** MAKROER BEGYNDER ***)

$$[\text{ph}_1 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{ph}_1 \ddot{=} a_{\text{Ph}}]])]$$

$$[\text{ph}_2 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{ph}_2 \ddot{=} b_{\text{Ph}}]])]$$

$$[\text{ph}_3 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{ph}_3 \ddot{=} c_{\text{Ph}}]])]$$

$$[\text{ph}_4 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{ph}_4 \ddot{=} d_{\text{Ph}}]])]$$

$$[\text{ph}_5 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{ph}_5 \ddot{=} e_{\text{Ph}}]])]$$

$$[\text{ph}_6 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{ph}_6 \ddot{=} f_{\text{Ph}}]])]$$

$$[x \wedge y \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \wedge y \ddot{=} \dot{\neg}((x \Rightarrow \dot{\neg}(y)n))n]])]$$

$$[x \dot{\vee} y \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \dot{\vee} y \ddot{=} \dot{\neg}(x)n \Rightarrow y]])]$$

$$[x \Leftrightarrow y \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \Leftrightarrow y \ddot{=} (x \Rightarrow y) \wedge (y \Rightarrow x)])]$$

$$[x \neq y \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \neq y \ddot{=} \dot{\neg}(x==y)n]])]$$

$$[x \notin y \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \notin y \ddot{=} \dot{\neg}(x \in y)n]])]$$

$$[x \subseteq y \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \subseteq y \ddot{=} \forall(S1ob): ((S1ob) \in x \Rightarrow (S1ob) \in y)])]$$

$$[\{x\} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\{x\} \ddot{=} \{x, x\}]])]$$

$$[x \cup y \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \cup y \ddot{=} \cup\{\{x\}, \{y\}\}]])]$$

$$[x \cap y \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \cap y \ddot{=} \{\text{ph} \in x \cup y \mid \text{ph}_3 \in x \wedge \text{ph}_3 \in y\}]])]$$

$$[\langle x, y \rangle \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\langle x, y \rangle \ddot{=} \{\{x\}, \{x, y\}\}]])]$$

$$[r(x, y) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[r(x, y) \ddot{=} \langle x, y \rangle \in r]])]$$

$$[\text{RefRel}(r, x) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{RefRel}(r, x) \ddot{=} \forall s: (s \in x \Rightarrow r(s, s))]])]$$

$$[\text{SymRel}(r, x) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{SymRel}(r, x) \ddot{=} \forall s, t: (s \in x \Rightarrow t \in x \Rightarrow r(s, t) \Rightarrow r(t, s))]])]$$

$$[\text{TransRel}(r, x) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{TransRel}(r, x) \ddot{=} \forall s, t, u: (s \in x \Rightarrow t \in x \Rightarrow u \in x \Rightarrow r(s, t) \Rightarrow r(t, u) \Rightarrow r(s, u))]])]$$

$$[\text{EqRel}(r, x) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{EqRel}(r, x) \ddot{=} \text{RefRel}(r, x) \wedge \text{SymRel}(r, x) \wedge \text{TransRel}(r, x)]])]$$

$$[\mathcal{BS} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\mathcal{BS} \ddot{=} \text{bs}]])]$$

$$[\text{OBS} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{OBS} \ddot{=} \overline{\text{bs}}]])]$$

$$[[x \in \text{bs}]_r \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[x \in \text{bs}]_r \ddot{=} \{\text{ph} \in \text{bs} \mid r(\text{ph}_1, x)\}]])]$$

$$[\text{bs}/r \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{bs}/r \ddot{=} \{\text{ph} \in P(\text{bs}) \mid \text{Ex}_{20} \in \text{bs} \wedge [\text{Ex}_{20} \in \text{bs}]_r == \text{ph}_2\}]])]$$

$$[\text{Partition}(p, \text{bs}) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{Partition}(p, \text{bs}) \ddot{=} (\forall s: (s \in p \Rightarrow s \neq \emptyset)) \wedge (\forall s, t: (s \in p \Rightarrow t \in p \Rightarrow s \neq t \Rightarrow s \cap t == \emptyset)) \wedge \cup p == \text{bs}]])]$$

(*** EKSISTENS-VARIABLE ***)

$$[x^{\text{Ex}} \xrightarrow{\text{val}} x \stackrel{r}{=} [x_{\text{Ex}}]]$$

$$[\text{Ex}_1 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{Ex}_1 \ddot{=} a_{\text{Ex}}]])]$$

$$\begin{aligned}
& [Ex_2 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[Ex_2 \doteq b_{Ex}]])] \\
& [Ex_{10} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[Ex_{10} \doteq j_{Ex}]])] \\
& [Ex_{20} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[Ex_{20} \doteq t_{Ex}]])] \\
& \langle [a \equiv b | x ::= t]_{Ex} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\langle a \equiv b | x ::= t \rangle_{Ex} \doteq \\
& \langle [a] \equiv^0 [b] | [x] ::= [t] \rangle_{Ex}]]] \rangle
\end{aligned}$$

$$\langle [a \equiv^0 b | x ::= t]_{Ex} \xrightarrow{\text{val}} \lambda c. x^{Ex} \wedge \langle a \equiv^1 b | x ::= t \rangle_{Ex} \rangle$$

$$\begin{aligned}
& \langle [a \equiv^1 b | x ::= t]_{Ex} \xrightarrow{\text{val}} a!x!t! \\
& \text{If}(b \stackrel{r}{=} [\forall_{\text{obj}} u: v], F, \\
& \text{If}(b^{Ex} \wedge b \stackrel{t}{=} x, a \stackrel{t}{=} t, \text{If}(\\
& a \stackrel{r}{=} b, \langle a^t \equiv^* b^t | x ::= t \rangle_{Ex}, F)) \rangle
\end{aligned}$$

$$\langle [a \equiv^* b | x ::= t]_{Ex} \xrightarrow{\text{val}} b!x!t!\text{If}(a, T, \text{If}(\langle a^h \equiv^1 b^h | x ::= t \rangle_{Ex}, \langle a^t \equiv^* b^t | x ::= t \rangle_{Ex}, F)) \rangle$$

(** AKSIOMATISK SYSTEM **)

$$\begin{aligned}
& [\text{SystemQ} \xrightarrow{\text{stmt}} \forall(fx): \forall(fy): R((fx)) + R((fy)) == R((fy)) + R((fx)) \oplus \\
& \forall(fx): \forall(fy): \forall(fz): R((fx)) ** R((fy)) ** R((fz)) == R((fx)) ** R((fy)) ** R((fz)) \oplus \\
& \forall(fx): \forall(rx): \forall(ry): (rx) == (ry) \vdash (fx) \in (rx) \vdash (fx) \in (ry) \oplus \forall m: \text{UB}(01//02 * \\
& *xs[m] + +us[m], \text{SetOfReals}) \vdash xs[(m+1)] == xs[m] \oplus \forall x: \forall y: x \leq y \Rightarrow y \leq x \\
& \Rightarrow x = y \oplus \forall s: \forall x: \forall y: \dot{\vdash} (s \in \{x, y\}) \Rightarrow \dot{\vdash} (s == x) \wedge \dot{\vdash} (s == y) \Rightarrow \dot{\vdash} (s == \\
& x) \wedge \dot{\vdash} (s == y) \Rightarrow \dot{\vdash} (s \in \{x, y\}) \wedge \forall m: \forall n: n = 0 \vdash \text{BS}(m, n) = \text{rec}(1+1)(\text{exp})m \oplus \\
& \forall x: (x+0) = x \oplus \forall(fx): \forall(fy): R((fx)) == R((fy)) \vdash \text{SF}((fx), (fy)) \oplus \forall x: \forall y: x = \\
& y \Rightarrow x \leq y \oplus \forall a: \forall b: a \Rightarrow b \vdash a \vdash b \oplus \forall(fx): \forall(fy): \forall(fz): R((fx)) = R((fy)) \vdash \\
& R((fx)) + R((fz)) = R((fy)) + R((fz)) \oplus \forall(fx): R((fx)) + +R(0f) == \\
& R((fx)) \oplus \forall x: (x * 1) = x \oplus \forall a: \forall b: a \vdash b \oplus \forall(rx): \forall(ry): (rx) == (ry) \vdash (ry) == \\
& (rx) \oplus \forall m: \forall x: m = 0 \vdash x(\text{exp})m = 1 \oplus \forall x: \forall y: \forall z: 0 \leq z \Rightarrow x \leq y \Rightarrow \\
& (x * z) \leq (y * z) \oplus \forall(fx): R((fx)) ** R(1f) == R((fx)) \oplus \dot{\vdash} (0 = 1) \wedge \forall m: \text{Nat}(m) \Vdash 0 <= m \\
& \oplus \forall x: \forall y: \dot{\vdash} (x == y) \Rightarrow \forall_{\text{obj}} \dot{s}: \dot{\vdash} (\bar{s} \in x \Rightarrow \bar{s} \in y) \Rightarrow \dot{\vdash} (\bar{s} \in y \Rightarrow \bar{s} \in x) \wedge \forall m: \text{Nat}(m) \Vdash 0 <= m \\
& \oplus \forall x: \forall y: \forall z: (rx) == (ry) \vdash (ry) == (rz) \vdash (rx) == (rz) \oplus \\
& \forall x: \forall y: (x + y) = (y + x) \oplus \forall m: \forall(fx): \forall(fy): (fx) +_f (fy) [m] = ((fx)[m] + (fy)[m]) \oplus \\
& \forall(v1): \forall a: \forall b: \forall c: \langle b \equiv a | (v1) ::= 0 \rangle_{\text{Me}} \Vdash \langle c \equiv a | (v1) ::= ((v1) + 1) \rangle_{\text{Me}} \Vdash b \Rightarrow \\
& \forall_{\text{obj}} (v1): a \Rightarrow c \Rightarrow \forall_{\text{obj}} (v1): a \oplus \forall m: \forall n: n = 0 \vdash \text{USteleScope}(m, n) = \\
& |(\text{us}[m] + (-\text{uus}[(m+1)]))| \oplus \forall(fx): \forall(fy): \forall(fz): R((fx)) + R((fy)) + R((fz)) = \\
& R((fx)) + R((fy)) + R((fz)) \oplus \forall x: \forall y: (x * y) = (y * x) \oplus \forall(fx): \forall(fy): (fx) \in \\
& R((fy)) \vdash \text{SF}((fx), (fy)) \oplus \forall x: \forall y: \forall z: x = y \Rightarrow (x * z) = (y * z) \oplus \forall a: a \vdash a \oplus \\
& \forall m: \text{UB}(01//02 * *xs[m] + +us[m], \text{SetOfReals}) \vdash \text{us}[(m+1)] == \\
& 01//02 * *xs[m] + +us[m] \oplus \forall x: \forall y: \dot{\vdash} (x \leq y) \wedge \forall s: \forall x: \dot{\vdash} (s \in \\
& P(x) \Rightarrow \forall_{\text{obj}} \dot{s}: \bar{s} \in s \Rightarrow \bar{s} \in x \Rightarrow \dot{\vdash} (\forall_{\text{obj}} \dot{s}: \bar{s} \in s \Rightarrow \bar{s} \in x \Rightarrow s \in P(x)) \wedge \forall m: \text{Nat}(m) \Vdash 0 <= m \\
& \oplus \text{us}[0] == \text{xs}[0] + +R(1f) \oplus \forall x: x \leq x \oplus \forall s: \dot{\vdash} (s \in \emptyset) \wedge \forall x: (x + (-ux)) = 0 \oplus \\
& \forall x: \forall y: \forall z: x = y \Rightarrow x = z \Rightarrow y = z \oplus \forall m: \forall n: \dot{\vdash} (0 <= n) \Rightarrow \dot{\vdash} (\dot{\vdash} (0 = n) \wedge n) \wedge \forall m: \text{Nat}(m) \Vdash 0 <= m \\
& \oplus \text{USteleScope}(m, n) = |(\text{us}[(m+n)] + (-\text{uus}[(m+(n+1)]))| + \text{USteleScope}(m, (n+ \\
& (-u1)))) \oplus \forall(fx): \forall(fy): \forall(fz): R((fx)) +_f (fy) +_f (fz) == R((fx)) +_f (fy) +_f (fz) \oplus \\
& \forall x: \dot{\vdash} (x = 0) \wedge \dot{\vdash} (x * \text{rec}x) = 1 \oplus \forall a: \forall b: \dot{\vdash} (b) \wedge \dot{\vdash} (b) \Rightarrow a \vdash \dot{\vdash} (b) \wedge \dot{\vdash} (b) \Rightarrow \dot{\vdash} (a) \wedge \dot{\vdash} (b) \oplus
\end{aligned}$$

$$\begin{aligned}
& \forall(\underline{rx}):(\underline{rx}) == (\underline{rx}) \oplus \forall \underline{m}: \dot{\vdash} (\text{UB}(01//02 * \text{xs}[\underline{m}] + \text{us}[\underline{m}], \text{SetOfReals}))n \vdash \\
& \text{us}[\underline{m} + 1] == \text{us}[\underline{m}] \oplus \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: \underline{x} <= \underline{y} \Rightarrow (\underline{x} + \underline{z}) <= (\underline{y} + \underline{z}) \oplus \\
& \forall \underline{a}: \forall \underline{b}: \forall \underline{p}: \forall \underline{x}: \forall \underline{z}: \underline{p}^{\text{Ph}} \wedge (\underline{b} \equiv \underline{a} | \underline{p}: == \underline{z})_{\text{Ph}} \Vdash \dot{\vdash} (\underline{z} \in \{\text{ph} \in \underline{x} \mid \underline{a}\}) \Rightarrow \dot{\vdash} (\underline{z} \in \underline{x} \Rightarrow \\
& \dot{\vdash} (\underline{b})n)n \Rightarrow \dot{\vdash} (\dot{\vdash} (\underline{z} \in \underline{x} \Rightarrow \dot{\vdash} (\underline{b})n)n \Rightarrow \underline{z} \in \{\text{ph} \in \underline{x} \mid \underline{a}\})n)n \oplus \\
& \forall \underline{m}: \forall(\underline{fx}): \text{R}((\underline{fx})) + +(- - \text{R}((\underline{fx}))) == \text{R}(\text{Of}) \oplus \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: (\underline{x} * (\underline{y} + \underline{z})) = \\
& ((\underline{x} * \underline{y}) + (\underline{x} * \underline{z})) \oplus \forall \underline{m}: \forall \underline{n}: \text{Nat}(\underline{m}) \Vdash \text{Nat}(\underline{n}) \Vdash \dot{\vdash} (\underline{m} <= (\underline{n} + 1)) \Rightarrow \dot{\vdash} (\dot{\vdash} (\underline{m} = \\
& (\underline{n} + 1))n)n)n \vdash \underline{m} <= \underline{n} \oplus \forall \underline{x}: \forall \underline{t}: \forall \underline{a}: \forall \underline{b}: \langle \underline{a} \equiv^0 \underline{b} \mid \underline{x}: == \underline{t} \rangle_{\text{Ex}} \Vdash \underline{a} \vdash \underline{b} \oplus \\
& \forall \underline{m}: \forall \underline{x}: \dot{\vdash} (0 <= \underline{m} \Rightarrow \dot{\vdash} (\dot{\vdash} (0 = \underline{m})n)n)n \vdash \underline{x}(\text{exp})\underline{m} = \\
& (\underline{x} * \underline{x}(\text{exp})(\underline{m} + (-u1))) \oplus \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: ((\underline{x} + \underline{y}) + \underline{z}) = (\underline{x} + (\underline{y} + \underline{z})) \oplus \\
& \forall(\underline{v1}): \forall(\underline{v2}): \forall \underline{n}: \forall(\underline{\epsilon}): \forall(\underline{fx}): \forall_{\text{obj}}(\underline{\epsilon}): \dot{\vdash} (\forall_{\text{obj}} \underline{n}: \dot{\vdash} (\forall_{\text{obj}}(\underline{v1}): \forall_{\text{obj}}(\underline{v2}): \dot{\vdash} (0 <= \\
& (\underline{\epsilon}) \Rightarrow \dot{\vdash} (\dot{\vdash} (0 = (\underline{\epsilon}))n)n)n \Rightarrow \underline{n} <= (\underline{v1}) \Rightarrow \underline{n} <= (\underline{v2}) \Rightarrow \\
& \dot{\vdash} (((\underline{fx})[(\underline{v1})] + (-u(\underline{fx})[(\underline{v2})]))) <= (\underline{\epsilon}) \Rightarrow \dot{\vdash} (\dot{\vdash} (((\underline{fx})[(\underline{v1})] + (-u(\underline{fx})[(\underline{v2})]))) = \\
& (\underline{\epsilon}))n)n)n)n \oplus \forall \underline{x}: \forall(\underline{v1}): \forall \underline{a}: \forall \underline{b}: \langle \underline{a} \equiv \underline{b} \mid (\underline{v1}): == \underline{x} \rangle_{\text{Me}} \Vdash \forall_{\text{obj}}(\underline{v1}): \underline{b} \Rightarrow \underline{a} \oplus \\
& \forall \underline{m}: \forall \underline{n}: \dot{\vdash} (0 <= \underline{n} \Rightarrow \dot{\vdash} (\dot{\vdash} (0 = \underline{n})n)n) \vdash \text{BS}(\underline{m}, \underline{n}) = \\
& (\text{rec}(1 + 1)(\text{exp})(\underline{m} + \underline{n}) + \text{BS}(\underline{m}, (\underline{n} + (-u1)))) \oplus \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: ((\underline{x} * \underline{y}) * \underline{z}) = \\
& (\underline{x} * (\underline{y} * \underline{z})) \oplus \forall(\underline{fx}): \forall(\underline{fy}): \text{SF}((\underline{fx}), (\underline{fy})) \vdash \text{R}((\underline{fx})) == \text{R}((\underline{fy})) \oplus \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: \underline{x} = \\
& \underline{y} \Rightarrow (\underline{x} + \underline{z}) = (\underline{y} + \underline{z}) \oplus \forall \underline{x}: \forall \underline{a}: \underline{a} \vdash \forall_{\text{obj}} \underline{x}: \underline{a} \oplus \\
& \forall \underline{m}: \dot{\vdash} (\text{UB}(01//02 * \text{xs}[\underline{m}] + \text{us}[\underline{m}], \text{SetOfReals}))n \vdash \text{xs}[\underline{m} + 1] == \\
& 01//02 * \text{xs}[\underline{m}] + \text{us}[\underline{m}] \oplus \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: \underline{x} <= \underline{y} \Rightarrow \underline{y} <= \underline{z} \Rightarrow \underline{x} <= \underline{z} \oplus \\
& \forall \underline{s}: \forall \underline{x}: \dot{\vdash} (\underline{s} \in \cup \underline{x} \Rightarrow \dot{\vdash} (\underline{s} \in \text{j}_{\text{Ex}} \Rightarrow \dot{\vdash} (\text{j}_{\text{Ex}} \in \underline{x})n)n \Rightarrow \dot{\vdash} (\dot{\vdash} (\underline{s} \in \text{j}_{\text{Ex}} \Rightarrow \dot{\vdash} (\text{j}_{\text{Ex}} \in \\
& \underline{x})n)n \Rightarrow \underline{s} \in \cup \underline{x})n)n \oplus \forall(\underline{fx}): \forall(\underline{fy}): \text{R}((\underline{fx})) * * \text{R}((\underline{fy})) == \text{R}((\underline{fy})) * * \text{R}((\underline{fx})) \oplus \\
& \forall(\underline{fx}): \forall(\underline{rx}): \forall(\underline{ry}): (\underline{rx}) == (\underline{ry}) \vdash (\underline{fx}) \in (\underline{ry}) \vdash (\underline{fx}) \in (\underline{rx})]
\end{aligned}$$

$$[\text{MP} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{a}: \forall \underline{b}: \underline{a} \Rightarrow \underline{b} \vdash \underline{a} \vdash \underline{b}][\text{MP} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

$$[\text{Gen} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{x}: \forall \underline{a}: \underline{a} \vdash \forall_{\text{obj}} \underline{x}: \underline{a}][\text{Gen} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

$$[\text{Repetition} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{a}: \underline{a} \vdash \underline{a}][\text{Repetition} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

$$[\text{Neg} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{a}: \forall \underline{b}: \dot{\vdash} (\underline{b})n \Rightarrow \underline{a} \vdash \dot{\vdash} (\underline{b})n \Rightarrow \dot{\vdash} (\underline{a})n \vdash \underline{b}][\text{Neg} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

$$[\text{Ded} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{a}: \forall \underline{b}: \underline{a} \vdash \underline{b}][\text{Ded} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

$$[\text{ExistIntro} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{x}: \forall \underline{t}: \forall \underline{a}: \forall \underline{b}: \langle \underline{a} \equiv^0 \underline{b} \mid \underline{x}: == \underline{t} \rangle_{\text{Ex}} \Vdash \underline{a} \vdash \underline{b}][\text{ExistIntro} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

$$[\text{Extensionality} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{x}: \forall \underline{y}: \dot{\vdash} (\underline{x} == \underline{y} \Rightarrow \forall_{\text{obj}} \underline{s}: \dot{\vdash} (\underline{s} \in \underline{x} \Rightarrow \underline{s} \in \underline{y} \Rightarrow \dot{\vdash} (\underline{s} \in \underline{y} \Rightarrow \underline{s} \in \underline{x})n)n \Rightarrow \dot{\vdash} (\forall_{\text{obj}} \underline{s}: \dot{\vdash} (\underline{s} \in \underline{x} \Rightarrow \underline{s} \in \underline{y} \Rightarrow \dot{\vdash} (\underline{s} \in \underline{y} \Rightarrow \underline{s} \in \underline{x})n)n \Rightarrow \underline{x} == \underline{y})n)n][\text{Extensionality} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

$$[\text{Odef} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{s}: \dot{\vdash} (\underline{s} \in \emptyset)n][\text{Odef} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

$$[\text{PairDef} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{s}: \forall \underline{x}: \forall \underline{y}: \dot{\vdash} (\underline{s} \in \{\underline{x}, \underline{y}\}) \Rightarrow \dot{\vdash} (\underline{s} == \underline{x})n \Rightarrow \underline{s} == \underline{y} \Rightarrow \dot{\vdash} (\dot{\vdash} (\underline{s} == \underline{x})n \Rightarrow \underline{s} == \underline{y} \Rightarrow \underline{s} \in \{\underline{x}, \underline{y}\})n)n][\text{PairDef} \xrightarrow{\text{proof}} \text{Rule tactic}]$$

[UnionDef $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{s}: \forall \underline{x}: \dot{\vdash} (\underline{s} \in \cup \underline{x} \Rightarrow \dot{\vdash} (\underline{s} \in \text{j}_{\text{Ex}} \Rightarrow \dot{\vdash} (\text{j}_{\text{Ex}} \in \underline{x})n)n \Rightarrow \dot{\vdash} (\underline{s} \in \text{j}_{\text{Ex}} \Rightarrow \dot{\vdash} (\text{j}_{\text{Ex}} \in \underline{x})n)n) \Rightarrow \underline{s} \in \cup \underline{x})n)n]$ [UnionDef $\xrightarrow{\text{proof}}$ Rule tactic]

[PowerDef $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{s}: \forall \underline{x}: \dot{\vdash} (\underline{s} \in \text{P}(\underline{x}) \Rightarrow \forall \text{obj} \bar{s}: \bar{s} \in \underline{s} \Rightarrow \bar{s} \in \underline{x} \Rightarrow \dot{\vdash} (\forall \text{obj} \bar{s}: \bar{s} \in \underline{s} \Rightarrow \bar{s} \in \underline{x} \Rightarrow \underline{s} \in \text{P}(\underline{x}))n)n)]$ [PowerDef $\xrightarrow{\text{proof}}$ Rule tactic]

[SeparationDef $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{a}: \forall \underline{b}: \forall \underline{p}: \forall \underline{x}: \forall \underline{z}: \underline{p}^{\text{Ph}} \wedge \langle \underline{b} \equiv \underline{a} | \underline{p} := \underline{z} \rangle_{\text{Ph}} \Vdash \dot{\vdash} (\underline{z} \in \{\text{ph} \in \underline{x} \mid \underline{a}\} \Rightarrow \dot{\vdash} (\underline{z} \in \underline{x} \Rightarrow \dot{\vdash} (\underline{b})n)n \Rightarrow \dot{\vdash} (\dot{\vdash} (\underline{z} \in \underline{x} \Rightarrow \dot{\vdash} (\underline{b})n)n \Rightarrow \underline{z} \in \{\text{ph} \in \underline{x} \mid \underline{a}\})n)n)]$ [SeparationDef $\xrightarrow{\text{proof}}$ Rule tactic]

————— RRRRRRRRRRRRRRRR —————

(** import fra A.M. **)

[TimesCommutativity(R) $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall (\underline{fx}): \forall (\underline{fy}): \text{R}(\underline{(fx)}) * \text{R}(\underline{(fy)}) == \text{R}(\underline{(fy)}) * \text{R}(\underline{(fx)})]$ [TimesCommutativity(R) $\xrightarrow{\text{proof}}$ Rule tactic]

(** aksiomer **)

[leqReflexivity $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \underline{x} <= \underline{x}]$ [leqReflexivity $\xrightarrow{\text{proof}}$ Rule tactic]

[leqAntisymmetryAxiom $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \underline{x} <= \underline{y} \Rightarrow \underline{y} <= \underline{x} \Rightarrow \underline{x} = \underline{y}]$ [leqAntisymmetryAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[leqTransitivityAxiom $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: \underline{x} <= \underline{y} \Rightarrow \underline{y} <= \underline{z} \Rightarrow \underline{x} <= \underline{z}]$ [leqTransitivityAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[leqTotality $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \dot{\vdash} (\underline{x} <= \underline{y})n \Rightarrow \underline{y} <= \underline{x}]$ [leqTotality $\xrightarrow{\text{proof}}$ Rule tactic]

[leqAdditionAxiom $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: \underline{x} <= \underline{y} \Rightarrow (\underline{x} + \underline{z}) <= (\underline{y} + \underline{z})]$ [leqAdditionAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[leqMultiplicationAxiom $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: 0 <= \underline{z} \Rightarrow \underline{x} <= \underline{y} \Rightarrow (\underline{x} * \underline{z}) <= (\underline{y} * \underline{z})]$ [leqMultiplicationAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[plusAssociativity $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: ((\underline{x} + \underline{y}) + \underline{z}) = (\underline{x} + (\underline{y} + \underline{z}))]$ [plusAssociativity $\xrightarrow{\text{proof}}$ Rule tactic]

[plusCommutativity $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: (\underline{x} + \underline{y}) = (\underline{y} + \underline{x})]$ [plusCommutativity $\xrightarrow{\text{proof}}$ Rule tactic]

[Negative $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: (\underline{x} + (-\underline{ux})) = 0]$ [Negative $\xrightarrow{\text{proof}}$ Rule tactic]

[plus0 $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: (\underline{x} + 0) = \underline{x}]$ [plus0 $\xrightarrow{\text{proof}}$ Rule tactic]

[timesAssociativity $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: ((\underline{x} * \underline{y}) * \underline{z}) = (\underline{x} * (\underline{y} * \underline{z}))]$ [timesAssociativity $\xrightarrow{\text{proof}}$ Rule tactic]

[timesCommutativity $\xrightarrow{\text{stmtt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: (\underline{x} * \underline{y}) = (\underline{y} * \underline{x})]$ [timesCommutativity $\xrightarrow{\text{proof}}$ Rule tactic]

[ReciprocalAxiom $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{x}: \dot{\neg}(\underline{x} = 0)n \Rightarrow (\underline{x} * \text{recx}) = 1$][ReciprocalAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[times1 $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{x}: (\underline{x} * 1) = \underline{x}$][times1 $\xrightarrow{\text{proof}}$ Rule tactic]

[Distribution $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: (\underline{x} * (\underline{y} + \underline{z})) = ((\underline{x} * \underline{y}) + (\underline{x} * \underline{z}))$][Distribution $\xrightarrow{\text{proof}}$ Rule tactic]

[0not1 $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \dot{\neg}(0 = 1)n$][0not1 $\xrightarrow{\text{proof}}$ Rule tactic]

[EqualityAxiom $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: \underline{x} = \underline{y} \Rightarrow \underline{x} = \underline{z} \Rightarrow \underline{y} = \underline{z}$][EqualityAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[EqLeqAxiom $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \underline{x} = \underline{y} \Rightarrow \underline{x} <= \underline{y}$][EqLeqAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[EqAdditionAxiom $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: \underline{x} = \underline{y} \Rightarrow (\underline{x} + \underline{z}) = (\underline{y} + \underline{z})$][EqAdditionAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[EqMultiplicationAxiom $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{x}: \forall \underline{y}: \forall \underline{z}: \underline{x} = \underline{y} \Rightarrow (\underline{x} * \underline{z}) = (\underline{y} * \underline{z})$][EqMultiplicationAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[A4(Axiom) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{x}: \forall (\underline{v1}): \forall \underline{a}: \forall \underline{b}: \langle \underline{a} \equiv \underline{b} | (\underline{v1}) \rangle == \underline{x}$] $\text{Me} \vdash$

$\forall \text{obj}(\underline{v1}): \underline{b} \Rightarrow \underline{a}$][A4(Axiom) $\xrightarrow{\text{proof}}$ Rule tactic]
 (***) XX snydeaksiomer (***)

[== Reflexivity $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall (\underline{rx}): (\underline{rx}) == (\underline{rx})$][== Reflexivity $\xrightarrow{\text{proof}}$ Rule tactic]

[== Symmetry $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall (\underline{rx}): \forall (\underline{ry}): (\underline{rx}) == (\underline{ry}) \vdash (\underline{ry}) == (\underline{rx})$][== Symmetry $\xrightarrow{\text{proof}}$ Rule tactic]

[== Transitivity $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall (\underline{rx}): \forall (\underline{ry}): \forall (\underline{rz}): (\underline{rx}) == (\underline{ry}) \vdash (\underline{ry}) == (\underline{rz}) \vdash (\underline{rx}) == (\underline{rz})$][== Transitivity $\xrightarrow{\text{proof}}$ Rule tactic]

XX ikke 100procent identisk med originalen fra equivalence-relations

[SENC1 $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall (\underline{fx}): \forall (\underline{rx}): \forall (\underline{ry}): (\underline{rx}) == (\underline{ry}) \vdash (\underline{fx}) \in (\underline{rx}) \vdash (\underline{fx}) \in (\underline{ry})$][SENC1 $\xrightarrow{\text{proof}}$ Rule tactic]

XX boer bevises ud fra nummer 1

[SENC2 $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall (\underline{fx}): \forall (\underline{rx}): \forall (\underline{ry}): (\underline{rx}) == (\underline{ry}) \vdash (\underline{fx}) \in (\underline{ry}) \vdash (\underline{fx}) \in (\underline{rx})$][SENC2 $\xrightarrow{\text{proof}}$ Rule tactic]

[PlusF $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \forall (\underline{fx}): \forall (\underline{fy}): (\underline{fx}) +_f (\underline{fy}) [\underline{m}] = ((\underline{fx})[\underline{m}] + (\underline{fy})[\underline{m}])$][PlusF $\xrightarrow{\text{proof}}$ Rule tactic]

[From == $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall (\underline{fx}): \forall (\underline{fy}): R((\underline{fx})) == R((\underline{fy})) \vdash SF((\underline{fx}), (\underline{fy}))$][From == $\xrightarrow{\text{proof}}$ Rule tactic]

[To == $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall (\underline{fx}): \forall (\underline{fy}): SF((\underline{fx}), (\underline{fy})) \vdash R((\underline{fx})) == R((\underline{fy}))$][To == $\xrightarrow{\text{proof}}$ Rule tactic]

$[\text{FromInR} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall(\underline{\text{fx}}): \forall(\underline{\text{fy}}): \underline{(\text{fx})} \in \text{R}(\underline{(\text{fy})})] \vdash$

$\text{SF}(\underline{(\text{fx})}, \underline{(\text{fy})})[\text{FromInR} \xrightarrow{\text{proof}} \text{Rule tactic}]$

$(*** \text{makroer} ***)$

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$[\text{M}_1 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{M}_1 \doteq \underline{(\text{m1})}]])]$

$[\text{M}_2 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{M}_2 \doteq \underline{(\text{m2})}]])]$

$[\text{N}_1 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{N}_1 \doteq \underline{(\text{n1})}]])]$

$[\text{N}_2 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{N}_2 \doteq \underline{(\text{n2})}]])]$

$[\text{N}_3 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{N}_3 \doteq \underline{(\text{n3})}]])]$

$[\epsilon \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\epsilon \doteq \underline{(\epsilon)}]])]$

$[\epsilon_1 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\epsilon_1 \doteq \underline{(\epsilon)_1}]])]$

$[\epsilon_2 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\epsilon_2 \doteq \underline{(\epsilon)_2}]])]$

$[\text{X}_1 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{X}_1 \doteq \underline{(\text{x1})}]])]$

$[\text{X}_2 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{X}_2 \doteq \underline{(\text{x2})}]])]$

$[\text{Y}_1 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{Y}_1 \doteq \underline{(\text{y1})}]])]$

$[\text{Y}_2 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{Y}_2 \doteq \underline{(\text{y2})}]])]$

$[\text{V}_1 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{V}_1 \doteq \underline{(\text{v1})}]])]$

$[\text{V}_2 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{V}_2 \doteq \underline{(\text{v2})}]])]$

$[\text{V}_3 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{V}_3 \doteq \underline{(\text{v3})}]])]$

$[\text{V}_4 \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{V}_4 \doteq \underline{(\text{v4})}]])]$

$[\text{V}_{2n} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{V}_{2n} \doteq \underline{(\text{v2n})}]])]$

$[\text{FX} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{FX} \doteq \underline{(\text{fx})}]])]$

$[\text{FY} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{FY} \doteq \underline{(\text{fy})}]])]$

$[\text{FZ} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{FZ} \doteq \underline{(\text{fz})}]])]$

$[\text{FU} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{FU} \doteq \underline{(\text{fu})}]])]$

$[\text{FV} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{FV} \doteq \underline{(\text{fv})}]])]$

$[\text{FW} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{FW} \doteq \underline{(\text{fw})}]])]$

$[\text{FEP} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{FEP} \doteq \underline{(\text{fep})}]])]$

$[\text{RX} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{RX} \doteq \underline{(\text{rx})}]])]$

$[\text{RY} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{RY} \doteq \underline{(\text{ry})}]])]$

$[\text{RZ} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{RZ} \doteq \underline{(\text{rz})}]])]$

$[\text{RU} \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[\text{RU} \doteq \underline{(\text{ru})}]])]$

$[(\text{SX}) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[(\text{SX}) \doteq \underline{(\text{sx})}]])]$

$[(\text{SX1}) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[(\text{SX1}) \doteq \underline{(\text{sx1})}]])]$

$[(\text{SY}) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[(\text{SY}) \doteq \underline{(\text{sy})}]])]$

$[(\text{SY1}) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [[(\text{SY1}) \doteq \underline{(\text{sy1})}]])]$

$[(SZ) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(SZ) \doteq (\underline{sz})]])]$
 $[(SZ1) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(SZ1) \doteq (\underline{sz1})]])]$
 $[(SU) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(SU) \doteq (\underline{su})]])]$
 $[(SU1) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(SU1) \doteq (\underline{su1})]])]$
 $[FXS \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[FXS \doteq (\underline{fxs})]])]$
 $[FYS \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[FYS \doteq (\underline{fys})]])]$
 $[(F1) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(F1) \doteq (\underline{f1})]])]$
 $[(F2) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(F2) \doteq (\underline{f2})]])]$
 $[(F3) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(F3) \doteq (\underline{f3})]])]$
 $[(F4) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(F4) \doteq (\underline{f4})]])]$
 $[(OP1) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(OP1) \doteq (\underline{op1})]])]$
 $[(OP2) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(OP2) \doteq (\underline{op2})]])]$
 $[(R1) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(R1) \doteq (\underline{r1})]])]$
 $[(S1) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(S1) \doteq (\underline{s1})]])]$
 $[(S2) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(S2) \doteq (\underline{s2})]])]$
 $[(EPob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(EPob) \doteq (\underline{\epsilon})]])]$
 $[(CRS1ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(CRS1ob) \doteq (\underline{crs1})]])]$
 $[(F1ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(F1ob) \doteq (\underline{f1})]])]$
 $[(F2ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(F2ob) \doteq (\underline{f2})]])]$
 $[(F3ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(F3ob) \doteq (\underline{f3})]])]$
 $[(F4ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(F4ob) \doteq (\underline{f4})]])]$
 $[(N1ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(N1ob) \doteq (\underline{n1})]])]$
 $[(N2ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(N2ob) \doteq (\underline{n2})]])]$
 $[(OP1ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(OP1ob) \doteq (\underline{op1})]])]$
 $[(OP2ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(OP2ob) \doteq (\underline{op2})]])]$
 $[(R1ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(R1ob) \doteq (\underline{r1})]])]$
 $[(S1ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(S1ob) \doteq (\underline{s1})]])]$
 $[(S2ob) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(S2ob) \doteq (\underline{s2})]])]$
 $[(fx) \leq_f (fy) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(fx) \leq_f (fy) \doteq (fx) <_f (fy) \dot{\vee} SF((fx), (fy))]])]$
 $[Ex3 \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[Ex3 \doteq c_{Ex}]])]$
 $[\exists(v1): a \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[\exists(v1): a \doteq \dot{\vee} (\forall(v1): \dot{\vee} (a)n)n]])]$
 $[x <<== y \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[x <<== y \doteq x << y \dot{\vee} x == y]])]$
 $[(-1) \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[(-1) \doteq (-u1)])]]]$
 $[2 \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[2 \doteq (1 + 1)])]]]$
 $[3 \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[3 \doteq (2 + 1)])]]]$
 $[1/2 \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[1/2 \doteq \text{rec2}]])]]$
 $[1/3 \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[1/3 \doteq \text{rec3}]])]]$
 $[2/3 \xrightarrow{\text{macro}} \lambda t.\lambda s.\lambda c.\tilde{\mathcal{M}}_4(t, s, c, [[2/3 \doteq (2 * 1/3)])]]]$

[FromNegated(2 * Imply) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: \dot{\neg}(\underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c}) \vdash \dot{\neg}(\dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})\text{n})\text{n} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{c})\text{n})\text{n})$]

[FromNegated(2 * Imply) $\xrightarrow{\text{proof}}$ $\lambda c. \lambda x. \mathcal{P}(\lceil \text{SystemQ} \vdash \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: \dot{\neg}(\underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c}) \text{n} \vdash \text{FromNegatedImply} \triangleright \dot{\neg}(\underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c})\text{n} \gg \dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b} \Rightarrow \underline{c})\text{n})\text{n}) \gg \underline{a}$; SecondConjunct $\triangleright \dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b} \Rightarrow \underline{c})\text{n})\text{n}) \gg \dot{\neg}(\underline{b} \Rightarrow \underline{c})\text{n}$; FromNegatedImply $\triangleright \dot{\neg}(\underline{b} \Rightarrow \underline{c})\text{n} \gg \dot{\neg}(\underline{b} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{c})\text{n})\text{n})$; FirstConjunct $\triangleright \dot{\neg}(\underline{b} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{c})\text{n})\text{n}) \gg \underline{b}$; SecondConjunct $\triangleright \dot{\neg}(\underline{b} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{c})\text{n})\text{n}) \gg \dot{\neg}(\underline{c})\text{n}$; JoinConjuncts $\triangleright \underline{a} \triangleright \underline{b} \gg \dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})\text{n})\text{n}$; JoinConjuncts $\triangleright \dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})\text{n})\text{n} \triangleright \dot{\neg}(\underline{c})\text{n} \gg \dot{\neg}(\dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})\text{n})\text{n} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{c})\text{n})\text{n})$, p_0, c]

[FromNegatedOr $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{a}: \forall \underline{b}: \dot{\neg}(\dot{\neg}(\underline{a})\text{n} \Rightarrow \underline{b})\text{n} \vdash \dot{\neg}(\dot{\neg}(\underline{a})\text{n} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})\text{n})\text{n})$]

[FromNegatedOr $\xrightarrow{\text{proof}}$ $\lambda c. \lambda x. \mathcal{P}(\lceil \text{SystemQ} \vdash \forall \underline{a}: \forall \underline{b}: \dot{\neg}(\dot{\neg}(\underline{a})\text{n} \Rightarrow \underline{b})\text{n} \vdash \text{Repetition} \triangleright \dot{\neg}(\dot{\neg}(\underline{a})\text{n} \Rightarrow \underline{b})\text{n} \gg \dot{\neg}(\dot{\neg}(\underline{a})\text{n} \Rightarrow \underline{b})\text{n}$; FromNegatedImply $\triangleright \dot{\neg}(\dot{\neg}(\underline{a})\text{n} \Rightarrow \underline{b})\text{n} \gg \dot{\neg}(\dot{\neg}(\underline{a})\text{n} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})\text{n})\text{n})$, p_0, c]

[InductionAxiom $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall (\underline{v1}): \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: \langle \underline{b} \equiv \underline{a} \mid (\underline{v1}) := 0 \rangle_{\text{Me}} \Vdash \langle \underline{c} \equiv \underline{a} \mid (\underline{v1}) := ((\underline{v1}) + 1) \rangle_{\text{Me}} \Vdash \underline{b} \Rightarrow \forall_{\text{obj}}(\underline{v1}): \underline{a} \Rightarrow \underline{c} \Rightarrow$

$\forall_{\text{obj}}(\underline{v1}): \underline{a}$] [InductionAxiom $\xrightarrow{\text{proof}}$ Rule tactic]

[LessMinus1(N) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \forall \underline{n}: \text{Nat}(\underline{m}) \Vdash \text{Nat}(\underline{n}) \Vdash \dot{\neg}(\underline{m} <= (\underline{n} + 1) \Rightarrow \dot{\neg}(\dot{\neg}(\underline{m} = (\underline{n} + 1))\text{n})\text{n}) \vdash \underline{m} <= \underline{n}$] [LessMinus1(N) $\xrightarrow{\text{proof}}$ Rule tactic]

[Nonnegative(N) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \text{Nat}(\underline{m}) \Vdash 0 <= \underline{m}$] [Nonnegative(N) $\xrightarrow{\text{proof}}$ Rule tactic]

[Cauchy $\xrightarrow{\text{stmt}}$ SystemQ \vdash

$\forall (\underline{v1}): \forall (\underline{v2}): \forall \underline{n}: \forall (\underline{\epsilon}): \forall (\underline{fx}): \forall_{\text{obj}}(\underline{\epsilon}): \dot{\neg}(\forall_{\text{obj}} \underline{n}: \dot{\neg}(\forall_{\text{obj}}(\underline{v1}): \forall_{\text{obj}}(\underline{v2}): \dot{\neg}(0 <= (\underline{\epsilon}) \Rightarrow \dot{\neg}(\dot{\neg}(0 = (\underline{\epsilon})\text{n})\text{n})\text{n} \Rightarrow \underline{n} <= (\underline{v1}) \Rightarrow \underline{n} <= (\underline{v2}) \Rightarrow \dot{\neg}(\lvert ((\underline{fx})[(\underline{v1})] + (-\underline{u}(\underline{fx})[(\underline{v2})])) \rvert <= (\underline{\epsilon})) \Rightarrow$

$\dot{\neg}(\dot{\neg}(\lvert ((\underline{fx})[(\underline{v1})] + (-\underline{u}(\underline{fx})[(\underline{v2})])) \rvert = (\underline{\epsilon})\text{n})\text{n})\text{n})\text{n})$] [Cauchy $\xrightarrow{\text{proof}}$ Rule tactic]

[JoinConjuncts(2conditions) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: \forall \underline{d}: \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c} \vdash \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{d} \vdash \underline{a} \Rightarrow \underline{b} \Rightarrow \dot{\neg}(\underline{c} \Rightarrow \dot{\neg}(\underline{d})\text{n})\text{n}$]

[JoinConjuncts(2conditions) $\xrightarrow{\text{proof}}$ $\lambda c. \lambda x. \mathcal{P}(\lceil \text{SystemQ} \vdash \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: \forall \underline{d}: \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c} \vdash \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{d} \vdash \underline{a} \vdash \underline{b} \vdash \text{MP2} \triangleright \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c} \triangleright \underline{a} \triangleright \underline{b} \gg \underline{c}$; MP2 $\triangleright \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{d} \triangleright \underline{a} \triangleright \underline{b} \gg \underline{d}$; JoinConjuncts $\triangleright \underline{c} \triangleright \underline{d} \gg \dot{\neg}(\underline{c} \Rightarrow \dot{\neg}(\underline{d})\text{n})\text{n}$; $\forall \underline{a}: \forall \underline{b}: \forall \underline{c}: \forall \underline{d}: \text{Ded} \triangleright \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: \forall \underline{d}: \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c} \vdash \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{d} \vdash \underline{a} \vdash \underline{b} \vdash \dot{\neg}(\underline{c} \Rightarrow \dot{\neg}(\underline{d})\text{n})\text{n} \gg \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c} \Rightarrow \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{d} \Rightarrow \underline{a} \Rightarrow \underline{b} \Rightarrow \dot{\neg}(\underline{c} \Rightarrow \dot{\neg}(\underline{d})\text{n})\text{n}$; $\underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c} \vdash \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{d} \vdash \text{MP2} \triangleright \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c} \Rightarrow \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{d} \Rightarrow \underline{a} \Rightarrow \underline{b} \Rightarrow \dot{\neg}(\underline{c} \Rightarrow \dot{\neg}(\underline{d})\text{n})\text{n} \triangleright \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{c} \triangleright \underline{a} \Rightarrow \underline{b} \Rightarrow \underline{d} \gg \underline{a} \Rightarrow \underline{b} \Rightarrow \dot{\neg}(\underline{c} \Rightarrow \dot{\neg}(\underline{d})\text{n})\text{n}$, p_0, c]

[FromNegatedAnd $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{a}: \forall \underline{b}: \dot{\neg}(\dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})\text{n})\text{n}) \vdash \underline{a} \vdash \dot{\neg}(\underline{b})\text{n}$]

[FromNegatedAnd $\xrightarrow{\text{proof}}$ $\lambda c. \lambda x. \mathcal{P}(\lceil \text{SystemQ} \vdash \forall \underline{a}: \forall \underline{b}: \dot{\neg}(\dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})\text{n})\text{n}) \vdash \underline{a} \vdash$

Repetition $\triangleright \dot{\neg}(\dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})n)n) \gg \dot{\neg}(\dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})n)n)n$; RemoveDoubleNeg $\triangleright \dot{\neg}(\dot{\neg}(\underline{a} \Rightarrow \dot{\neg}(\underline{b})n)n) \gg \underline{a} \Rightarrow \dot{\neg}(\underline{b})n$; MP $\triangleright \underline{a} \Rightarrow \dot{\neg}(\underline{b})n \triangleright \underline{a} \gg \dot{\neg}(\underline{b})n$, p_0, c]

[ToNegatedOr $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{a}: \forall \underline{b}: \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \vdash \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \underline{b})n$]

[ToNegatedOr $\xrightarrow{\text{proof}}$ $\lambda c. \lambda x. \mathcal{P}([\text{SystemQ} \vdash \forall \underline{a}: \forall \underline{b}: \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \vdash \dot{\neg}(\underline{a})n \Rightarrow \underline{b}] \vdash \text{FirstConjunct} \triangleright \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \gg \dot{\neg}(\underline{a})n$; SecondConjunct $\triangleright \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \gg \dot{\neg}(\underline{b})n$; NegateDisjunct1 $\triangleright \dot{\neg}(\underline{a})n \Rightarrow \underline{b} \triangleright \dot{\neg}(\underline{a})n \gg \underline{b}$; FromContradiction $\triangleright \underline{b} \triangleright \dot{\neg}(\underline{b})n \gg \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \underline{b})n$; $\forall \underline{a}: \forall \underline{b}: \text{Ded} \triangleright \forall \underline{a}: \forall \underline{b}: \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \vdash \dot{\neg}(\underline{a})n \Rightarrow \underline{b} \vdash \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \underline{b})n \gg \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \Rightarrow \dot{\neg}(\underline{a})n \Rightarrow \underline{b} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \underline{b})n$; $\dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \vdash \text{MP} \triangleright \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \Rightarrow \dot{\neg}(\underline{a})n \Rightarrow \underline{b} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \underline{b})n \triangleright \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \dot{\neg}(\dot{\neg}(\underline{b})n)n) \gg \dot{\neg}(\underline{a})n \Rightarrow \underline{b} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \underline{b})n$; prop lemma imply negation $\triangleright \dot{\neg}(\underline{a})n \Rightarrow \underline{b} \Rightarrow \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \underline{b})n \gg \dot{\neg}(\dot{\neg}(\underline{a})n \Rightarrow \underline{b})n$, p_0, c]

[NextXS(UpperBound) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \text{UB}(01//02 * *xs[\underline{m}] + +us[\underline{m}], \text{SetOfReals}) \vdash xs[(\underline{m} + 1)] == xs[\underline{m}]$] [NextXS(UpperBound) $\xrightarrow{\text{proof}}$ Rule tactic]

[NextXS(NoUpperBound) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \dot{\neg}(\text{UB}(01//02 * *xs[\underline{m}] + +us[\underline{m}], \text{SetOfReals}))n \vdash xs[(\underline{m} + 1)] == 01//02 * *xs[\underline{m}] + +us[\underline{m}]$] [NextXS(NoUpperBound) $\xrightarrow{\text{proof}}$ Rule tactic]

[NextUS(UpperBound) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \text{UB}(01//02 * *xs[\underline{m}] + +us[\underline{m}], \text{SetOfReals}) \vdash us[(\underline{m} + 1)] == 01//02 * *xs[\underline{m}] + +us[\underline{m}]$] [NextUS(UpperBound) $\xrightarrow{\text{proof}}$ Rule tactic]

[NextUS(NoUpperBound) $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \dot{\neg}(\text{UB}(01//02 * *xs[\underline{m}] + +us[\underline{m}], \text{SetOfReals}))n \vdash us[(\underline{m} + 1)] == us[\underline{m}]$] [NextUS(NoUpperBound) $\xrightarrow{\text{proof}}$ Rule tactic]

[US0 $\xrightarrow{\text{stmt}}$ SystemQ $\vdash us[0] == xs[0] + +R(1f)$] [US0 $\xrightarrow{\text{proof}}$ Rule tactic]

[ExpZero $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \forall \underline{x}: \underline{m} = 0 \vdash \underline{x}(\text{exp})\underline{m} = 1$] [ExpZero $\xrightarrow{\text{proof}}$ Rule tactic]

[ExpPositive $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \forall \underline{x}: \dot{\neg}(0 <= \underline{m} \Rightarrow \dot{\neg}(\dot{\neg}(0 = \underline{m})n)n) \vdash \underline{x}(\text{exp})\underline{m} = (\underline{x} * \underline{x}(\text{exp})(\underline{m} + (-u1)))$] [ExpPositive $\xrightarrow{\text{proof}}$ Rule tactic]

[BSzero $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \forall \underline{n}: \underline{n} = 0 \vdash \text{BS}(\underline{m}, \underline{n}) = \text{rec}(1 + 1)(\text{exp})\underline{m}$] [BSzero $\xrightarrow{\text{proof}}$ Rule tactic]

[BSpositive $\xrightarrow{\text{stmt}}$ SystemQ $\vdash \forall \underline{m}: \forall \underline{n}: \dot{\neg}(0 <= \underline{n} \Rightarrow \dot{\neg}(\dot{\neg}(0 = \underline{n})n)n) \vdash \text{BS}(\underline{m}, \underline{n}) = (\text{rec}(1 + 1)(\text{exp})(\underline{m} + \underline{n}) + \text{BS}(\underline{m}, (\underline{n} + (-u1))))$] [BSpositive $\xrightarrow{\text{proof}}$ Rule tactic]

$[\text{UStelescope}(\text{Zero}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{m}: \forall \underline{n}: \underline{n} = 0 \vdash \text{UStelescope}(\underline{m}, \underline{n}) = |(\text{us}[\underline{m}] + (-\text{uus}[\underline{m} + 1]))|][\text{UStelescope}(\text{Zero}) \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[\text{UStelescope}(\text{Positive}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{m}: \forall \underline{n}: \dot{\vdash} (0 \leq \underline{n} \Rightarrow \dot{\vdash} (\dot{\vdash} (0 = \underline{n})\underline{n})\underline{n}) \vdash \text{UStelescope}(\underline{m}, \underline{n}) = (|(\text{us}[\underline{m} + \underline{n}] + (-\text{uus}[\underline{m} + (\underline{n} + 1)]))| + \text{UStelescope}(\underline{m}, (\underline{n} + (-\text{u}1))))][\text{UStelescope}(\text{Positive}) \xrightarrow{\text{proof}} \text{Rule tactic}]$
 $[(\underline{x}) \xrightarrow{\text{macro}} \lambda t. \lambda s. \lambda c. \tilde{\mathcal{M}}_4(t, s, c, [(\underline{x}) \doteq (\underline{x})])]$

$[\text{EqAddition}(\text{R}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall (\underline{fx}): \forall (\underline{fy}): \forall (\underline{fz}): \text{R}(\underline{fx}) = \text{R}(\underline{fy}) \vdash \text{R}(\underline{fx}) + \text{R}(\underline{fz}) = \text{R}(\underline{fy}) + \text{R}(\underline{fz})][\text{EqAddition}(\text{R}) \xrightarrow{\text{proof}} \text{Rule tactic}]$
 $[\text{PlusCommutativity}(\text{R}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall (\underline{fx}): \forall (\underline{fy}): \text{R}(\underline{fx}) + \text{R}(\underline{fy}) == \text{R}(\underline{fy}) + \text{R}(\underline{fx})][\text{PlusCommutativity}(\text{R}) \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[\text{PlusAssociativity}(\text{R}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall (\underline{fx}): \forall (\underline{fy}): \forall (\underline{fz}): \text{R}(\underline{fx}) + \text{R}(\underline{fy}) + \text{R}(\underline{fz}) = \text{R}(\underline{fx}) + \text{R}(\underline{fy} + \text{R}(\underline{fz}))][\text{PlusAssociativity}(\text{R}) \xrightarrow{\text{proof}} \text{Rule tactic}]$
 $[\text{PlusAssociativity}(\text{R})\text{XX} \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall (\underline{fx}): \forall (\underline{fy}): \forall (\underline{fz}): \text{R}(\underline{fx}) +_f (\underline{fy}) +_f (\underline{fz}) == \text{R}(\underline{fx}) +_f (\underline{fy}) +_f (\underline{fz})][\text{PlusAssociativity}(\text{R})\text{XX} \xrightarrow{\text{proof}} \text{Rule tactic}]$
 $[\text{Plus0}(\text{R}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall (\underline{fx}): \text{R}(\underline{fx}) + \text{R}(0f) == \text{R}(\underline{fx})][\text{Plus0}(\text{R}) \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[\text{Negative}(\text{R}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall \underline{m}: \forall (\underline{fx}): \text{R}(\underline{fx}) + (- - \text{R}(\underline{fx})) == \text{R}(0f)][\text{Negative}(\text{R}) \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[\text{TimesAssociativity}(\text{R}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall (\underline{fx}): \forall (\underline{fy}): \forall (\underline{fz}): \text{R}(\underline{fx}) * * \text{R}(\underline{fy}) * * \text{R}(\underline{fz}) == \text{R}(\underline{fx}) * * \text{R}(\underline{fy}) * * \text{R}(\underline{fz})][\text{TimesAssociativity}(\text{R}) \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[\text{Times1}(\text{R}) \xrightarrow{\text{stmt}} \text{SystemQ} \vdash \forall (\underline{fx}): \text{R}(\underline{fx}) * * \text{R}(1f) == \text{R}(\underline{fx})][\text{Times1}(\text{R}) \xrightarrow{\text{proof}} \text{Rule tactic}]$

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$[\text{kvanti} \xrightarrow{\text{prio}}$

Preassociative

$[\text{kvanti}], [\text{base}], [\text{bracket} * \text{end bracket}], [\text{big bracket} * \text{end bracket}], [\$ * \$],$
 $[\text{flush left} *], [x], [y], [z], [[* \bowtie *]], [[* \xrightarrow{*} *]], [\text{pyk}], [\text{tex}], [\text{name}], [\text{prio}], [*], [T],$
 $[\text{if}(*, *, *)], [[* \xrightarrow{*} *]], [\text{val}], [\text{claim}], [\perp], [f(*)], [(*)^I], [F], [0], [1], [2], [3], [4], [5], [6],$
 $[7], [8], [9], [0], [1], [2], [3], [4], [5], [6], [7], [8], [9], [a], [b], [c], [d], [e], [f], [g], [h], [i], [j],$
 $[k], [l], [m], [n], [o], [p], [q], [r], [s], [t], [u], [v], [w], [(*)^M], [\text{If}(*, *, *)],$
 $[\text{array}\{ * \} * \text{end array}], [l], [c], [r], [\text{empty}], [\{ * | * := * \}], [\mathcal{M}(*)], [\tilde{\mathcal{U}}(*)], [\mathcal{U}(*)],$
 $[\mathcal{U}^M(*)], [\text{apply}(*, *)], [\text{apply}_1(*, *)], [\text{identifier}(*)], [\text{identifier}_1(*, *)], [\text{array-}$
 $\text{plus}(*, *)], [\text{array-remove}(*, *, *)], [\text{array-put}(*, *, *, *)], [\text{array-add}(*, *, *, *, *)],$
 $[\text{bit}(*, *)], [\text{bit}_1(*, *)], [\text{rack}], ["vector"], ["bibliography"], ["dictionary"],$

["body"], ["codex"], ["expansion"], ["code"], ["cache"], ["diagnose"], ["pyk"],
["tex"], ["texname"], ["value"], ["message"], ["macro"], ["definition"],
["unpack"], ["claim"], ["priority"], ["lambda"], ["apply"], ["true"], ["if"],
["quote"], ["proclaim"], ["define"], ["introduce"], ["hide"], ["pre"], ["post"],
 $\mathcal{E}(*, *, *)$, $\mathcal{E}_2(*, *, *, *, *)$, $\mathcal{E}_3(*, *, *, *, *)$, $\mathcal{E}_4(*, *, *, *, *)$, **lookup**(* , * , * , *),
abstract(* , * , * , *), [\ast], $\mathcal{M}(*, *, *, *)$, $\mathcal{M}_2(*, *, *, *)$, $\mathcal{M}^*(*, *, *, *)$, [macro],
 s_0 , [**zip**(* , * , *)], [**assoc** $_1$ (* , * , * , *)], [$(*)^{\mathbf{P}}$], [self], [$[\ast \doteq \ast]$], [$[[\ast \doteq \ast]]$], [$[[\ast \doteq \ast]]$],
 $[[\ast \stackrel{\text{pyk}}{=} \ast]]$, [$[[\ast \stackrel{\text{tex}}{=} \ast]]$], [$[[\ast \stackrel{\text{name}}{=} \ast]]$], [**Priority table**[*]], $[\tilde{\mathcal{M}}_1]$, $[\tilde{\mathcal{M}}_2(*)]$, $[\tilde{\mathcal{M}}_3(*)]$,
 $[\tilde{\mathcal{M}}_4(*, *, *, *, *)]$, $[\mathcal{M}(*, *, *, *)]$, $[\mathcal{Q}(*, *, *, *)]$, $[\tilde{\mathcal{Q}}_2(*, *, *, *)]$, $[\tilde{\mathcal{Q}}_3(*, *, *, *, *)]$, $[\tilde{\mathcal{Q}}^*(*, *, *, *)]$,
 $[[\ast]]$, $[[\ast]]$, [display(*)], [statement(*)], $[[\ast]^{\cdot}]$, $[[\ast]^{-}]$, [**aspect**(* , * , *)],
aspect(* , * , * , *) , [$\langle \ast \rangle$], [**tuple** $_1$ (*)], [**tuple** $_2$ (*)], [let $_2$ (* , * , *)], [let $_1$ (* , * , *)],
 $[[\ast \stackrel{\text{claim}}{=} \ast]]$, [checker], [**check**(* , * , *)], [**check** $_2$ (* , * , * , *)], [**check** $_3$ (* , * , * , *)],
check * (* , * , *) , [**check** $_2^*$ (* , * , * , *)], $[[\ast]^{\cdot}]$, $[[\ast]^{-}]$, $[[\ast]^{\circ}]$, [msg], [$[[\ast \stackrel{\text{msg}}{=} \ast]]$], [$\langle \text{stmt} \rangle$],
[stmt], [$[[\ast \stackrel{\text{stmt}}{=} \ast]]$], [HeadNil'], [HeadPair'], [Transitivity'], [\perp], [Contra'], [T'_E],
 $[L_1]$, [$\underline{\ast}$], [\mathcal{A}], [\mathcal{B}], [\mathcal{C}], [\mathcal{D}], [\mathcal{E}], [\mathcal{F}], [\mathcal{G}], [\mathcal{H}], [\mathcal{I}], [\mathcal{J}], [\mathcal{K}], [\mathcal{L}], [\mathcal{M}], [\mathcal{N}], [\mathcal{O}], [\mathcal{P}], [\mathcal{Q}],
 \mathcal{R}], [\mathcal{S}], [\mathcal{T}], [\mathcal{U}], [\mathcal{V}], [\mathcal{W}], [\mathcal{X}], [\mathcal{Y}], [\mathcal{Z}], [$[\ast \mid \ast := \ast]$], [$[\ast^* \mid \ast := \ast]$], $[\emptyset]$, [Remainder],
 $[(\ast)^{\vee}]$, [intro(* , * , * , * , *)], [intro(* , * , * , *)], [error(* , * , *)], [error $_2$ (* , * , *)], [proof(* , * , * , *)],
[proof $_2$ (* , * , *)], [$\mathcal{S}(*, *, *)$], [$\mathcal{S}^I(*, *, *)$], [$\mathcal{S}^{\triangleright}(*, *, *)$], [$\mathcal{S}_1^{\triangleright}(*, *, *, *)$], [$\mathcal{S}^E(*, *, *)$], [$\mathcal{S}_E^F(*, *, *, *)$],
 $[\mathcal{S}^+(*, *, *)]$, [$\mathcal{S}_1^+(*, *, *, *)$], [$\mathcal{S}^-(*, *, *)$], [$\mathcal{S}_1^-(*, *, *, *)$], [$\mathcal{S}^*(*, *, *)$], [$\mathcal{S}_1^*(*, *, *, *)$],
 $[\mathcal{S}_2^*(*, *, *, *, *)]$, [$\mathcal{S}^{\textcircled{a}}(*, *, *)$], [$\mathcal{S}_1^{\textcircled{a}}(*, *, *, *, *)$], [$\mathcal{S}^{\dagger}(*, *, *)$], [$\mathcal{S}_1^{\dagger}(*, *, *, *, *)$], [$\mathcal{S}^{\text{H}}(*, *, *)$],
 $[\mathcal{S}_1^{\text{H}}(*, *, *, *, *)]$, [$\mathcal{S}^{\text{i.e.}}(*, *, *)$], [$\mathcal{S}_1^{\text{i.e.}}(*, *, *, *, *)$], [$\mathcal{S}_2^{\text{i.e.}}(*, *, *, *, *, *)$], [$\mathcal{S}^{\vee}(*, *, *)$],
 $[\mathcal{S}_1^{\vee}(*, *, *, *, *, *)]$, [$\mathcal{S}^{\text{i}}(*, *, *)$], [$\mathcal{S}_1^{\text{i}}(*, *, *, *, *)$], [$\mathcal{S}_2^{\text{i}}(*, *, *, *, *, *)$], [$\mathcal{T}(*, *)$], [claims(* , * , * , *)],
[claims $_2$ (* , * , * , *)], [$\langle \text{proof} \rangle$], [proof], [**Lemma** * : *], [**Proof of** * : *],
 $[[\ast \text{ lemma } * : *]]$, [$[[\ast \text{ antilemma } * : *]]$], [$[[\ast \text{ rule } * : *]]$], [$[[\ast \text{ antirule } * : *]]$],
[verifier], [\mathcal{V}_1 (*)], [\mathcal{V}_2 (* , * , *)], [\mathcal{V}_3 (* , * , * , *)], [\mathcal{V}_4 (* , * , *)], [\mathcal{V}_5 (* , * , * , *)], [\mathcal{V}_6 (* , * , * , * , *)],
 \mathcal{V}_7 (* , * , * , * , *)], [Cut(* , * , *)], [Head $_{\oplus}$ (*)], [Tail $_{\oplus}$ (*)], [rule $_1$ (* , * , *)], [rule(* , * , *)],
[Rule tactic], [Plus(* , * , *)], [**Theory** *], [theory $_2$ (* , * , *)], [theory $_3$ (* , * , *)],
[theory $_4$ (* , * , * , *)], [HeadNil''], [HeadPair''], [Transitivity''], [Contra''], [HeadNil],
[HeadPair], [Transitivity], [Contra], [T_E], [ragged right],
[ragged right expansion], [parm(* , * , *)], [parm * (* , * , *)], [inst(* , * , *)],
[inst * (* , * , *)], [occur(* , * , *)], [occur * (* , * , *)], [unify(* = * , * , *)], [unify * (* = * , * , *)],
[unify $_2$ (* = * , * , *)], [L_a], [L_b], [L_c], [L_d], [L_e], [L_f], [L_g], [L_h], [L_i], [L_j], [L_k], [L_l], [L_m],
 L_n], [L_o], [L_p], [L_q], [L_r], [L_s], [L_t], [L_u], [L_v], [L_w], [L_x], [L_y], [L_z], [L_A], [L_B], [L_C],
 L_D], [L_E], [L_F], [L_G], [L_H], [L_I], [L_J], [L_K], [L_L], [L_M], [L_N], [L_O], [L_P], [L_Q], [L_R],
 L_S], [L_T], [L_U], [L_V], [L_W], [L_X], [L_Y], [L_Z], [$L_?$], [Reflexivity], [Reflexivity $_1$],
[Commutativity], [Commutativity $_1$], [$\langle \text{tactic} \rangle$], [tactic], [$[[\ast \stackrel{\text{tactic}}{=} \ast]]$], [$\mathcal{P}(*, *, *, *)$],
 $\mathcal{P}^*(*, *, *, *)$, [p_0], [conclude $_1$ (* , * , *)], [conclude $_2$ (* , * , * , *)], [conclude $_3$ (* , * , * , * , *)],
[conclude $_4$ (* , * , *)], [check], [$[[\ast \doteq \ast]]$], [RootVisible(*)], [\mathcal{A}], [\mathcal{R}], [\mathcal{C}], [\mathcal{T}], [\mathcal{L}], [$\{\ast\}$], $[\bar{\ast}]$,
 $[a]$, $[b]$, $[c]$, $[d]$, $[e]$, $[f]$, $[g]$, $[h]$, $[i]$, $[j]$, $[k]$, $[l]$, $[m]$, $[n]$, $[o]$, $[p]$, $[q]$, $[r]$, $[s]$, $[t]$, $[u]$, $[v]$,
 $[w]$, $[x]$, $[y]$, $[z]$, [$[\ast \equiv \ast \mid \ast := \ast]$], [$[\ast \equiv^0 \ast \mid \ast := \ast]$], [$[\ast \equiv^1 \ast \mid \ast := \ast]$], [$[\ast \equiv^* \ast \mid \ast := \ast]$],
[Ded(* , * , *)], [Ded $_0$ (* , * , *)], [Ded $_1$ (* , * , * , *)], [Ded $_2$ (* , * , * , *)], [Ded $_3$ (* , * , * , * , *)],
[Ded $_4$ (* , * , * , * , *)], [Ded $_4^*$ (* , * , * , * , *)], [Ded $_5$ (* , * , * , *)], [Ded $_6$ (* , * , * , * , *)],
[Ded $_6^*$ (* , * , * , * , *)], [Ded $_7$ (*)], [Ded $_8$ (* , * , *)], [Ded $_8^*$ (* , * , *)], [\mathcal{S}], [Neg], [MP], [Gen],
[Ded], [\mathcal{S}_1], [\mathcal{S}_2], [\mathcal{S}_3], [\mathcal{S}_4], [\mathcal{S}_5], [\mathcal{S}_6], [\mathcal{S}_7], [\mathcal{S}_8], [\mathcal{S}_9], [Repetition], [\mathcal{A}_1'], [\mathcal{A}_2'], [\mathcal{A}_4'],

[A5'], [Prop 3.2a], [Prop 3.2b], [Prop 3.2c], [Prop 3.2d], [Prop 3.2e₁], [Prop 3.2e₂],
 [Prop 3.2e], [Prop 3.2f₁], [Prop 3.2f₂], [Prop 3.2f], [Prop 3.2g₁], [Prop 3.2g₂],
 [Prop 3.2g], [Prop 3.2h₁], [Prop 3.2h₂], [Prop 3.2h], [Block₁(*, *, *)], [Block₂(*)],
 [UniqueMember], [UniqueMember(Type)], [SameSeries], [A4], [SameMember],
 [Qclosed(Addition)], [Qclosed(Multiplication)], [FromCartProd(1)],
 [1rule fromCartProd(2)], [constantRationalSeries(*, *)], [cartProd(*, *)], [Power(*, *)],
 [binaryUnion(*, *)], [SetOfRationalSeries], [IsSubset(*, *)], [(p*, *)], [(s*)],
 [(...)], [Objekt-var], [Ex-var], [Ph-var], [Værdi], [Variabel], [Op(*, *)], [Op(*, *)],
 [* ::= *], [ContainsEmpty(*)], [Nat(*)], [Dedu(*, *)], [Dedu₀(*, *)],
 [Dedu_s(*, *, *)], [Dedu₁(*, *, *)], [Dedu₂(*, *, *)], [Dedu₃(*, *, *, *)],
 [Dedu₄(*, *, *, *)], [Dedu₄^{*}(*, *, *, *)], [Dedu₅(*, *, *)], [Dedu₆(*, *, *, *)],
 [Dedu₆^{*}(*, *, *, *)], [Dedu₇(*, *)], [Dedu₈(*, *)], [Dedu₈^{*}(*, *)], [Ex₁], [Ex₂], [Ex₃],
 [Ex₁₀], [Ex₂₀], [*Ex], [*^{Ex}], [(\equiv * | * ::= *)_{Ex}], [(\equiv ⁰ * | * ::= *)_{Ex}],
 [(\equiv ¹ * | * ::= *)_{Ex}], [(\equiv *^{*} | * ::= *)_{Ex}], [ph₁], [ph₂], [ph₃], [*Ph], [*^{Ph}],
 [(\equiv * | * ::= *)_{Ph}], [(\equiv ⁰ * | * ::= *)_{Ph}], [(\equiv ¹ * | * ::= *)_{Ph}],
 [(\equiv *^{*} | * ::= *)_{Ph}], [(\equiv * | * ::= *)_{Me}], [(\equiv ¹ * | * ::= *)_{Me}],
 [(\equiv *^{*} | * ::= *)_{Me}], [bs], [OBS], [BS], [Ø], [SystemQ], [MP], [Gen], [Repetition],
 [Neg], [Ded], [ExistIntro], [Extensionality], [Ødef], [PairDef], [UnionDef],
 [PowerDef], [SeparationDef], [AddDoubleNeg], [RemoveDoubleNeg],
 [AndCommutativity], [AutoImPLY], [Contrapositive], [FirstConjunct],
 [SecondConjunct], [FromContradiction], [FromDisjuncts], [IffCommutativity],
 [IffFirst], [IffSecond], [ImPLYTransitivity], [JoinConjuncts], [MP2], [MP3], [MP4],
 [MP5], [MT], [NegativeMT], [Technicality], [Weakening], [WeakenOr1],
 [WeakenOr2], [Formula2Pair], [Pair2Formula], [Formula2Union],
 [Union2Formula], [Formula2Sep], [Sep2Formula], [Formula2Power],
 [SubsetInPower], [HelperPowerIsSub], [PowerIsSub],
 [(Switch)HelperPowerIsSub], [(Switch)PowerIsSub], [ToSetEquality],
 [HelperToSetEquality(t)], [ToSetEquality(t)], [HelperFromSetEquality],
 [FromSetEquality], [HelperReflexivity], [Reflexivity], [HelperSymmetry],
 [Symmetry], [HelperTransitivity], [Transitivity], [ERisReflexive],
 [ERisSymmetric], [ERisTransitive], [ØisSubset], [HelperMemberNotØ],
 [MemberNotØ], [HelperUniqueØ], [UniqueØ], [= Reflexivity], [= Symmetry],
 [Helper == Transitivity], [= Transitivity], [HelperTransferNotEq],
 [TransferNotEq], [HelperPairSubset], [Helper(2)PairSubset], [PairSubset],
 [SamePair], [SameSingleton], [UnionSubset], [SameUnion], [SeparationSubset],
 [SameSeparation], [SameBinaryUnion], [IntersectionSubset], [SameIntersection],
 [AutoMember], [HelperEqSysNotØ], [EqSysNotØ], [HelperEqSubset],
 [EqSubset], [HelperEqNecessary], [EqNecessary], [HelperNoneEqNecessary],
 [Helper(2)NoneEqNecessary], [NoneEqNecessary], [EqClassIsSubset],
 [EqClassesAreDisjoint], [AllDisjoint], [AllDisjointImPLY], [BSsubset],
 [Union(BS/R)subset], [UnionIdentity], [EqSysIsPartition], [(x1)], [(x2)], [(y1)],
 [(y2)], [(v1)], [(v2)], [(v3)], [(v4)], [(v2n)], [(m1)], [(m2)], [(n1)], [(n2)], [(n3)], [(ε)],
 [(ε₁)], [(ε₂)], [(fep)], [(fx)], [(fy)], [(fz)], [(fu)], [(fv)], [(fw)], [(rx)], [(ry)], [(rz)],
 [(ru)], [(sx)], [(sx1)], [(sy)], [(sy1)], [(sz)], [(sz1)], [(su)], [(su1)], [(fxs)], [(fys)],
 [(crs1)], [(f1)], [(f2)], [(f3)], [(f4)], [(op1)], [(op2)], [(r1)], [(s1)], [(s2)], [X₁], [X₂],
 [Y₁], [Y₂], [V₁], [V₂], [V₃], [V₄], [V_{2n}], [M₁], [M₂], [N₁], [N₂], [N₃], [ε], [ε₁], [ε₂],

[FX], [FY], [FZ], [FU], [FV], [FW], [FEP], [RX], [RY], [RZ], [RU], [(SX)], [(SX1)], [(SY)], [(SY1)], [(SZ)], [(SZ1)], [(SU)], [(SU1)], [FXS], [FYS], [(F1)], [(F2)], [(F3)], [(F4)], [(OP1)], [(OP2)], [(R1)], [(S1)], [(S2)], [(EPob)], [(CRS1ob)], [(F1ob)], [(F2ob)], [(F3ob)], [(F4ob)], [(N1ob)], [(N2ob)], [(OP1ob)], [(OP2ob)], [(R1ob)], [(S1ob)], [(S2ob)], [ph₄], [ph₅], [ph₆], [NAT], [RATIONALSERIES], [SERIES], [SetOfReals], [SetOfFxs], [N], [Q], [X], [xs], [xaF], [ysF], [us], [usFoelge], [0], [1], [(-1)], [2], [3], [1/2], [1/3], [2/3], [0f], [1f], [00], [01], [(- - 01)], [02], [01/02], [PlusAssociativity(R)], [PlusAssociativity(R)XX], [Plus0(R)], [Negative(R)], [Times1(R)], [lessAddition(R)], [PlusCommutativity(R)], [LeqAntisymmetry(R)], [LeqTransitivity(R)], [leqAddition(R)], [Distribution(R)], [A4(Axiom)], [InductionAxiom], [EqualityAxiom], [EqLeqAxiom], [EqAdditionAxiom], [EqMultiplicationAxiom], [QisClosed(Reciprocal)(ImPLY)], [QisClosed(Reciprocal)], [QisClosed(Negative)(ImPLY)], [QisClosed(Negative)], [leqReflexivity], [leqAntisymmetryAxiom], [leqTransitivityAxiom], [leqTotality], [leqAdditionAxiom], [leqMultiplicationAxiom], [plusAssociativity], [plusCommutativity], [Negative], [plus0], [timesAssociativity], [timesCommutativity], [ReciprocalAxiom], [times1], [Distribution], [0not1], [lemma eqLeq(R)], [TimesAssociativity(R)], [TimesCommutativity(R)], [(Adgic)SameR], [Separation2formula(1)], [Separation2formula(2)], [Cauchy], [PlusF], [ReciprocalF], [From ==], [To ==], [FromInR], [PlusR(Sym)], [ReciprocalR(Axiom)], [LessMinus1(N)], [Nonnegative(N)], [US0], [NextXS(UpperBound)], [NextXS(NoUpperBound)], [NextUS(UpperBound)], [NextUS(NoUpperBound)], [ExpZero], [ExpPositive], [ExpZero(R)], [ExpPositive(R)], [BSzero], [BSpositive], [USteleScope(Zero)], [USteleScope(Positive)], [EqAddition(R)], [FromLimit], [ToUpperBound], [FromUpperBound], [USisUpperBound], [0not1(R)], [ExpUnbounded(R)], [FromLeq(Advanced)(N)], [FromLeastUpperBound], [ToLeastUpperBound], [XSisNotUpperBound], [ysFGreater], [ysFLess], [SmallInverse], [NatType], [RationalType], [SeriesType], [Max], [Numerical], [NumericalF], [MemberOfSeries(ImPLY)], [JoinConjuncts(2conditions)], [prop lemma imply negation], [TND], [FromNegatedImPLY], [ToNegatedImPLY], [FromNegated(2 * ImPLY)], [FromNegatedAnd], [FromNegatedOr], [ToNegatedOr], [FromNegations], [From3Disjuncts], [From2 * 2Disjuncts], [NegateDisjunct1], [NegateDisjunct2], [ExpandDisjuncts], [SENC1], [SENC2], [LessLeq(R)], [MemberOfSeries], [memberOfSeries(Type)];

Preassociative

[*_{*}], [*/indexintro(*, *, *, *)], [*/intro(*, *, *)], [*/bothintro(*, *, *, *, *)], [*/nameintro(*, *, *, *)], [*'], [*[*]], [*[*→*]], [*[*⇒*]], [*0], [*1], [0b], [*-color(*)], [*-color*(*)], [*^H], [*^T], [*^U], [*^h], [*^t], [*^s], [*^c], [*^d], [*^a], [*^C], [*^M], [*^B], [*^r], [*ⁱ], [*^d], [*^R], [*⁰], [*¹], [*²], [*³], [*⁴], [*⁵], [*⁶], [*⁷], [*⁸], [*⁹], [*^E], [*^ν], [*^C], [*^{C*}], [*hide];

Preassociative

[“ * ”], [], [(*)^t], [string(*) + *], [string(*) ++ *], [*], [*], [!*, [“*], [#*], [\$*], [%*], [&*], [’*], [(*)], [D*], [**], [+*], [, *], [-*], [.*], [/ *], [0*], [1*], [2*], [3*], [4*], [5*], [6*], [7*], [8*], [9*], [:*], [; *], [<*], [= *], [>*], [?*],

[@*], [A*], [B*], [C*], [D*], [E*], [F*], [G*], [H*], [I*], [J*], [K*], [L*], [M*], [N*], [O*], [P*], [Q*], [R*], [S*], [T*], [U*], [V*], [W*], [X*], [Y*], [Z*], [[*], [*], [^*], [_*], [*], [a*], [b*], [c*], [d*], [e*], [f*], [g*], [h*], [i*], [j*], [k*], [l*], [m*], [n*], [o*], [p*], [q*], [r*], [s*], [t*], [u*], [v*], [w*], [x*], [y*], [z*], [{*}, [{}], [~*], [**Preassociative** *; *], [**Postassociative** *; *], [[*], *], [priority * end], [newline *], [macro newline *], [MacroIndent(*)];

Preassociative

[* ' *], [* ' *];

Preassociative

(exp);

Preassociative

[*'], [R(*)], [— — R(*)], [rec*];

Preassociative

[*/ *], [* ∩ *], [*[*]];

Preassociative

[∪ *], [* ∪ *], [P(*)];

Preassociative

[{*}], [StateExpand(*, *, *)], [extractSeries(*)], [SetOfSeries(*)], [— — Macro(*)], [ExpandList(*, *, *)], [* * Macro(*)], [+ + Macro(*)], [<< Macro(*)], [||Macro(*)], [01//Macro(*)], [UB(*, *)], [LUB(*, *)], [BS(*, *)], [UStescope(*, *)], [(*)], [|f * |], [|r * |], [Limit(*, *)], [Union(*)], [IsOrderedPair(*, *, *)], [IsRelation(*, *, *)], [isFunction(*, *, *)], [IsSeries(*, *)], [IsNatural(*, *)], [OrderedPair(*, *)], [TypeNat(*)], [TypeNat0(*)], [TypeRational(*)], [TypeRational0(*)], [TypeSeries(*, *)], [Typeseries0(*, *)];

Preassociative

[{* , *}], [(< * , *)], [(-u*)], [-f*], [(- — *)], [1f/*], [01//temp*];

Preassociative

[*(* , *)], [RefRel(*, *)], [SymRel(*, *)], [TransRel(*, *)], [EqRel(*, *)], [[* ∈ *]_*], [Partition(*, *)];

Preassociative

[* · *], [* · 0 *], [(** **)], [* *f *], [* * **];

Preassociative

[* + *], [* + 0 *], [* + 1 *], [* - *], [* - 0 *], [* - 1 *], [(* + *)], [(* - *)], [* + f *], [* - f *], [* + + *], [R(*) — — R(*)];

Preassociative

[* ∈ *];

Preassociative

[| * |], [if(*, *, *)], [Max(*, *)], [Max(*, *)];

Preassociative

[* = *], [* ≠ *], [* ≤ *], [* < *], [* <f *], [* ≤f *], [SF(*, *)], [* == *], [*!! == *], [* << *], [* <<== *];

Preassociative

[* ∪ { * }], [* ∪ *], [* \ { * }];

Postassociative

[* . : *], [* . : *], [* : : *], [* + 2 * *], [* : : *], [* + 2 * *];

Postassociative

[*, *];

Preassociative

[* $\overset{B}{\approx}$ *], [* $\overset{D}{\approx}$ *], [* $\overset{C}{\approx}$ *], [* $\overset{P}{\approx}$ *], [* \approx *], [* = *], [* \rightarrow *], [* $\overset{t}{=}$ *], [* $\overset{t^*}{=}$ *], [* $\overset{r}{=}$ *],
[* \in_t *], [* \subseteq_T *], [* $\overset{T}{=}$ *], [* $\overset{s}{=}$ *], [* free in *], [* free in* *], [* free for * in *],
[* free for* * in *], [* \in_c *], [* < *], [* <' *], [* \leq' *], [* = *], [* \neq *], [*^{var}],
[*⁰ *], [*^{#1} *], [*^{#*} *], [* == *], [* \subseteq *];

Preassociative

[\neg *], [$\dot{\neg}$ (*n)], [* \notin *], [* \neq *];

Preassociative

[* \wedge *], [* $\overset{\sim}{\wedge}$ *], [* $\bar{\wedge}$ *], [* \wedge_c *], [* $\hat{\wedge}$ *];

Preassociative

[* \vee *], [* \parallel *], [* $\overset{\vee}{\vee}$ *];

Postassociative

[* $\dot{\vee}$ *];

Preassociative

[\exists *: *], [\forall *: *], [\forall_{obj} *: *], [\exists *: *];

Postassociative

[* $\overset{\Rightarrow}{\Rightarrow}$ *], [* \Rightarrow *], [* \Leftrightarrow *], [* \Leftrightarrow *];

Preassociative

[{ph \in * | *}];

Postassociative

[* : *], [* spy *], [*!*];

Preassociative

[* $\left\{ \begin{array}{l} * \\ * \end{array} \right.$];

Preassociative

[λ * .*], [Λ * .*], [Λ *], [if * then * else *], [let * = * in *], [let * $\ddot{=}$ * in *];

Preassociative

[*^{#*}];

Preassociative

[*¹], [*^{\triangleright}], [*^{\vee}], [*⁺], [*⁻], [*^{*}];

Preassociative

[* @ *], [* \triangleright *], [* \blacktriangleright *], [* \gg *], [* \triangleright *];

Postassociative

[* \vdash *], [* \Vdash *], [* i.e. *];

Preassociative

[\forall *: *], [Π *: *];

Postassociative

[* \oplus *];

Postassociative

[*, *];

Preassociative

[* proves *];

Preassociative

[* **proof of** * : *], [Line * : * \gg *; *], [Last line * \gg * \square],

[Line * : Premise \gg *, *], [Line * : Side-condition \gg *, *], [Arbitrary \gg *, *],
 [Local \gg * = *, *], [Begin *, * : End; *], [Last block line * \gg *, *],
 [Arbitrary \gg *, *];

Postassociative

[* | *];

Postassociative

[* , *], [* [*]*];

Preassociative

[*&*];

Preassociative

[**], [* linebreak[4] *], [**];]

A Pyk definitioner

[UniqueMember $\xrightarrow{\text{pyk}}$ “lemma uniqueMember”]

[UniqueMember(Type) $\xrightarrow{\text{pyk}}$ “lemma uniqueMember(Type)”]

[SameSeries $\xrightarrow{\text{pyk}}$ “lemma sameSeries”]

[A4 $\xrightarrow{\text{pyk}}$ “lemma a4”]

[SameMember $\xrightarrow{\text{pyk}}$ “lemma sameMember”]

[Qclosed(Addition) $\xrightarrow{\text{pyk}}$ “1rule Qclosed(Addition)”]

[Qclosed(Multiplication) $\xrightarrow{\text{pyk}}$ “1rule Qclosed(Multiplication)”]

[FromCartProd(1) $\xrightarrow{\text{pyk}}$ “1rule fromCartProd(1)”]

[1rule fromCartProd(2) $\xrightarrow{\text{pyk}}$ “1rule fromCartProd(2)”]

[constantRationalSeries(*) $\xrightarrow{\text{pyk}}$ “constantRationalSeries(")”]

[cartProd(*) $\xrightarrow{\text{pyk}}$ “cartProd(" , ")”]

[Power(*) $\xrightarrow{\text{pyk}}$ “P(")”]

[binaryUnion(*, *) $\xrightarrow{\text{pyk}}$ “binaryUnion(" , ")”]

[SetOfRationalSeries $\xrightarrow{\text{pyk}}$ “setOfRationalSeries”]

[IsSubset(*, *) $\xrightarrow{\text{pyk}}$ “isSubset(" , ")”]

[(p*, *) $\xrightarrow{\text{pyk}}$ “(p " , ")”]

[(s*) $\xrightarrow{\text{pyk}}$ “(s ")”]

[(...) $\xrightarrow{\text{pyk}}$ “cdots”]

[Objekt-var $\xrightarrow{\text{pyk}}$ “object-var”]

[Ex-var $\xrightarrow{\text{pyk}}$ “ex-var”]

[Ph-var $\xrightarrow{\text{pyk}}$ “ph-var”]

[Værdi $\xrightarrow{\text{pyk}}$ “vaerdi”]

[Variabel $\xrightarrow{\text{pyk}}$ “variabel”]

[Op(*) $\xrightarrow{\text{pyk}}$ “op " end op”]

$[\text{Op}(*, *) \xrightarrow{\text{pyk}} \text{"op2 " comma " end op2"}]$
 $[* ::= * \xrightarrow{\text{pyk}} \text{"define-equal " comma " end equal"}]$
 $[\text{ContainsEmpty}(*) \xrightarrow{\text{pyk}} \text{"contains-empty " end empty"}]$
 $[\text{Nat}(*) \xrightarrow{\text{pyk}} \text{"Nat(")"}]$
 $[\text{Dedu}(*, *) \xrightarrow{\text{pyk}} \text{"1deduction " conclude " end 1deduction"}]$
 $[\text{Dedu}_0(*, *) \xrightarrow{\text{pyk}} \text{"1deduction zero " conclude " end 1deduction"}]$
 $[\text{Dedu}_s(*, *, *) \xrightarrow{\text{pyk}} \text{"1deduction side " conclude " condition " end 1deduction"}]$
 $[\text{Dedu}_1(*, *, *) \xrightarrow{\text{pyk}} \text{"1deduction one " conclude " condition " end 1deduction"}]$
 $[\text{Dedu}_2(*, *, *) \xrightarrow{\text{pyk}} \text{"1deduction two " conclude " condition " end 1deduction"}]$
 $[\text{Dedu}_3(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction three " conclude " condition " bound " end 1deduction"}]$
 $[\text{Dedu}_4(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction four " conclude " condition " bound " end 1deduction"}]$
 $[\text{Dedu}_4^*(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction four star " conclude " condition " bound " end 1deduction"}]$
 $[\text{Dedu}_5(*, *, *) \xrightarrow{\text{pyk}} \text{"1deduction five " condition " bound " end 1deduction"}]$
 $[\text{Dedu}_6(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction six " conclude " exception " bound " end 1deduction"}]$
 $[\text{Dedu}_6^*(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction six star " conclude " exception " bound " end 1deduction"}]$
 $[\text{Dedu}_7(*) \xrightarrow{\text{pyk}} \text{"1deduction seven " end 1deduction"}]$
 $[\text{Dedu}_8(*, *) \xrightarrow{\text{pyk}} \text{"1deduction eight " bound " end 1deduction"}]$
 $[\text{Dedu}_8^*(*, *) \xrightarrow{\text{pyk}} \text{"1deduction eight star " bound " end 1deduction"}]$
 $[\text{Ex}_1 \xrightarrow{\text{pyk}} \text{"ex1"}]$
 $[\text{Ex}_2 \xrightarrow{\text{pyk}} \text{"ex2"}]$
 $[\text{Ex}_3 \xrightarrow{\text{pyk}} \text{"ex3"}]$
 $[\text{Ex}_{10} \xrightarrow{\text{pyk}} \text{"ex10"}]$
 $[\text{Ex}_{20} \xrightarrow{\text{pyk}} \text{"ex20"}]$
 $[*_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"existential var " end var"}]$
 $[*_{\text{Ex}} \xrightarrow{\text{pyk}} \text{" " is existential var"}]$
 $[\langle * \equiv * \mid * ::= * \rangle_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"exist-sub " is " where " is " end sub"}]$
 $[\langle * \equiv^0 * \mid * ::= * \rangle_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"exist-sub0 " is " where " is " end sub"}]$
 $[\langle * \equiv^1 * \mid * ::= * \rangle_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"exist-sub1 " is " where " is " end sub"}]$
 $[\langle * \equiv^* * \mid * ::= * \rangle_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"exist-sub* " is " where " is " end sub"}]$
 $[\text{ph}_1 \xrightarrow{\text{pyk}} \text{"ph1"}]$
 $[\text{ph}_2 \xrightarrow{\text{pyk}} \text{"ph2"}]$

$[\text{ph}_3 \xrightarrow{\text{pyk}} \text{"ph3"}]$
 $[*_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"placeholder-var " end var"}]$
 $[*^{\text{Ph}} \xrightarrow{\text{pyk}} \text{" " is placeholder-var"}]$
 $[\langle * \equiv * \mid * := * \rangle_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"ph-sub " is " where " is " end sub"}]$
 $[\langle * \equiv^0 * \mid * := * \rangle_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"ph-sub0 " is " where " is " end sub"}]$
 $[\langle * \equiv^1 * \mid * := * \rangle_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"ph-sub1 " is " where " is " end sub"}]$
 $[\langle * \equiv * * \mid * := * \rangle_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"ph-sub* " is " where " is " end sub"}]$
 $[\langle * \equiv * \mid * := * \rangle_{\text{Me}} \xrightarrow{\text{pyk}} \text{"meta-sub " is " where " is " end sub"}]$
 $[\langle * \equiv^1 * \mid * := * \rangle_{\text{Me}} \xrightarrow{\text{pyk}} \text{"meta-sub1 " is " where " is " end sub"}]$
 $[\langle * \equiv * * \mid * := * \rangle_{\text{Me}} \xrightarrow{\text{pyk}} \text{"meta-sub* " is " where " is " end sub"}]$
 $[\text{bs} \xrightarrow{\text{pyk}} \text{"var big set"}]$
 $[\text{OBS} \xrightarrow{\text{pyk}} \text{"object big set"}]$
 $[\mathcal{BS} \xrightarrow{\text{pyk}} \text{"meta big set"}]$
 $[\emptyset \xrightarrow{\text{pyk}} \text{"zermelo empty set"}]$
 $[\text{SystemQ} \xrightarrow{\text{pyk}} \text{"system Q"}]$
 $[\text{MP} \xrightarrow{\text{pyk}} \text{"1rule mp"}]$
 $[\text{Gen} \xrightarrow{\text{pyk}} \text{"1rule gen"}]$
 $[\text{Repetition} \xrightarrow{\text{pyk}} \text{"1rule repetition"}]$
 $[\text{Neg} \xrightarrow{\text{pyk}} \text{"1rule ad absurdum"}]$
 $[\text{Ded} \xrightarrow{\text{pyk}} \text{"1rule deduction"}]$
 $[\text{ExistIntro} \xrightarrow{\text{pyk}} \text{"1rule exist intro"}]$
 $[\text{Extensionality} \xrightarrow{\text{pyk}} \text{"axiom extensionality"}]$
 $[\emptyset\text{def} \xrightarrow{\text{pyk}} \text{"axiom empty set"}]$
 $[\text{PairDef} \xrightarrow{\text{pyk}} \text{"axiom pair definition"}]$
 $[\text{UnionDef} \xrightarrow{\text{pyk}} \text{"axiom union definition"}]$
 $[\text{PowerDef} \xrightarrow{\text{pyk}} \text{"axiom power definition"}]$
 $[\text{SeparationDef} \xrightarrow{\text{pyk}} \text{"axiom separation definition"}]$
 $[\text{AddDoubleNeg} \xrightarrow{\text{pyk}} \text{"prop lemma add double neg"}]$
 $[\text{RemoveDoubleNeg} \xrightarrow{\text{pyk}} \text{"prop lemma remove double neg"}]$
 $[\text{AndCommutativity} \xrightarrow{\text{pyk}} \text{"prop lemma and commutativity"}]$
 $[\text{AutoImply} \xrightarrow{\text{pyk}} \text{"prop lemma auto imply"}]$
 $[\text{Contrapositive} \xrightarrow{\text{pyk}} \text{"prop lemma contrapositive"}]$
 $[\text{FirstConjunct} \xrightarrow{\text{pyk}} \text{"prop lemma first conjunct"}]$
 $[\text{SecondConjunct} \xrightarrow{\text{pyk}} \text{"prop lemma second conjunct"}]$
 $[\text{FromContradiction} \xrightarrow{\text{pyk}} \text{"prop lemma from contradiction"}]$

[FromDisjuncts $\xrightarrow{\text{pyk}}$ “prop lemma from disjuncts”]
 [IffCommutativity $\xrightarrow{\text{pyk}}$ “prop lemma iff commutativity”]
 [IffFirst $\xrightarrow{\text{pyk}}$ “prop lemma iff first”]
 [IffSecond $\xrightarrow{\text{pyk}}$ “prop lemma iff second”]
 [ImplyTransitivity $\xrightarrow{\text{pyk}}$ “prop lemma imply transitivity”]
 [JoinConjuncts $\xrightarrow{\text{pyk}}$ “prop lemma join conjuncts”]
 [MP2 $\xrightarrow{\text{pyk}}$ “prop lemma mp2”]
 [MP3 $\xrightarrow{\text{pyk}}$ “prop lemma mp3”]
 [MP4 $\xrightarrow{\text{pyk}}$ “prop lemma mp4”]
 [MP5 $\xrightarrow{\text{pyk}}$ “prop lemma mp5”]
 [MT $\xrightarrow{\text{pyk}}$ “prop lemma mt”]
 [NegativeMT $\xrightarrow{\text{pyk}}$ “prop lemma negative mt”]
 [Technicality $\xrightarrow{\text{pyk}}$ “prop lemma technicality”]
 [Weakening $\xrightarrow{\text{pyk}}$ “prop lemma weakening”]
 [WeakenOr1 $\xrightarrow{\text{pyk}}$ “prop lemma weaken or first”]
 [WeakenOr2 $\xrightarrow{\text{pyk}}$ “prop lemma weaken or second”]
 [Formula2Pair $\xrightarrow{\text{pyk}}$ “lemma formula2pair”]
 [Pair2Formula $\xrightarrow{\text{pyk}}$ “lemma pair2formula”]
 [Formula2Union $\xrightarrow{\text{pyk}}$ “lemma formula2union”]
 [Union2Formula $\xrightarrow{\text{pyk}}$ “lemma union2formula”]
 [Formula2Sep $\xrightarrow{\text{pyk}}$ “lemma formula2separation”]
 [Sep2Formula $\xrightarrow{\text{pyk}}$ “lemma separation2formula”]
 [Formula2Power $\xrightarrow{\text{pyk}}$ “lemma formula2power”]
 [SubsetInPower $\xrightarrow{\text{pyk}}$ “lemma subset in power set”]
 [HelperPowerIsSub $\xrightarrow{\text{pyk}}$ “lemma power set is subset0”]
 [PowerIsSub $\xrightarrow{\text{pyk}}$ “lemma power set is subset”]
 [(Switch)HelperPowerIsSub $\xrightarrow{\text{pyk}}$ “lemma power set is subset0-switch”]
 [(Switch)PowerIsSub $\xrightarrow{\text{pyk}}$ “lemma power set is subset-switch”]
 [ToSetEquality $\xrightarrow{\text{pyk}}$ “lemma set equality suff condition”]
 [HelperToSetEquality(t) $\xrightarrow{\text{pyk}}$ “lemma set equality suff condition(t)0”]
 [ToSetEquality(t) $\xrightarrow{\text{pyk}}$ “lemma set equality suff condition(t)”]
 [HelperFromSetEquality $\xrightarrow{\text{pyk}}$ “lemma set equality skip quantifier”]
 [FromSetEquality $\xrightarrow{\text{pyk}}$ “lemma set equality nec condition”]
 [HelperReflexivity $\xrightarrow{\text{pyk}}$ “lemma reflexivity0”]
 [Reflexivity $\xrightarrow{\text{pyk}}$ “lemma reflexivity”]

[HelperSymmetry $\xrightarrow{\text{pyk}}$ “lemma symmetry0”]
 [Symmetry $\xrightarrow{\text{pyk}}$ “lemma symmetry”]
 [HelperTransitivity $\xrightarrow{\text{pyk}}$ “lemma transitivity0”]
 [Transitivity $\xrightarrow{\text{pyk}}$ “lemma transitivity”]
 [ERisReflexive $\xrightarrow{\text{pyk}}$ “lemma er is reflexive”]
 [ERisSymmetric $\xrightarrow{\text{pyk}}$ “lemma er is symmetric”]
 [ERisTransitive $\xrightarrow{\text{pyk}}$ “lemma er is transitive”]
 [ØisSubset $\xrightarrow{\text{pyk}}$ “lemma empty set is subset”]
 [HelperMemberNotØ $\xrightarrow{\text{pyk}}$ “lemma member not empty0”]
 [MemberNotØ $\xrightarrow{\text{pyk}}$ “lemma member not empty”]
 [HelperUniqueØ $\xrightarrow{\text{pyk}}$ “lemma unique empty set0”]
 [UniqueØ $\xrightarrow{\text{pyk}}$ “lemma unique empty set”]
 [== Reflexivity $\xrightarrow{\text{pyk}}$ “lemma ==Reflexivity”]
 [== Symmetry $\xrightarrow{\text{pyk}}$ “lemma ==Symmetry”]
 [Helper== Transitivity $\xrightarrow{\text{pyk}}$ “lemma ==Transitivity0”]
 [== Transitivity $\xrightarrow{\text{pyk}}$ “lemma ==Transitivity”]
 [HelperTransferNotEq $\xrightarrow{\text{pyk}}$ “lemma transfer ~is0”]
 [TransferNotEq $\xrightarrow{\text{pyk}}$ “lemma transfer ~is”]
 [HelperPairSubset $\xrightarrow{\text{pyk}}$ “lemma pair subset0”]
 [Helper(2)PairSubset $\xrightarrow{\text{pyk}}$ “lemma pair subset1”]
 [PairSubset $\xrightarrow{\text{pyk}}$ “lemma pair subset”]
 [SamePair $\xrightarrow{\text{pyk}}$ “lemma same pair”]
 [SameSingleton $\xrightarrow{\text{pyk}}$ “lemma same singleton”]
 [UnionSubset $\xrightarrow{\text{pyk}}$ “lemma union subset”]
 [SameUnion $\xrightarrow{\text{pyk}}$ “lemma same union”]
 [SeparationSubset $\xrightarrow{\text{pyk}}$ “lemma separation subset”]
 [SameSeparation $\xrightarrow{\text{pyk}}$ “lemma same separation”]
 [SameBinaryUnion $\xrightarrow{\text{pyk}}$ “lemma same binary union”]
 [IntersectionSubset $\xrightarrow{\text{pyk}}$ “lemma intersection subset”]
 [SameIntersection $\xrightarrow{\text{pyk}}$ “lemma same intersection”]
 [AutoMember $\xrightarrow{\text{pyk}}$ “lemma auto member”]
 [HelperEqSysNotØ $\xrightarrow{\text{pyk}}$ “lemma eq-system not empty0”]
 [EqSysNotØ $\xrightarrow{\text{pyk}}$ “lemma eq-system not empty”]
 [HelperEqSubset $\xrightarrow{\text{pyk}}$ “lemma eq subset0”]
 [EqSubset $\xrightarrow{\text{pyk}}$ “lemma eq subset”]

[HelperEqNecessary $\xrightarrow{\text{pyk}}$ “lemma equivalence nec condition0”]
 [EqNecessary $\xrightarrow{\text{pyk}}$ “lemma equivalence nec condition”]
 [HelperNoneEqNecessary $\xrightarrow{\text{pyk}}$ “lemma none-equivalence nec condition0”]
 [Helper(2)NoneEqNecessary $\xrightarrow{\text{pyk}}$ “lemma none-equivalence nec condition1”]
 [NoneEqNecessary $\xrightarrow{\text{pyk}}$ “lemma none-equivalence nec condition”]
 [EqClassIsSubset $\xrightarrow{\text{pyk}}$ “lemma equivalence class is subset”]
 [EqClassesAreDisjoint $\xrightarrow{\text{pyk}}$ “lemma equivalence classes are disjoint”]
 [AllDisjoint $\xrightarrow{\text{pyk}}$ “lemma all disjoint”]
 [AllDisjointImply $\xrightarrow{\text{pyk}}$ “lemma all disjoint-imply”]
 [BSsubset $\xrightarrow{\text{pyk}}$ “lemma bs subset union(bs/r)”]
 [Union(BS/R)subset $\xrightarrow{\text{pyk}}$ “lemma union(bs/r) subset bs”]
 [UnionIdentity $\xrightarrow{\text{pyk}}$ “lemma union(bs/r) is bs”]
 [EqSysIsPartition $\xrightarrow{\text{pyk}}$ “theorem eq-system is partition”]
 [(x1) $\xrightarrow{\text{pyk}}$ “var x1”]
 [(x2) $\xrightarrow{\text{pyk}}$ “var x2”]
 [(y1) $\xrightarrow{\text{pyk}}$ “var y1”]
 [(y2) $\xrightarrow{\text{pyk}}$ “var y2”]
 [(v1) $\xrightarrow{\text{pyk}}$ “var v1”]
 [(v2) $\xrightarrow{\text{pyk}}$ “var v2”]
 [(v3) $\xrightarrow{\text{pyk}}$ “var v3”]
 [(v4) $\xrightarrow{\text{pyk}}$ “var v4”]
 [(v2n) $\xrightarrow{\text{pyk}}$ “var v2n”]
 [(m1) $\xrightarrow{\text{pyk}}$ “var m1”]
 [(m2) $\xrightarrow{\text{pyk}}$ “var m2”]
 [(n1) $\xrightarrow{\text{pyk}}$ “var n1”]
 [(n2) $\xrightarrow{\text{pyk}}$ “var n2”]
 [(n3) $\xrightarrow{\text{pyk}}$ “var n3”]
 [(ϵ) $\xrightarrow{\text{pyk}}$ “var ep”]
 [(ϵ)₁ $\xrightarrow{\text{pyk}}$ “var ep1”]
 [(ϵ)₂ $\xrightarrow{\text{pyk}}$ “var ep2”]
 [(fep) $\xrightarrow{\text{pyk}}$ “var fep”]
 [(fx) $\xrightarrow{\text{pyk}}$ “var fx”]
 [(fy) $\xrightarrow{\text{pyk}}$ “var fy”]
 [(fz) $\xrightarrow{\text{pyk}}$ “var fz”]
 [(fu) $\xrightarrow{\text{pyk}}$ “var fu”]

$[(fv) \xrightarrow{\text{pyk}} \text{“var fv”}]$
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 $[(rz) \xrightarrow{\text{pyk}} \text{“var rz”}]$
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 $[(sx) \xrightarrow{\text{pyk}} \text{“var sx”}]$
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 $[(sy) \xrightarrow{\text{pyk}} \text{“var sy”}]$
 $[(sy1) \xrightarrow{\text{pyk}} \text{“var sy1”}]$
 $[(sz) \xrightarrow{\text{pyk}} \text{“var sz”}]$
 $[(sz1) \xrightarrow{\text{pyk}} \text{“var sz1”}]$
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 $[(su1) \xrightarrow{\text{pyk}} \text{“var su1”}]$
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 $[(s1) \xrightarrow{\text{pyk}} \text{“var s1”}]$
 $[(s2) \xrightarrow{\text{pyk}} \text{“var s2”}]$
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 $[Y_1 \xrightarrow{\text{pyk}} \text{“meta y1”}]$
 $[Y_2 \xrightarrow{\text{pyk}} \text{“meta y2”}]$
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 $[V_2 \xrightarrow{\text{pyk}} \text{“meta v2”}]$
 $[V_3 \xrightarrow{\text{pyk}} \text{“meta v3”}]$
 $[V_4 \xrightarrow{\text{pyk}} \text{“meta v4”}]$
 $[V_{2n} \xrightarrow{\text{pyk}} \text{“meta v2n”}]$

$[M_1 \xrightarrow{\text{pyk}} \text{“meta m1”}]$
 $[M_2 \xrightarrow{\text{pyk}} \text{“meta m2”}]$
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 $[N_2 \xrightarrow{\text{pyk}} \text{“meta n2”}]$
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 $[\epsilon 1 \xrightarrow{\text{pyk}} \text{“meta ep1”}]$
 $[\epsilon 2 \xrightarrow{\text{pyk}} \text{“meta ep2”}]$
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 $[FY \xrightarrow{\text{pyk}} \text{“meta fy”}]$
 $[FZ \xrightarrow{\text{pyk}} \text{“meta fz”}]$
 $[FU \xrightarrow{\text{pyk}} \text{“meta fu”}]$
 $[FV \xrightarrow{\text{pyk}} \text{“meta fv”}]$
 $[FW \xrightarrow{\text{pyk}} \text{“meta fw”}]$
 $[FEP \xrightarrow{\text{pyk}} \text{“meta fep”}]$
 $[RX \xrightarrow{\text{pyk}} \text{“meta rx”}]$
 $[RY \xrightarrow{\text{pyk}} \text{“meta ry”}]$
 $[RZ \xrightarrow{\text{pyk}} \text{“meta rz”}]$
 $[RU \xrightarrow{\text{pyk}} \text{“meta ru”}]$
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 $[(SX1) \xrightarrow{\text{pyk}} \text{“meta sx1”}]$
 $[(SY) \xrightarrow{\text{pyk}} \text{“meta sy”}]$
 $[(SY1) \xrightarrow{\text{pyk}} \text{“meta sy1”}]$
 $[(SZ) \xrightarrow{\text{pyk}} \text{“meta sz”}]$
 $[(SZ1) \xrightarrow{\text{pyk}} \text{“meta sz1”}]$
 $[(SU) \xrightarrow{\text{pyk}} \text{“meta su”}]$
 $[(SU1) \xrightarrow{\text{pyk}} \text{“meta su1”}]$
 $[FXS \xrightarrow{\text{pyk}} \text{“meta fxs”}]$
 $[FYS \xrightarrow{\text{pyk}} \text{“meta fys”}]$
 $[(F1) \xrightarrow{\text{pyk}} \text{“meta f1”}]$
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 $[(OP2) \xrightarrow{\text{pyk}} \text{“meta op2”}]$

$[(R1) \xrightarrow{\text{pyk}} \text{“meta r1”}]$
 $[(S1) \xrightarrow{\text{pyk}} \text{“meta s1”}]$
 $[(S2) \xrightarrow{\text{pyk}} \text{“meta s2”}]$
 $[(EPob) \xrightarrow{\text{pyk}} \text{“object ep”}]$
 $[(CRS1ob) \xrightarrow{\text{pyk}} \text{“object crs1”}]$
 $[(F1ob) \xrightarrow{\text{pyk}} \text{“object f1”}]$
 $[(F2ob) \xrightarrow{\text{pyk}} \text{“object f2”}]$
 $[(F3ob) \xrightarrow{\text{pyk}} \text{“object f3”}]$
 $[(F4ob) \xrightarrow{\text{pyk}} \text{“object f4”}]$
 $[(N1ob) \xrightarrow{\text{pyk}} \text{“object n1”}]$
 $[(N2ob) \xrightarrow{\text{pyk}} \text{“object n2”}]$
 $[(OP1ob) \xrightarrow{\text{pyk}} \text{“object op1”}]$
 $[(OP2ob) \xrightarrow{\text{pyk}} \text{“object op2”}]$
 $[(R1ob) \xrightarrow{\text{pyk}} \text{“object r1”}]$
 $[(S1ob) \xrightarrow{\text{pyk}} \text{“object s1”}]$
 $[(S2ob) \xrightarrow{\text{pyk}} \text{“object s2”}]$
 $[\text{ph}_4 \xrightarrow{\text{pyk}} \text{“ph4”}]$
 $[\text{ph}_5 \xrightarrow{\text{pyk}} \text{“ph5”}]$
 $[\text{ph}_6 \xrightarrow{\text{pyk}} \text{“ph6”}]$
 $[\text{NAT} \xrightarrow{\text{pyk}} \text{“NAT”}]$
 $[\text{RATIONAL}_S\text{ERIES} \xrightarrow{\text{pyk}} \text{“RATIONAL_SERIES”}]$
 $[\text{SERIES} \xrightarrow{\text{pyk}} \text{“SERIES”}]$
 $[\text{SetOfReals} \xrightarrow{\text{pyk}} \text{“setOfReals”}]$
 $[\text{SetOfFxs} \xrightarrow{\text{pyk}} \text{“setOfFxs”}]$
 $[\text{N} \xrightarrow{\text{pyk}} \text{“N”}]$
 $[\text{Q} \xrightarrow{\text{pyk}} \text{“Q”}]$
 $[\text{X} \xrightarrow{\text{pyk}} \text{“X”}]$
 $[\text{xs} \xrightarrow{\text{pyk}} \text{“xs”}]$
 $[\text{xaF} \xrightarrow{\text{pyk}} \text{“xsF”}]$
 $[\text{ysF} \xrightarrow{\text{pyk}} \text{“ysF”}]$
 $[\text{us} \xrightarrow{\text{pyk}} \text{“us”}]$
 $[\text{usFoelge} \xrightarrow{\text{pyk}} \text{“usF”}]$
 $[0 \xrightarrow{\text{pyk}} \text{“0”}]$
 $[1 \xrightarrow{\text{pyk}} \text{“1”}]$
 $[(-1) \xrightarrow{\text{pyk}} \text{“(-1)”}]$

$[2 \xrightarrow{\text{pyk}} \text{"2"}]$
 $[3 \xrightarrow{\text{pyk}} \text{"3"}]$
 $[1/2 \xrightarrow{\text{pyk}} \text{"1/2"}]$
 $[1/3 \xrightarrow{\text{pyk}} \text{"1/3"}]$
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 $[1f \xrightarrow{\text{pyk}} \text{"1f"}]$
 $[00 \xrightarrow{\text{pyk}} \text{"00"}]$
 $[01 \xrightarrow{\text{pyk}} \text{"01"}]$
 $[(- - 01) \xrightarrow{\text{pyk}} \text{"(-01)"}]$
 $[02 \xrightarrow{\text{pyk}} \text{"02"}]$
 $[01//02 \xrightarrow{\text{pyk}} \text{"01//02"}]$
 $[\text{PlusAssociativity}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma plusAssociativity}(\text{R})"]$
 $[\text{PlusAssociativity}(\text{R})\text{XX} \xrightarrow{\text{pyk}} \text{"lemma plusAssociativity}(\text{R})\text{XX}"]$
 $[\text{Plus0}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma plus0}(\text{R})"]$
 $[\text{Negative}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma negative}(\text{R})"]$
 $[\text{Times1}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma times1}(\text{R})"]$
 $[\text{lessAddition}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma lessAddition}(\text{R})"]$
 $[\text{PlusCommutativity}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma plusCommutativity}(\text{R})"]$
 $[\text{LeqAntisymmetry}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma leqAntisymmetry}(\text{R})"]$
 $[\text{LeqTransitivity}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma leqTransitivity}(\text{R})"]$
 $[\text{leqAddition}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma leqAddition}(\text{R})"]$
 $[\text{Distribution}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma distribution}(\text{R})"]$
 $[\text{A4}(\text{Axiom}) \xrightarrow{\text{pyk}} \text{"axiom a4"}]$
 $[\text{InductionAxiom} \xrightarrow{\text{pyk}} \text{"axiom induction"}]$
 $[\text{EqualityAxiom} \xrightarrow{\text{pyk}} \text{"axiom equality"}]$
 $[\text{EqLeqAxiom} \xrightarrow{\text{pyk}} \text{"axiom eqLeq"}]$
 $[\text{EqAdditionAxiom} \xrightarrow{\text{pyk}} \text{"axiom eqAddition"}]$
 $[\text{EqMultiplicationAxiom} \xrightarrow{\text{pyk}} \text{"axiom eqMultiplication"}]$
 $[\text{QisClosed}(\text{Reciprocal})(\text{Imply}) \xrightarrow{\text{pyk}} \text{"axiom QisClosed}(\text{reciprocal})"]$
 $[\text{QisClosed}(\text{Reciprocal}) \xrightarrow{\text{pyk}} \text{"lemma QisClosed}(\text{reciprocal})"]$
 $[\text{QisClosed}(\text{Negative})(\text{Imply}) \xrightarrow{\text{pyk}} \text{"axiom QisClosed}(\text{negative})"]$
 $[\text{QisClosed}(\text{Negative}) \xrightarrow{\text{pyk}} \text{"lemma QisClosed}(\text{negative})"]$
 $[\text{leqReflexivity} \xrightarrow{\text{pyk}} \text{"axiom leqReflexivity"}]$
 $[\text{leqAntisymmetryAxiom} \xrightarrow{\text{pyk}} \text{"axiom leqAntisymmetry"}]$

$[\text{leqTransitivityAxiom} \xrightarrow{\text{pyk}} \text{“axiom leqTransitivity”}]$
 $[\text{leqTotality} \xrightarrow{\text{pyk}} \text{“axiom leqTotality”}]$
 $[\text{leqAdditionAxiom} \xrightarrow{\text{pyk}} \text{“axiom leqAddition”}]$
 $[\text{leqMultiplicationAxiom} \xrightarrow{\text{pyk}} \text{“axiom leqMultiplication”}]$
 $[\text{plusAssociativity} \xrightarrow{\text{pyk}} \text{“axiom plusAssociativity”}]$
 $[\text{plusCommutativity} \xrightarrow{\text{pyk}} \text{“axiom plusCommutativity”}]$
 $[\text{Negative} \xrightarrow{\text{pyk}} \text{“axiom negative”}]$
 $[\text{plus0} \xrightarrow{\text{pyk}} \text{“axiom plus0”}]$
 $[\text{timesAssociativity} \xrightarrow{\text{pyk}} \text{“axiom timesAssociativity”}]$
 $[\text{timesCommutativity} \xrightarrow{\text{pyk}} \text{“axiom timesCommutativity”}]$
 $[\text{ReciprocalAxiom} \xrightarrow{\text{pyk}} \text{“axiom reciprocal”}]$
 $[\text{times1} \xrightarrow{\text{pyk}} \text{“axiom times1”}]$
 $[\text{Distribution} \xrightarrow{\text{pyk}} \text{“axiom distribution”}]$
 $[\text{0not1} \xrightarrow{\text{pyk}} \text{“axiom 0not1”}]$
 $[\text{lemma eqLeq(R)} \xrightarrow{\text{pyk}} \text{“lemma eqLeq(R)”}]$
 $[\text{TimesAssociativity(R)} \xrightarrow{\text{pyk}} \text{“lemma timesAssociativity(R)”}]$
 $[\text{TimesCommutativity(R)} \xrightarrow{\text{pyk}} \text{“lemma timesCommutativity(R)”}]$
 $[(\text{Adgic})\text{SameR} \xrightarrow{\text{pyk}} \text{“1rule adhoc sameR”}]$
 $[\text{Separation2formula(1)} \xrightarrow{\text{pyk}} \text{“lemma separation2formula(1)”}]$
 $[\text{Separation2formula(2)} \xrightarrow{\text{pyk}} \text{“lemma separation2formula(2)”}]$
 $[\text{Cauchy} \xrightarrow{\text{pyk}} \text{“axiom cauchy”}]$
 $[\text{PlusF} \xrightarrow{\text{pyk}} \text{“axiom plusF”}]$
 $[\text{ReciprocalF} \xrightarrow{\text{pyk}} \text{“axiom reciprocalF”}]$
 $[\text{From} \xrightarrow{\text{pyk}} \text{“1rule from”}]$
 $[\text{To} \xrightarrow{\text{pyk}} \text{“1rule to”}]$
 $[\text{FromInR} \xrightarrow{\text{pyk}} \text{“1rule fromInR”}]$
 $[\text{PlusR(Sym)} \xrightarrow{\text{pyk}} \text{“lemma plusR(Sym)”}]$
 $[\text{ReciprocalR(Axiom)} \xrightarrow{\text{pyk}} \text{“axiom reciprocalR”}]$
 $[\text{LessMinus1(N)} \xrightarrow{\text{pyk}} \text{“1rule lessMinus1(N)”}]$
 $[\text{Nonnegative(N)} \xrightarrow{\text{pyk}} \text{“axiom nonnegative(N)”}]$
 $[\text{US0} \xrightarrow{\text{pyk}} \text{“axiom US0”}]$
 $[\text{NextXS(UpperBound)} \xrightarrow{\text{pyk}} \text{“1rule nextXS(upperBound)”}]$
 $[\text{NextXS(NoUpperBound)} \xrightarrow{\text{pyk}} \text{“1rule nextXS(noUpperBound)”}]$
 $[\text{NextUS(UpperBound)} \xrightarrow{\text{pyk}} \text{“1rule nextUS(upperBound)”}]$
 $[\text{NextUS(NoUpperBound)} \xrightarrow{\text{pyk}} \text{“1rule nextUS(noUpperBound)”}]$

$[\text{ExpZero} \xrightarrow{\text{pyk}} \text{"1rule expZero"}]$
 $[\text{ExpPositive} \xrightarrow{\text{pyk}} \text{"1rule expPositive"}]$
 $[\text{ExpZero}(\text{R}) \xrightarrow{\text{pyk}} \text{"1rule expZero}(\text{R})"]$
 $[\text{ExpPositive}(\text{R}) \xrightarrow{\text{pyk}} \text{"1rule expPositive}(\text{R})"]$
 $[\text{BSzero} \xrightarrow{\text{pyk}} \text{"1rule base}(1/2)\text{Sum zero}"]$
 $[\text{BSpositive} \xrightarrow{\text{pyk}} \text{"1rule base}(1/2)\text{Sum positive}"]$
 $[\text{UStelescope}(\text{Zero}) \xrightarrow{\text{pyk}} \text{"1rule UStelescope zero"}]$
 $[\text{UStelescope}(\text{Positive}) \xrightarrow{\text{pyk}} \text{"1rule UStelescope positive"}]$
 $[\text{EqAddition}(\text{R}) \xrightarrow{\text{pyk}} \text{"1rule adhoc eqAddition}(\text{R})"]$
 $[\text{FromLimit} \xrightarrow{\text{pyk}} \text{"1rule fromLimit"}]$
 $[\text{ToUpperBound} \xrightarrow{\text{pyk}} \text{"1rule toUpperBound"}]$
 $[\text{FromUpperBound} \xrightarrow{\text{pyk}} \text{"1rule fromUpperBound"}]$
 $[\text{USisUpperBound} \xrightarrow{\text{pyk}} \text{"axiom USisUpperBound"}]$
 $[\text{0not1}(\text{R}) \xrightarrow{\text{pyk}} \text{"axiom 0not1}(\text{R})"]$
 $[\text{ExpUnbounded}(\text{R}) \xrightarrow{\text{pyk}} \text{"1rule expUnbounded"}]$
 $[\text{FromLeq}(\text{Advanced})(\text{N}) \xrightarrow{\text{pyk}} \text{"1rule fromLeq}(\text{Advanced})(\text{N})"]$
 $[\text{FromLeastUpperBound} \xrightarrow{\text{pyk}} \text{"1rule fromLeastUpperBound"}]$
 $[\text{ToLeastUpperBound} \xrightarrow{\text{pyk}} \text{"1rule toLeastUpperBound"}]$
 $[\text{XSisNotUpperBound} \xrightarrow{\text{pyk}} \text{"axiom XSisNotUpperBound"}]$
 $[\text{ysFGreater} \xrightarrow{\text{pyk}} \text{"axiom ysFGreater"}]$
 $[\text{ysFLess} \xrightarrow{\text{pyk}} \text{"axiom ysFLess"}]$
 $[\text{SmallInverse} \xrightarrow{\text{pyk}} \text{"1rule smallInverse"}]$
 $[\text{NatType} \xrightarrow{\text{pyk}} \text{"axiom natType"}]$
 $[\text{RationalType} \xrightarrow{\text{pyk}} \text{"axiom rationalType"}]$
 $[\text{SeriesType} \xrightarrow{\text{pyk}} \text{"axiom seriesType"}]$
 $[\text{Max} \xrightarrow{\text{pyk}} \text{"axiom max"}]$
 $[\text{Numerical} \xrightarrow{\text{pyk}} \text{"axiom numerical"}]$
 $[\text{NumericalF} \xrightarrow{\text{pyk}} \text{"axiom numericalF"}]$
 $[\text{MemberOfSeries}(\text{ImPLY}) \xrightarrow{\text{pyk}} \text{"axiom memberOfSeries"}]$
 $[\text{JoinConjuncts}(2\text{conditions}) \xrightarrow{\text{pyk}} \text{"prop lemma doubly conditioned join conjuncts"}]$
 $[\text{prop lemma imply negation} \xrightarrow{\text{pyk}} \text{"prop lemma imply negation"}]$
 $[\text{TND} \xrightarrow{\text{pyk}} \text{"prop lemma tertium non datur"}]$
 $[\text{FromNegatedImPLY} \xrightarrow{\text{pyk}} \text{"prop lemma from negated imply"}]$
 $[\text{ToNegatedImPLY} \xrightarrow{\text{pyk}} \text{"prop lemma to negated imply"}]$

[FromNegated(2 * Imply) $\xrightarrow{\text{pyk}}$ “prop lemma from negated double imply”]
 [FromNegatedAnd $\xrightarrow{\text{pyk}}$ “prop lemma from negated and”]
 [FromNegatedOr $\xrightarrow{\text{pyk}}$ “prop lemma from negated or”]
 [ToNegatedOr $\xrightarrow{\text{pyk}}$ “prop lemma to negated or”]
 [FromNegations $\xrightarrow{\text{pyk}}$ “prop lemma from negations”]
 [From3Disjuncts $\xrightarrow{\text{pyk}}$ “prop lemma from three disjuncts”]
 [From2 * 2Disjuncts $\xrightarrow{\text{pyk}}$ “prop lemma from two times two disjuncts”]
 [NegateDisjunct1 $\xrightarrow{\text{pyk}}$ “prop lemma negate first disjunct”]
 [NegateDisjunct2 $\xrightarrow{\text{pyk}}$ “prop lemma negate second disjunct”]
 [ExpandDisjuncts $\xrightarrow{\text{pyk}}$ “prop lemma expand disjuncts”]
 [SENC1 $\xrightarrow{\text{pyk}}$ “lemma set equality nec condition(1)”]
 [SENC2 $\xrightarrow{\text{pyk}}$ “lemma set equality nec condition(2)”]
 [LessLeq(R) $\xrightarrow{\text{pyk}}$ “lemma lessLeq(R)”]
 [MemberOfSeries $\xrightarrow{\text{pyk}}$ “lemma memberOfSeries”]
 [memberOfSeries(Type) $\xrightarrow{\text{pyk}}$ “lemma memberOfSeries(Type)”]
 [* (exp) * $\xrightarrow{\text{pyk}}$ “ ” ^ “ ”]
 [R(*) $\xrightarrow{\text{pyk}}$ “R(”)”]
 [– – R(*) $\xrightarrow{\text{pyk}}$ “--R(”)”]
 [rec* $\xrightarrow{\text{pyk}}$ “1/ ””]
 [* / * $\xrightarrow{\text{pyk}}$ “eq-system of ” modulo ””]
 [* \cap * $\xrightarrow{\text{pyk}}$ “intersection ” comma ” end intersection”]
 [* [*] $\xrightarrow{\text{pyk}}$ “[” ; ”]”]
 [\cup * $\xrightarrow{\text{pyk}}$ “union ” end union”]
 [* \cup * $\xrightarrow{\text{pyk}}$ “binary-union ” comma ” end union”]
 [P(*) $\xrightarrow{\text{pyk}}$ “power ” end power”]
 [{*} $\xrightarrow{\text{pyk}}$ “zermelo singleton ” end singleton”]
 [StateExpand(*, *, *) $\xrightarrow{\text{pyk}}$ “stateExpand(” , ” , ”)”]
 [extractSeries(*) $\xrightarrow{\text{pyk}}$ “extractSeries(”)”]
 [SetOfSeries(*) $\xrightarrow{\text{pyk}}$ “setOfSeries(”)”]
 [– – Macro(*) $\xrightarrow{\text{pyk}}$ “--Macro(”)”]
 [ExpandList(*, *, *) $\xrightarrow{\text{pyk}}$ “expandList(” , ” , ”)”]
 [* * Macro(*) $\xrightarrow{\text{pyk}}$ “**Macro(”)”]
 [+ + Macro(*) $\xrightarrow{\text{pyk}}$ “++Macro(”)”]
 [<< Macro(*) $\xrightarrow{\text{pyk}}$ “<<Macro(”)”]
 [|Macro(*) $\xrightarrow{\text{pyk}}$ “|Macro(”)”]

$[01//Macro(*) \xrightarrow{pyk} \text{"01//Macro(")"}]$
 $[UB(*, *) \xrightarrow{pyk} \text{"upperBound(" , ")"}]$
 $[LUB(*, *) \xrightarrow{pyk} \text{"leastUpperBound(" , ")"}]$
 $[BS(*, *) \xrightarrow{pyk} \text{"base(1/2)Sum(" , ")"}]$
 $[UStelescope(*, *) \xrightarrow{pyk} \text{"UStelescope(" , ")"}]$
 $[(*) \xrightarrow{pyk} \text{"(")"}]$
 $[|f * | \xrightarrow{pyk} \text{"|f " |"}]$
 $[|r * | \xrightarrow{pyk} \text{"|r " |"}]$
 $[Limit(*, *) \xrightarrow{pyk} \text{"limit(" , ")"}]$
 $[Union(*) \xrightarrow{pyk} \text{"U(")"}]$
 $[IsOrderedPair(*, *, *) \xrightarrow{pyk} \text{"isOrderedPair(" , " , ")"}]$
 $[IsRelation(*, *, *) \xrightarrow{pyk} \text{"isRelation(" , " , ")"}]$
 $[isFunction(*, *, *) \xrightarrow{pyk} \text{"isFunction(" , " , ")"}]$
 $[IsSeries(*, *) \xrightarrow{pyk} \text{"isSeries(" , ")"}]$
 $[IsNatural(*, *) \xrightarrow{pyk} \text{"isNatural(")"}]$
 $[OrderedPair(*, *) \xrightarrow{pyk} \text{"(o " , ")"}]$
 $[TypeNat(*) \xrightarrow{pyk} \text{"typeNat(")"}]$
 $[TypeNat0(*) \xrightarrow{pyk} \text{"typeNat0(")"}]$
 $[TypeRational(*) \xrightarrow{pyk} \text{"typeRational(")"}]$
 $[TypeRational0(*) \xrightarrow{pyk} \text{"typeRational0(")"}]$
 $[TypeSeries(*, *) \xrightarrow{pyk} \text{"typeSeries(" , ")"}]$
 $[Typeseries0(*, *) \xrightarrow{pyk} \text{"typeSeries0(" , ")"}]$
 $[\{*, *\} \xrightarrow{pyk} \text{"zermelo pair " comma " end pair"}]$
 $[\langle *, *\rangle \xrightarrow{pyk} \text{"zermelo ordered pair " comma " end pair"}]$
 $[(-u*) \xrightarrow{pyk} \text{"- " }]$
 $[-f* \xrightarrow{pyk} \text{"-f " }]$
 $[(- - *) \xrightarrow{pyk} \text{"-- " }]$
 $[1f/* \xrightarrow{pyk} \text{"1f/ " }]$
 $[01//temp* \xrightarrow{pyk} \text{"01// " }]$
 $[*(*, *) \xrightarrow{pyk} \text{" " is related to " under " }]$
 $[RefRel(*, *) \xrightarrow{pyk} \text{" " is reflexive relation in " }]$
 $[SymRel(*, *) \xrightarrow{pyk} \text{" " is symmetric relation in " }]$
 $[TransRel(*, *) \xrightarrow{pyk} \text{" " is transitive relation in " }]$
 $[EqRel(*, *) \xrightarrow{pyk} \text{" " is equivalence relation in " }]$
 $[[* \in *]_* \xrightarrow{pyk} \text{"equivalence class of " in " modulo " }]$

[Partition(*, *) $\xrightarrow{\text{pyk}}$ " is partition of "]
 [(***) $\xrightarrow{\text{pyk}}$ " * "]
 [* *_f * $\xrightarrow{\text{pyk}}$ " *_f "]
 [* * * * $\xrightarrow{\text{pyk}}$ " * * * "]
 [(* + *) $\xrightarrow{\text{pyk}}$ " + "]
 [(* - *) $\xrightarrow{\text{pyk}}$ " - "]
 [* +_f * $\xrightarrow{\text{pyk}}$ " +_f "]
 [* -_f * $\xrightarrow{\text{pyk}}$ " -_f "]
 [* + + * $\xrightarrow{\text{pyk}}$ " ++ "]
 [R(*) - -R(*) $\xrightarrow{\text{pyk}}$ "R() -- R()"]
 [* ∈ * $\xrightarrow{\text{pyk}}$ " in0 "]
 [| * | $\xrightarrow{\text{pyk}}$ " | "]
 [if(*, *, *) $\xrightarrow{\text{pyk}}$ "if(, ,)"]
 [Max(*, *) $\xrightarrow{\text{pyk}}$ "max(,)"]
 [Max(*, *) $\xrightarrow{\text{pyk}}$ "maxR(,)"]
 [* = * $\xrightarrow{\text{pyk}}$ " = "]
 [* ≠ * $\xrightarrow{\text{pyk}}$ " != "]
 [* <= * $\xrightarrow{\text{pyk}}$ " <= "]
 [* < * $\xrightarrow{\text{pyk}}$ " < "]
 [* <_f * $\xrightarrow{\text{pyk}}$ " <_f "]
 [* ≤_f * $\xrightarrow{\text{pyk}}$ " <=_f "]
 [SF(*, *) $\xrightarrow{\text{pyk}}$ " sameF "]
 [* == * $\xrightarrow{\text{pyk}}$ " == "]
 [* !! == * $\xrightarrow{\text{pyk}}$ " !! == "]
 [* << * $\xrightarrow{\text{pyk}}$ " << "]
 [* << == * $\xrightarrow{\text{pyk}}$ " << == "]
 [* == * $\xrightarrow{\text{pyk}}$ " zermelo is "]
 [* ⊆ * $\xrightarrow{\text{pyk}}$ " is subset of "]
 [¬(*)_n $\xrightarrow{\text{pyk}}$ "not0 "]
 [* ∉ * $\xrightarrow{\text{pyk}}$ " zermelo ~in "]
 [* ≠ * $\xrightarrow{\text{pyk}}$ " zermelo ~is "]
 [* ∧ * $\xrightarrow{\text{pyk}}$ " and0 "]
 [* ∨ * $\xrightarrow{\text{pyk}}$ " or0 "]
 [∃*: * $\xrightarrow{\text{pyk}}$ "exist0 " indeed "]
 [* ⇔ * $\xrightarrow{\text{pyk}}$ " iff "]

[{ph ∈ * | *} $\xrightarrow{\text{pyk}}$ “the set of ph in " such that " end set”]
[kvanti $\xrightarrow{\text{pyk}}$ “kvanti”]

B T_EX definitioner

[kvanti $\xrightarrow{\text{tex}}$ “kvanti”]

[(\cdots) $\xrightarrow{\text{tex}}$ “(\cdots)”]

[Objekt-var $\xrightarrow{\text{tex}}$ “\texttt{Objekt-var}”]

[Ex-var $\xrightarrow{\text{tex}}$ “\texttt{Ex-var}”]

[Ph-var $\xrightarrow{\text{tex}}$ “\texttt{Ph-var}”]

[Værdi $\xrightarrow{\text{tex}}$ “\texttt{V\ae{rdi}}”]

[Variabel $\xrightarrow{\text{tex}}$ “\texttt{Variabel}”]

[Op(x) $\xrightarrow{\text{tex}}$ “Op(#1.
)”]

[Op(x, y) $\xrightarrow{\text{tex}}$ “Op(#1.
, #2.
)”]

[x \doteq y $\xrightarrow{\text{tex}}$ “#1.
\mathrel {\ddot{=}} #2.”]

[ContainsEmpty(x) $\xrightarrow{\text{tex}}$ “ContainsEmpty(#1.
)”]

[Dedu(x, y) $\xrightarrow{\text{tex}}$ “
Dedu(#1.
, #2.
)”]

[Dedu₀(x, y) $\xrightarrow{\text{tex}}$ “
Dedu_0(#1.
, #2.
)”]

[Dedu_s(x, y, z) $\xrightarrow{\text{tex}}$ “Dedu_{s}(#1.
, #2.
, #3.
)”]

[Dedu₁(x, y, z) $\xrightarrow{\text{tex}}$ “
Dedu_1(#1.
, #2.
)”]

, #3.
)”]

[Dedu₂(x, y, z) $\xrightarrow{\text{tex}}$ “
Dedu_2(#1.

, #2.
, #3.
)”]

[Dedu₃(x, y, z, u) $\xrightarrow{\text{tex}}$ “
Dedu_3(#1.

, #2.
, #3.
, #4.
)”]

[Dedu₄(x, y, z, u) $\xrightarrow{\text{tex}}$ “
Dedu_4(#1.

, #2.
, #3.
, #4.
)”]

[Dedu₄^{*}(x, y, z, u) $\xrightarrow{\text{tex}}$ “
Dedu_4^*(#1.

, #2.
, #3.
, #4.
)”]

[Dedu₅(x, y, z) $\xrightarrow{\text{tex}}$ “
Dedu_5(#1.

, #2.
, #3.
)”]

[Dedu₆(p, c, e, b) $\xrightarrow{\text{tex}}$ “
Dedu_6(#1.

, #2.
, #3.
, #4.
)”]

[Dedu₆^{*}(p, c, e, b) $\xrightarrow{\text{tex}}$ “
Dedu_6^*(#1.

, #2.
, #3.

, #4.
)”]

[Dedu₇(p) $\xrightarrow{\text{tex}}$ “
Dedu_7(#1.
)”]

[Dedu₈(p, b) $\xrightarrow{\text{tex}}$ “
Dedu_8(#1.
, #2.
)”]

[Dedu₈^{*}(p, b) $\xrightarrow{\text{tex}}$ “
Dedu_8^*(#1.
, #2.
)”]

[Ex₁ $\xrightarrow{\text{tex}}$ “Ex_{1}”]

[Ex₂ $\xrightarrow{\text{tex}}$ “Ex_{2}”]

[Ex₁₀ $\xrightarrow{\text{tex}}$ “Ex_{10}”]

[Ex₂₀ $\xrightarrow{\text{tex}}$ “Ex_{20}”]

[x_{Ex} $\xrightarrow{\text{tex}}$ “#1.
_{Ex}”]

[x^{Ex} $\xrightarrow{\text{tex}}$ “#1.
^_{Ex}”]

[(x≡y|z:=u)_{Ex} $\xrightarrow{\text{tex}}$ “\langle #1.
\equiv #2.
| #3.
{:=} #4.
\rangle_{Ex} ”]

[(x≡⁰y|z:=u)_{Ex} $\xrightarrow{\text{tex}}$ “\langle #1.
\equiv⁰ #2.
| #3.
{:=} #4.
\rangle_{Ex} ”]

[(x≡¹y|z:=u)_{Ex} $\xrightarrow{\text{tex}}$ “\langle #1.
\equiv¹ #2.
| #3.
{:=} #4.
\rangle_{Ex} ”]

$\langle x \equiv *y | z := u \rangle_{\text{Ex}} \xrightarrow{\text{tex}} \text{"\langle \rangle \#1.}$
 $\{\text{equiv}\}^* \#2.$
 $| \#3.$
 $\{:=\} \#4.$
 \rangle_{Ex}

$\text{ph}_1 \xrightarrow{\text{tex}} \text{"ph_{1}}"$

$\text{ph}_2 \xrightarrow{\text{tex}} \text{"ph_{2}}"$

$\text{ph}_3 \xrightarrow{\text{tex}} \text{"ph_{3}}"$

$\text{ph}_4 \xrightarrow{\text{tex}} \text{"ph_{4}}"$

$\text{ph}_5 \xrightarrow{\text{tex}} \text{"ph_{5}}"$

$\text{ph}_6 \xrightarrow{\text{tex}} \text{"ph_{6}}"$

$*_{\text{Ph}} \xrightarrow{\text{tex}} \text{"\#1.}$
 -Ph

$x^{\text{Ph}} \xrightarrow{\text{tex}} \text{"\#1.}$
 \^Ph

$\langle x \equiv y | z := u \rangle_{\text{Ph}} \xrightarrow{\text{tex}} \text{"\langle \rangle \#1.}$
 $\{\text{equiv}\} \#2.$
 $| \#3.$
 $\{:=\} \#4.$
 \rangle_{Ph}

$\langle x \equiv^0 y | z := u \rangle_{\text{Ph}} \xrightarrow{\text{tex}} \text{"\langle \rangle \#1.}$
 $\{\text{equiv}\}^0 \#2.$
 $| \#3.$
 $\{:=\} \#4.$
 \rangle_{Ph}

$\langle x \equiv^1 y | z := u \rangle_{\text{Ph}} \xrightarrow{\text{tex}} \text{"\langle \rangle \#1.}$
 $\{\text{equiv}\}^1 \#2.$
 $| \#3.$
 $\{:=\} \#4.$
 \rangle_{Ph}

$\langle x \equiv *y | z := u \rangle_{\text{Ph}} \xrightarrow{\text{tex}} \text{"\langle \rangle \#1.}$
 $\{\text{equiv}\}^* \#2.$
 $| \#3.$
 $\{:=\} \#4.$
 \rangle_{Ph}

[$\text{bs} \xrightarrow{\text{tex}}$ “ $\backslash\text{mathsf}\{\text{bs}\}$ ”]

[$\text{OBS} \xrightarrow{\text{tex}}$ “ $\backslash\text{mathsf}\{\text{OBS}\}$ ”]

[$\mathcal{BS} \xrightarrow{\text{tex}}$ “ $\{\backslash\text{cal BS}\}$ ”]

[$\emptyset \xrightarrow{\text{tex}}$ “ $\backslash\text{mathrm}\{\backslash\text{O}\}$ ”]

[$\text{SystemQ} \xrightarrow{\text{tex}}$ “ SystemQ ”]

[$\text{MP} \xrightarrow{\text{tex}}$ “ MP ”]

[$\text{Gen} \xrightarrow{\text{tex}}$ “ Gen ”]

[$\text{Repetition} \xrightarrow{\text{tex}}$ “ Repetition ”]

[$\text{Neg} \xrightarrow{\text{tex}}$ “ Neg ”]

[$\text{Ded} \xrightarrow{\text{tex}}$ “ Ded ”]

[$\text{ExistIntro} \xrightarrow{\text{tex}}$ “ ExistIntro ”]

[$\text{Extensionality} \xrightarrow{\text{tex}}$ “ Extensionality ”]

[$\emptyset\text{def} \xrightarrow{\text{tex}}$ “ $\backslash\text{O}\{\}\text{def}$ ”]

[$\text{PairDef} \xrightarrow{\text{tex}}$ “ PairDef ”]

[$\text{UnionDef} \xrightarrow{\text{tex}}$ “ UnionDef ”]

[$\text{PowerDef} \xrightarrow{\text{tex}}$ “ PowerDef ”]

[$\text{SeparationDef} \xrightarrow{\text{tex}}$ “ SeparationDef ”]

[$\text{AddDoubleNeg} \xrightarrow{\text{tex}}$ “ AddDoubleNeg ”]

[$\text{RemoveDoubleNeg} \xrightarrow{\text{tex}}$ “ RemoveDoubleNeg ”]

[$\text{AndCommutativity} \xrightarrow{\text{tex}}$ “ AndCommutativity ”]

[$\text{AutoImply} \xrightarrow{\text{tex}}$ “ AutoImply ”]

[$\text{Contrapositive} \xrightarrow{\text{tex}}$ “ Contrapositive ”]

[$\text{FirstConjunct} \xrightarrow{\text{tex}}$ “ FirstConjunct ”]

[$\text{SecondConjunct} \xrightarrow{\text{tex}}$ “ SecondConjunct ”]

[$\text{FromContradiction} \xrightarrow{\text{tex}}$ “ FromContradiction ”]

[FromDisjuncts $\xrightarrow{\text{tex}}$ “FromDisjuncts”]
[IffCommutativity $\xrightarrow{\text{tex}}$ “IffCommutativity”]
[IffFirst $\xrightarrow{\text{tex}}$ “IffFirst”]
[IffSecond $\xrightarrow{\text{tex}}$ “IffSecond”]
[ImplyTransitivity $\xrightarrow{\text{tex}}$ “ImplyTransitivity”]
[JoinConjuncts $\xrightarrow{\text{tex}}$ “JoinConjuncts”]
[MP2 $\xrightarrow{\text{tex}}$ “MP2”]
[MP3 $\xrightarrow{\text{tex}}$ “MP3”]
[MP4 $\xrightarrow{\text{tex}}$ “MP4”]
[MP5 $\xrightarrow{\text{tex}}$ “MP5”]
[MT $\xrightarrow{\text{tex}}$ “MT”]
[NegativeMT $\xrightarrow{\text{tex}}$ “NegativeMT”]
[Technicality $\xrightarrow{\text{tex}}$ “Technicality”]
[Weakening $\xrightarrow{\text{tex}}$ “Weakening”]
[WeakenOr1 $\xrightarrow{\text{tex}}$ “WeakenOr1”]
[WeakenOr2 $\xrightarrow{\text{tex}}$ “WeakenOr2”]
[Pair2Formula $\xrightarrow{\text{tex}}$ “Pair2Formula”]
[Formula2Pair $\xrightarrow{\text{tex}}$ “Formula2Pair”]
[Union2Formula $\xrightarrow{\text{tex}}$ “Union2Formula”]
[Formula2Union $\xrightarrow{\text{tex}}$ “Formula2Union”]
[Formula2Power $\xrightarrow{\text{tex}}$ “Formula2Power”]
[Sep2Formula $\xrightarrow{\text{tex}}$ “Sep2Formula”]
[Formula2Sep $\xrightarrow{\text{tex}}$ “Formula2Sep”]
[SubsetInPower $\xrightarrow{\text{tex}}$ “SubsetInPower”]
[HelperPowerIsSub $\xrightarrow{\text{tex}}$ “HelperPowerIsSub”]

[PowerIsSub $\xrightarrow{\text{tex}}$ “PowerIsSub”]

[(Switch)HelperPowerIsSub $\xrightarrow{\text{tex}}$ “(Switch)HelperPowerIsSub”]

[(Switch)PowerIsSub $\xrightarrow{\text{tex}}$ “(Switch)PowerIsSub”]

[ToSetEquality $\xrightarrow{\text{tex}}$ “ToSetEquality”]

[HelperToSetEquality(t) $\xrightarrow{\text{tex}}$ “HelperToSetEquality(t)”]

[ToSetEquality(t) $\xrightarrow{\text{tex}}$ “ToSetEquality(t)”]

[HelperFromSetEquality $\xrightarrow{\text{tex}}$ “HelperFromSetEquality”]

[FromSetEquality $\xrightarrow{\text{tex}}$ “FromSetEquality”]

[HelperReflexivity $\xrightarrow{\text{tex}}$ “HelperReflexivity”]

[Reflexivity $\xrightarrow{\text{tex}}$ “Reflexivity”]

[HelperSymmetry $\xrightarrow{\text{tex}}$ “HelperSymmetry”]

[Symmetry $\xrightarrow{\text{tex}}$ “Symmetry”]

[HelperTransitivity $\xrightarrow{\text{tex}}$ “HelperTransitivity”]

[Transitivity $\xrightarrow{\text{tex}}$ “Transitivity”],

[ERisReflexive $\xrightarrow{\text{tex}}$ “ERisReflexive”]

[ERisSymmetric $\xrightarrow{\text{tex}}$ “ERisSymmetric”]

[ERisTransitive $\xrightarrow{\text{tex}}$ “ERisTransitive”]

[\emptyset isSubset $\xrightarrow{\text{tex}}$ “ \emptyset isSubset”]

[HelperMemberNot \emptyset $\xrightarrow{\text{tex}}$ “HelperMemberNot \emptyset ”]

[MemberNot \emptyset $\xrightarrow{\text{tex}}$ “MemberNot \emptyset ”]

[HelperUnique \emptyset $\xrightarrow{\text{tex}}$ “HelperUnique \emptyset ”]

[Unique \emptyset $\xrightarrow{\text{tex}}$ “Unique \emptyset ”]

[== Reflexivity $\xrightarrow{\text{tex}}$ “==\!{ }Reflexivity”]

[== Symmetry $\xrightarrow{\text{tex}}$ “==\!{ }Symmetry”]

[Helper == Transitivity $\xrightarrow{\text{tex}}$ “Helper\!{ } ==\!{ }Transitivity”]

[==Transitivity $\xrightarrow{\text{tex}}$ “\!\{ }==\!\{ }Transitivity”]

[HelperTransferNotEq $\xrightarrow{\text{tex}}$ “HelperTransferNotEq”]

[TransferNotEq $\xrightarrow{\text{tex}}$ “TransferNotEq”]

[HelperPairSubset $\xrightarrow{\text{tex}}$ “HelperPairSubset”]

[Helper(2)PairSubset $\xrightarrow{\text{tex}}$ “Helper(2)PairSubset”]

[PairSubset $\xrightarrow{\text{tex}}$ “PairSubset”]

[SamePair $\xrightarrow{\text{tex}}$ “SamePair”]

[SameSingleton $\xrightarrow{\text{tex}}$ “SameSingleton”]

[UnionSubset $\xrightarrow{\text{tex}}$ “UnionSubset”]

[SameUnion $\xrightarrow{\text{tex}}$ “SameUnion”]

[SeparationSubset $\xrightarrow{\text{tex}}$ “SeparationSubset”]

[SameSeparation $\xrightarrow{\text{tex}}$ “SameSeparation”]

[SameBinaryUnion $\xrightarrow{\text{tex}}$ “SameBinaryUnion”]

[IntersectionSubset $\xrightarrow{\text{tex}}$ “IntersectionSubset”]

[SameIntersection $\xrightarrow{\text{tex}}$ “SameIntersection”]

[AutoMember $\xrightarrow{\text{tex}}$ “AutoMember”]

[HelperEqSysNot \emptyset $\xrightarrow{\text{tex}}$ “HelperEqSysNot\O{ }”]

[EqSysNot \emptyset $\xrightarrow{\text{tex}}$ “EqSysNot\O{ }”]

[HelperEqSubset $\xrightarrow{\text{tex}}$ “HelperEqSubset”]

[EqSubset $\xrightarrow{\text{tex}}$ “EqSubset”]

[EqNecessary $\xrightarrow{\text{tex}}$ “EqNecessary”]

[HelperEqNecessary $\xrightarrow{\text{tex}}$ “HelperEqNecessary”]

[HelperNoneEqNecessary $\xrightarrow{\text{tex}}$ “HelperNoneEqNecessary”]

[Helper(2)NoneEqNecessary $\xrightarrow{\text{tex}}$ “Helper(2)NoneEqNecessary”]

[NoneEqNecessary $\xrightarrow{\text{tex}}$ “NoneEqNecessary”]

[EqClassIsSubset $\xrightarrow{\text{tex}}$ “EqClassIsSubset”]

[EqClassesAreDisjoint $\xrightarrow{\text{tex}}$ “EqClassesAreDisjoint”]

[AllDisjoint $\xrightarrow{\text{tex}}$ “AllDisjoint”]

[AllDisjointImply $\xrightarrow{\text{tex}}$ “AllDisjointImply”]

[BSsubset $\xrightarrow{\text{tex}}$ “BSsubset”]

[Union(BS/R)subset $\xrightarrow{\text{tex}}$ “Union(BS/R)subset”]

[UnionIdentity $\xrightarrow{\text{tex}}$ “UnionIdentity”]

[EqSysIsPartition $\xrightarrow{\text{tex}}$ “EqSysIsPartition”]

[x/y $\xrightarrow{\text{tex}}$ “#1.
/ #2.”]

[x \cap y $\xrightarrow{\text{tex}}$ “#1.
\cap #2.”]

[\cup x $\xrightarrow{\text{tex}}$ “\cup #1.”]

[x \cup y $\xrightarrow{\text{tex}}$ “#1.
\mathrel{\cup} #2.”]

[P(x) $\xrightarrow{\text{tex}}$ “P(#1.
)”]

[{x} $\xrightarrow{\text{tex}}$ “\{#1.
\}”]

[{x, y} $\xrightarrow{\text{tex}}$ “\{#1.
, #2.
\}”]

[<x, y> $\xrightarrow{\text{tex}}$ “\langle #1.
, #2.
\rangle”],

[x \in y $\xrightarrow{\text{tex}}$ “#1.
\mathrel{\in} #2.”]

[z(x, y) $\xrightarrow{\text{tex}}$ “#3.
(#1.
, #2.
)”]

[RefRel(r, x) $\xrightarrow{\text{tex}}$ “RefRel(#1.
, #2.
)”]

[SymRel(r, x) $\xrightarrow{\text{tex}}$ “SymRel(#1.
, #2.
)”]

[TransRel(r, x) $\xrightarrow{\text{tex}}$ “TransRel(#1.
, #2.
)”]

[EqRel(r, x) $\xrightarrow{\text{tex}}$ “EqRel(#1.
, #2.
)”]

[[x \in bs]_r $\xrightarrow{\text{tex}}$ “[#1.
\mathrel{\in} #2.
]-{#3.
}”]

[Partition(x, y) $\xrightarrow{\text{tex}}$ “Partition(#1.
, #2.
)”]

[x == y $\xrightarrow{\text{tex}}$ “#1.
\!\mathrel{=} #2.”]

[x \subseteq y $\xrightarrow{\text{tex}}$ “#1.
\mathrel{\subseteq} #2.”]

[$\dot{\neg}(x)$ n $\xrightarrow{\text{tex}}$ “\dot{\neg}\, (#1.
n)”]

[x \notin y $\xrightarrow{\text{tex}}$ “#1.
\mathrel{\notin} #2.”]

[x \neq y $\xrightarrow{\text{tex}}$ “#1.
\mathrel{\neq} #2.”]

[x $\dot{\wedge}$ y $\xrightarrow{\text{tex}}$ “#1.
\mathrel{\dot{\wedge}} #2.”]

[x $\dot{\vee}$ y $\xrightarrow{\text{tex}}$ “#1.
\mathrel{\dot{\vee}} #2.”]

[x $\dot{\leftrightarrow}$ y $\xrightarrow{\text{tex}}$ “#1.
\mathrel{\dot{\leftrightarrow}} #2.”]

[{ph ∈ x | a} $\xrightarrow{\text{tex}}$ “ \{ ph \mathrel{\in} \} #1.
\mid #2.
\}”]

[x ⇒ y $\xrightarrow{\text{tex}}$ “(i#1.
\Rightarrow #2.
i”]

[Nat(x) $\xrightarrow{\text{tex}}$ “Nat(#1.
)”]

[(x≡y|z:=u)_{Me} $\xrightarrow{\text{tex}}$ “\langle #1.
\equiv #2.
| #3.
{:=} #4.
\rangle_{Me}”]

[(x≡¹y|z:=u)_{Me} $\xrightarrow{\text{tex}}$ “\langle #1.
\equiv¹ #2.
| #3.
{:=} #4.
\rangle_{Me} ”]

[(x≡*y|z:=u)_{Me} $\xrightarrow{\text{tex}}$ “\langle #1.
\equiv* #2.
| #3.
{:=} #4.
\rangle_{Me} ”]

[∃x:y $\xrightarrow{\text{tex}}$ “
\exists #1.
: #2.”]

[(x1) $\xrightarrow{\text{tex}}$ “(x1)”]

[(x2) $\xrightarrow{\text{tex}}$ “(x2)”]

[(y1) $\xrightarrow{\text{tex}}$ “(y1)”]

[(y2) $\xrightarrow{\text{tex}}$ “(y2)”]

[(v1) $\xrightarrow{\text{tex}}$ “(v1)”]

[(v2) $\xrightarrow{\text{tex}}$ “(v2)”]

[(v3) $\xrightarrow{\text{tex}}$ “(v3)”]

[(v4) $\xrightarrow{\text{tex}}$ “(v4)”]

$[(v2n) \xrightarrow{\text{tex}} "(v2n)"]$

$[(n1) \xrightarrow{\text{tex}} "(n1)"]$

$[(n2) \xrightarrow{\text{tex}} "(n2)"]$

$[(n3) \xrightarrow{\text{tex}} "(n3)"]$

$[(m1) \xrightarrow{\text{tex}} "(m1)"]$

$[(m2) \xrightarrow{\text{tex}} "(m2)"]$

$[(\epsilon) \xrightarrow{\text{tex}} "(\backslash\epsilonpsilon)"]$

$[(\epsilon)_1 \xrightarrow{\text{tex}} "(\backslash\epsilonpsilon)_{1}"]$

$[(\epsilon)_2 \xrightarrow{\text{tex}} "(\backslash\epsilonpsilon)_2"]$

$[(fx) \xrightarrow{\text{tex}} "(fx)"]$

$[(fy) \xrightarrow{\text{tex}} "(fy)"]$

$[(fz) \xrightarrow{\text{tex}} "(fz)"]$

$[(fu) \xrightarrow{\text{tex}} "(fu)"]$

$[(fv) \xrightarrow{\text{tex}} "(fv)"]$

$[(fw) \xrightarrow{\text{tex}} "(fw)"]$

$[(fep) \xrightarrow{\text{tex}} "(fep)"]$

$[(rx) \xrightarrow{\text{tex}} "(rx)"]$

$[(ry) \xrightarrow{\text{tex}} "(ry)"]$

$[(rz) \xrightarrow{\text{tex}} "(rz)"]$

$[(ru) \xrightarrow{\text{tex}} "(ru)"]$

$[(sx) \xrightarrow{\text{tex}} "(sx)"]$

$[(sx1) \xrightarrow{\text{tex}} "(sx1)"]$

$[(sy) \xrightarrow{\text{tex}} "(sy)"]$

$[(sy1) \xrightarrow{\text{tex}} "(sy1)"]$

$[(sz) \xrightarrow{\text{tex}} "(sz)"]$

$[(sz1) \xrightarrow{\text{tex}} \text{“(sz1)”}]$

$[(su) \xrightarrow{\text{tex}} \text{“(su)”}]$

$[(su1) \xrightarrow{\text{tex}} \text{“(su1)”}]$

$[(fxs) \xrightarrow{\text{tex}} \text{“(fxs)”}]$

$[(fys) \xrightarrow{\text{tex}} \text{“(fys)”}]$

$[(crs1) \xrightarrow{\text{tex}} \text{“(crs1)”}]$

$[(f1) \xrightarrow{\text{tex}} \text{“(f1)”}]$

$[(f2) \xrightarrow{\text{tex}} \text{“(f2)”}]$

$[(f3) \xrightarrow{\text{tex}} \text{“(f3)”}]$

$[(f4) \xrightarrow{\text{tex}} \text{“(f4)”}]$

$[(op1) \xrightarrow{\text{tex}} \text{“(op1)”}]$

$[(op2) \xrightarrow{\text{tex}} \text{“(op2)”}]$

$[(r1) \xrightarrow{\text{tex}} \text{“(r1)”}]$

$[(s1) \xrightarrow{\text{tex}} \text{“(s1)”}]$

$[(s2) \xrightarrow{\text{tex}} \text{“(s2)”}]$

$[X_1 \xrightarrow{\text{tex}} \text{“X_{1}”}]$

$[X_2 \xrightarrow{\text{tex}} \text{“X_{2}”}]$

$[Y_1 \xrightarrow{\text{tex}} \text{“Y_{1}”}]$

$[Y_2 \xrightarrow{\text{tex}} \text{“Y_{2}”}]$

$[V_1 \xrightarrow{\text{tex}} \text{“V_{1}”}]$

$[V_2 \xrightarrow{\text{tex}} \text{“V_{2}”}]$

$[V_3 \xrightarrow{\text{tex}} \text{“V_{3}”}]$

$[V_4 \xrightarrow{\text{tex}} \text{“V_{4}”}]$

$[V_{2n} \xrightarrow{\text{tex}} \text{“V_{2n}”}]$

$[\epsilon \xrightarrow{\text{tex}} \text{“\epsilon”}]$

[M₁ $\xrightarrow{\text{tex}}$ “M_{1}”]

[M₂ $\xrightarrow{\text{tex}}$ “M_{2}”]

[N₁ $\xrightarrow{\text{tex}}$ “N_{1} ”]

[N₂ $\xrightarrow{\text{tex}}$ “N_{2} ”]

[N₃ $\xrightarrow{\text{tex}}$ “N_{3} ”]

[ε1 $\xrightarrow{\text{tex}}$ “\epsilon 1”]

[ε2 $\xrightarrow{\text{tex}}$ “\epsilon 2”]

[FX $\xrightarrow{\text{tex}}$ “FX”]

[FY $\xrightarrow{\text{tex}}$ “FY”]

[FZ $\xrightarrow{\text{tex}}$ “FZ”]

[FU $\xrightarrow{\text{tex}}$ “FU”]

[FV $\xrightarrow{\text{tex}}$ “FV”]

[FW $\xrightarrow{\text{tex}}$ “FW”]

[FEP $\xrightarrow{\text{tex}}$ “FEP”]

[RX $\xrightarrow{\text{tex}}$ “RX”]

[RY $\xrightarrow{\text{tex}}$ “RY”]

[RZ $\xrightarrow{\text{tex}}$ “RZ”]

[RU $\xrightarrow{\text{tex}}$ “RU”]

[(SX) $\xrightarrow{\text{tex}}$ “(SX)”]

[(SX1) $\xrightarrow{\text{tex}}$ “(SX1)”]

[(SY) $\xrightarrow{\text{tex}}$ “(SY)”]

[(SY1) $\xrightarrow{\text{tex}}$ “(SY1)”]

[(SZ) $\xrightarrow{\text{tex}}$ “(SZ)”]

[(SZ1) $\xrightarrow{\text{tex}}$ “(SZ1)”]

[(SU) $\xrightarrow{\text{tex}}$ “(SU)”]

[(SU1) $\xrightarrow{\text{tex}}$ “(SU1)”]

[FXS $\xrightarrow{\text{tex}}$ “FXS”]

[FYS $\xrightarrow{\text{tex}}$ “FYS”]

[(F1) $\xrightarrow{\text{tex}}$ “(F1)”]

[(F2) $\xrightarrow{\text{tex}}$ “(F2)”]

[(F3) $\xrightarrow{\text{tex}}$ “(F3)”]

[(F4) $\xrightarrow{\text{tex}}$ “(F4)”]

[(OP1) $\xrightarrow{\text{tex}}$ “(OP1)”]

[(OP2) $\xrightarrow{\text{tex}}$ “(OP2)”]

[(R1) $\xrightarrow{\text{tex}}$ “(R1)”]

[(S1) $\xrightarrow{\text{tex}}$ “(S1)”]

[(S2) $\xrightarrow{\text{tex}}$ “(S2)”]

[(EPob) $\xrightarrow{\text{tex}}$ “(EPob)”]

[(CRS1ob) $\xrightarrow{\text{tex}}$ “(CRS1ob)”]

[(F1ob) $\xrightarrow{\text{tex}}$ “(F1ob)”]

[(F2ob) $\xrightarrow{\text{tex}}$ “(F2ob)”]

[(F3ob) $\xrightarrow{\text{tex}}$ “(F3ob)”]

[(F4ob) $\xrightarrow{\text{tex}}$ “(F4ob)”]

[(N1ob) $\xrightarrow{\text{tex}}$ “(N1ob)”]

[(N2ob) $\xrightarrow{\text{tex}}$ “(N2ob)”]

[(OP1ob) $\xrightarrow{\text{tex}}$ “(OP1ob)”]

[(OP2ob) $\xrightarrow{\text{tex}}$ “(OP2ob)”]

[(R1ob) $\xrightarrow{\text{tex}}$ “(R1ob)”]

[(S1ob) $\xrightarrow{\text{tex}}$ “(S1ob)”]

[(S2ob) $\xrightarrow{\text{tex}}$ “(S2ob)”]

[Ex3 $\xrightarrow{\text{tex}}$ “Ex3”]

[NAT $\xrightarrow{\text{tex}}$ “NAT”]

[RATIONAL_SSERIES $\xrightarrow{\text{tex}}$ “RATIONAL_SERIES”]

[SERIES $\xrightarrow{\text{tex}}$ “SERIES”]

[SetOfReals $\xrightarrow{\text{tex}}$ “SetOfReals”]

[SetOfFxs $\xrightarrow{\text{tex}}$ “SetOfFxs”]

[N $\xrightarrow{\text{tex}}$ “N”]

[Q $\xrightarrow{\text{tex}}$ “Q”]

[X $\xrightarrow{\text{tex}}$ “X”]

[xs $\xrightarrow{\text{tex}}$ “xs”]

[xaF $\xrightarrow{\text{tex}}$ “xaF”]

[ysF $\xrightarrow{\text{tex}}$ “ysF”]

[us $\xrightarrow{\text{tex}}$ “us”]

[usFoelge $\xrightarrow{\text{tex}}$ “usFoelge”]

[0 $\xrightarrow{\text{tex}}$ “0”]

[1 $\xrightarrow{\text{tex}}$ “1”]

[(-1) $\xrightarrow{\text{tex}}$ “(-1)”]

[2 $\xrightarrow{\text{tex}}$ “2”]

[3 $\xrightarrow{\text{tex}}$ “3”]

[1/2 $\xrightarrow{\text{tex}}$ “1/2”]

[1/3 $\xrightarrow{\text{tex}}$ “1/3”]

[2/3 $\xrightarrow{\text{tex}}$ “2/3”]

[0f $\xrightarrow{\text{tex}}$ “0f”]

[00 $\xrightarrow{\text{tex}}$ “00”]

[(- - 01) $\xrightarrow{\text{tex}}$ “(-01)”]

[02 $\xrightarrow{\text{tex}}$ “02”]

[01//02 $\xrightarrow{\text{tex}}$ “01//02”]

[x = y $\xrightarrow{\text{tex}}$ “#1.
= #2.”]

[x \neq y $\xrightarrow{\text{tex}}$ “#1.
\neq #2.”]

[x < y $\xrightarrow{\text{tex}}$ “#1.
< #2.”]

[x <= y $\xrightarrow{\text{tex}}$ “#1.
<= #2.”]

[x <_f y $\xrightarrow{\text{tex}}$ “#1.
<_{f} #2.”]

[x \leq_f y $\xrightarrow{\text{tex}}$ “#1.
\leq_{f} #2.”]

[SF(x,y) $\xrightarrow{\text{tex}}$ “SF(#1.
, #2.
)”]

[x == y $\xrightarrow{\text{tex}}$ “#1.
== #2.”]

[x!! == y $\xrightarrow{\text{tex}}$ “#1.
!!== #2.”]

[x << y $\xrightarrow{\text{tex}}$ “#1.
<< #2.”]

[x <<== y $\xrightarrow{\text{tex}}$ “#1.
<<== #2.”]

[x[y] $\xrightarrow{\text{tex}}$ “#1.
[#2.
]”]

[(-ux) $\xrightarrow{\text{tex}}$ “(-u#1.
)”]

[-_f x $\xrightarrow{\text{tex}}$ “-_{f} #1.”]

$[(- - x) \xrightarrow{\text{tex}} “(--\#1.$
)]”]

$[1f/x \xrightarrow{\text{tex}} “1f/\#1.”]$

$[01//tempx \xrightarrow{\text{tex}} “01//temp\#1.”]$

$[(x + y) \xrightarrow{\text{tex}} “(\#1.$
+ $\#2.$
)]”]

$[(x - y) \xrightarrow{\text{tex}} “(\#1.$
- $\#2.$
)]”]

$[(fx) +_f (fy) \xrightarrow{\text{tex}} “\#1.$
+ $_{-}\{f\}\#2.”]$

$[(fx) -_f (fy) \xrightarrow{\text{tex}} “\#1.$
- $_{-}\{f\}\#2.”]$

$[(fx) *_f (fy) \xrightarrow{\text{tex}} “\#1.$
* $_{-}\{f\}\#2.”]$

$[x + +y \xrightarrow{\text{tex}} “\#1.$
++ $\#2.”]$

$[R((fx)) - -R((fy)) \xrightarrow{\text{tex}} “R(\#1.$
) -- R($\#2.$
)]”]

$[(x * y) \xrightarrow{\text{tex}} “(\#1.$
* $\#2.$
)]”]

$[x * *y \xrightarrow{\text{tex}} “\#1.$
** $\#2.”]$

$[x(\text{exp})y \xrightarrow{\text{tex}} “ \#1.$
(exp) $\#2.”]$

$[\text{leqReflexivity} \xrightarrow{\text{tex}} “\text{leqReflexivity}”]$

$[\text{recx} \xrightarrow{\text{tex}} “\text{rec}\#1.”]$

$[|x| \xrightarrow{\text{tex}} “|\#1.$
|”]

[StateExpand(t, s, c) $\xrightarrow{\text{tex}}$ “StateExpand(#1.
, #2.
, #3.
)”]

[extractSeries(t) $\xrightarrow{\text{tex}}$ “extractSeries(#1.
)”]

[|f|x| $\xrightarrow{\text{tex}}$ “|f#1.
”]

[|r|x| $\xrightarrow{\text{tex}}$ “|r#1.
”]

[SetOfSeries(x) $\xrightarrow{\text{tex}}$ “SetOfSeries(#1.
)”]

[ExpandList(x, y, z) $\xrightarrow{\text{tex}}$ “ExpandList(#1.
, #2.
, #3.
)”]

[* * Macro(x) $\xrightarrow{\text{tex}}$ “**Macro(#1.
)”]

[+ + Macro(x) $\xrightarrow{\text{tex}}$ “++Macro(#1.
)”]

[– – Macro(x) $\xrightarrow{\text{tex}}$ “--Macro(#1.
)”]

[<< Macro(x) $\xrightarrow{\text{tex}}$ “<<Macro(#1.
)”]

[|Macro(x) $\xrightarrow{\text{tex}}$ “|Macro(#1.
)”]

[01//Macro(x) $\xrightarrow{\text{tex}}$ “01//Macro(#1.
)”]

[Max(x, y) $\xrightarrow{\text{tex}}$ “Max(#1.
, #2.
)”]

[Max(x, y) $\xrightarrow{\text{tex}}$ “Max(#1.
, #2.
)”]

[Limit(x, y) $\xrightarrow{\text{tex}}$ “Limit(#1.
, #2.
)”]

[Union(x) $\xrightarrow{\text{tex}}$ “Union(#1.
)”]

[if(x, y, z) $\xrightarrow{\text{tex}}$ “if(#1.
, #2.
, #3.
)”]

[IsOrderedPair(x, y, z) $\xrightarrow{\text{tex}}$ “IsOrderedPair(#1.
, #2.
, #3.
)”]

[IsRelation(x, y, z) $\xrightarrow{\text{tex}}$ “IsRelation(#1.
, #2.
, #3.
)”]

[isFunction(x, y, z) $\xrightarrow{\text{tex}}$ “isFunction(#1.
, #2.
, #3.
)”]

[TypeNat(x) $\xrightarrow{\text{tex}}$ “TypeNat(#1.
)”]

[TypeNat0(x) $\xrightarrow{\text{tex}}$ “TypeNat0(#1.
)”]

[TypeRational(x) $\xrightarrow{\text{tex}}$ “TypeRational(#1.
)”]

[TypeRational0(x) $\xrightarrow{\text{tex}}$ “TypeRational0(#1.
)”]

[TypeSeries(x, y) $\xrightarrow{\text{tex}}$ “TypeSeries(#1.
, #2.
)”]

[Typeseries0(x, y) $\xrightarrow{\text{tex}}$ “Typeseries0(#1.
, #2.
)”]

[UB(x, y) $\xrightarrow{\text{tex}}$ “UB(#1.
, #2.
)”]

[LUB(x, y) $\xrightarrow{\text{tex}}$ “LUB(#1.
, #2.
)”]

[BS(x, y) $\xrightarrow{\text{tex}}$ “BS(#1.
, #2.
)”]

[UStelescope(x, y) $\xrightarrow{\text{tex}}$ “UStelescope(#1.
, #2.
)”]

[(x) $\xrightarrow{\text{tex}}$ “(#1.
)”]

[R(x) $\xrightarrow{\text{tex}}$ “R(#1.
)”]

[- - R(x) $\xrightarrow{\text{tex}}$ “--R(#1.
)”]

[IsSeries(x, y) $\xrightarrow{\text{tex}}$ “IsSeries(#1.
, #2.
)”]

[IsNatural(xy, *) $\xrightarrow{\text{tex}}$ “IsNatural(#1.
, #2.
)”]

[OrderedPair(x, y) $\xrightarrow{\text{tex}}$ “OrderedPair(#1.
, #2.
)”]

[leqAntisymmetryAxiom $\xrightarrow{\text{tex}}$ “leqAntisymmetryAxiom”]

[leqTransitivityAxiom $\xrightarrow{\text{tex}}$ “leqTransitivityAxiom”]

[leqTotality $\xrightarrow{\text{tex}}$ “leqTotality”]

[leqAdditionAxiom $\xrightarrow{\text{tex}}$ “leqAdditionAxiom”]

[leqMultiplicationAxiom $\xrightarrow{\text{tex}}$ “leqMultiplicationAxiom”]

[plusAssociativity $\xrightarrow{\text{tex}}$ “plusAssociativity”]

$[\text{plusCommutativity} \xrightarrow{\text{tex}} \text{“plusCommutativity”}]$
 $[\text{Negative} \xrightarrow{\text{tex}} \text{“Negative”}]$
 $[\text{plus0} \xrightarrow{\text{tex}} \text{“plus0”}]$
 $[\text{timesAssociativity} \xrightarrow{\text{tex}} \text{“timesAssociativity”}]$
 $[\text{timesCommutativity} \xrightarrow{\text{tex}} \text{“timesCommutativity”}]$
 $[\text{ReciprocalAxiom} \xrightarrow{\text{tex}} \text{“ReciprocalAxiom”}]$
 $[\text{times1} \xrightarrow{\text{tex}} \text{“times1”}]$
 $[\text{plusAssociativity} \xrightarrow{\text{tex}} \text{“plusAssociativity”}]$
 $[\text{plusCommutativity} \xrightarrow{\text{tex}} \text{“plusCommutativity”}]$
 $[\text{Negative} \xrightarrow{\text{tex}} \text{“Negative”}]$
 $[\text{Distribution} \xrightarrow{\text{tex}} \text{“Distribution”}]$
 $[\text{0not1} \xrightarrow{\text{tex}} \text{“0not1”}]$
 $[\text{A4(Axiom)} \xrightarrow{\text{tex}} \text{“A4(Axiom)”}]$
 $[\text{InductionAxiom} \xrightarrow{\text{tex}} \text{“InductionAxiom”}]$
 $[\text{EqualityAxiom} \xrightarrow{\text{tex}} \text{“EqualityAxiom”}]$
 $[\text{EqLeqAxiom} \xrightarrow{\text{tex}} \text{“EqLeqAxiom”}]$
 $[\text{EqAdditionAxiom} \xrightarrow{\text{tex}} \text{“EqAdditionAxiom”}]$
 $[\text{EqMultiplicationAxiom} \xrightarrow{\text{tex}} \text{“EqMultiplicationAxiom”}]$
 $[\text{SENC1} \xrightarrow{\text{tex}} \text{“SENC1”}]$
 $[\text{SENC2} \xrightarrow{\text{tex}} \text{“SENC2”}]$
 $[\text{Cauchy} \xrightarrow{\text{tex}} \text{“Cauchy”}]$
 $[\text{PlusF} \xrightarrow{\text{tex}} \text{“PlusF”}]$
 $[\text{ReciprocalF} \xrightarrow{\text{tex}} \text{“ReciprocalF”}]$
 $[\text{From} == \xrightarrow{\text{tex}} \text{“From==”}]$
 $[\text{To} == \xrightarrow{\text{tex}} \text{“To==”}]$

[FromInR $\xrightarrow{\text{tex}}$ "FromInR"]

[ReciprocalR(Axiom) $\xrightarrow{\text{tex}}$ "ReciprocalR(Axiom)"]

[US0 $\xrightarrow{\text{tex}}$ "US0"]

[NextXS(UpperBound) $\xrightarrow{\text{tex}}$ "NextXS(UpperBound)"]

[NextXS(NoUpperBound) $\xrightarrow{\text{tex}}$ "NextXS(NoUpperBound)"]

[NextUS(UpperBound) $\xrightarrow{\text{tex}}$ "NextUS(UpperBound)"]

[NextUS(NoUpperBound) $\xrightarrow{\text{tex}}$ "NextUS(NoUpperBound)"]

[ExpZero $\xrightarrow{\text{tex}}$ "ExpZero"]

[ExpPositive $\xrightarrow{\text{tex}}$ "ExpPositive"]

[ExpZero(R) $\xrightarrow{\text{tex}}$ "ExpZero(R)"]

[ExpPositive(R) $\xrightarrow{\text{tex}}$ "ExpPositive(R)"]

[LessMinus1(N) $\xrightarrow{\text{tex}}$ "LessMinus1(N)"]

[Nonnegative(N) $\xrightarrow{\text{tex}}$ "Nonnegative(N)"]

[BSzero $\xrightarrow{\text{tex}}$ "BSzero"]

[BSpositive $\xrightarrow{\text{tex}}$ "BSpositive"]

[USTelescope(Zero) $\xrightarrow{\text{tex}}$ "USTelescope(Zero)"]

[USTelescope(Positive) $\xrightarrow{\text{tex}}$ "USTelescope(Positive)"]

[EqAddition(R) $\xrightarrow{\text{tex}}$ "EqAddition(R)"]

[FromLimit $\xrightarrow{\text{tex}}$ "FromLimit"]

[ToUpperBound $\xrightarrow{\text{tex}}$ "ToUpperBound"]

[FromUpperBound $\xrightarrow{\text{tex}}$ "FromUpperBound"]

[USisUpperBound $\xrightarrow{\text{tex}}$ "USisUpperBound"]

[0not1(R) $\xrightarrow{\text{tex}}$ "0not1(R)"]

[ExpUnbounded(R) $\xrightarrow{\text{tex}}$ "ExpUnbounded(R)"]

[FromLeq(Advanced)(N) $\xrightarrow{\text{tex}}$ "FromLeq(Advanced)(N)"]

$[FromLeastUpperBound \xrightarrow{\text{tex}} \text{“FromLeastUpperBound”}]$
 $[ToLeastUpperBound \xrightarrow{\text{tex}} \text{“ToLeastUpperBound”}]$
 $[XSisNotUpperBound \xrightarrow{\text{tex}} \text{“XSisNotUpperBound”}]$
 $[ysFGreater \xrightarrow{\text{tex}} \text{“ysFGreater”}]$
 $[ysFLess \xrightarrow{\text{tex}} \text{“ysFLess”}]$
 $[SmallInverse \xrightarrow{\text{tex}} \text{“SmallInverse”}]$
 $[MemberOfSeries(ImPLY) \xrightarrow{\text{tex}} \text{“MemberOfSeries(ImPLY)”}]$
 $[NatType \xrightarrow{\text{tex}} \text{“NatType”}]$
 $[RationalType \xrightarrow{\text{tex}} \text{“RationalType”}]$
 $[SeriesType \xrightarrow{\text{tex}} \text{“SeriesType”}]$
 $[JoinConjuncts(2conditions) \xrightarrow{\text{tex}} \text{“JoinConjuncts(2conditions)”}]$
 $[TND \xrightarrow{\text{tex}} \text{“TND”}]$
 $[FromNegatedImPLY \xrightarrow{\text{tex}} \text{“FromNegatedImPLY”}]$
 $[ToNegatedImPLY \xrightarrow{\text{tex}} \text{“ToNegatedImPLY”}]$
 $[FromNegated(2 * ImPLY) \xrightarrow{\text{tex}} \text{“FromNegated(2*ImPLY)”}]$
 $[FromNegatedAnd \xrightarrow{\text{tex}} \text{“FromNegatedAnd”}]$
 $[FromNegatedOr \xrightarrow{\text{tex}} \text{“FromNegatedOr”}]$
 $[ToNegatedOr \xrightarrow{\text{tex}} \text{“ToNegatedOr”}]$
 $[FromNegations \xrightarrow{\text{tex}} \text{“FromNegations”}]$
 $[From3Disjuncts \xrightarrow{\text{tex}} \text{“From3Disjuncts”}]$
 $[NegateDisjunct1 \xrightarrow{\text{tex}} \text{“NegateDisjunct1”}]$
 $[NegateDisjunct2 \xrightarrow{\text{tex}} \text{“NegateDisjunct2”}]$
 $[ExpandDisjuncts \xrightarrow{\text{tex}} \text{“ExpandDisjuncts”}]$
 $[From2 * 2Disjuncts \xrightarrow{\text{tex}} \text{“From2*2Disjuncts”}]$
 $[PlusR(Sym) \xrightarrow{\text{tex}} \text{“PlusR(Sym)”}]$

[LessLeq(R) $\xrightarrow{\text{tex}}$ “LessLeq(R)”]

[LeqAntisymmetry(R) $\xrightarrow{\text{tex}}$ “LeqAntisymmetry(R)”]

[LeqTransitivity(R) $\xrightarrow{\text{tex}}$ “LeqTransitivity(R)”]

[Plus0(R) $\xrightarrow{\text{tex}}$ “Plus0(R)”]

[lessAddition(R) $\xrightarrow{\text{tex}}$ “lessAddition(R)”]

[leqAddition(R) $\xrightarrow{\text{tex}}$ “leqAddition(R)”]

[PlusAssociativity(R)XX $\xrightarrow{\text{tex}}$ “PlusAssociativity(R)XX”]

[PlusAssociativity(R) $\xrightarrow{\text{tex}}$ “PlusAssociativity(R)”]

[Negative(R) $\xrightarrow{\text{tex}}$ “Negative(R)”]

[PlusCommutativity(R) $\xrightarrow{\text{tex}}$ “PlusCommutativity(R)”]

[Times1(R) $\xrightarrow{\text{tex}}$ “Times1(R)”]

[TimesAssociativity(R) $\xrightarrow{\text{tex}}$ “TimesAssociativity(R)”]

[TimesCommutativity(R) $\xrightarrow{\text{tex}}$ “TimesCommutativity(R)”]

[Distribution(R) $\xrightarrow{\text{tex}}$ “Distribution(R)”]

[$\exists x: y \xrightarrow{\text{tex}}$ “(AARRGGHH!-exist-bug!”]

[constantRationalSeries(x) $\xrightarrow{\text{tex}}$ “constantRationalSeries(#1.
)”]

[Power(x) $\xrightarrow{\text{tex}}$ “Power(#1.
)”]

[cartProd(x) $\xrightarrow{\text{tex}}$ “cartProd(#1.
)”]

[binaryUnion(x, y) $\xrightarrow{\text{tex}}$ “binaryUnion(#1.
, #2.
)”]

[SetOfRationalSeries $\xrightarrow{\text{tex}}$ “SetOfRationalSeries”]

[MemberOfSeries $\xrightarrow{\text{tex}}$ “MemberOfSeries”]

[IsSubset(x, y) $\xrightarrow{\text{tex}}$ “IsSubset(#1.
, #2.
)”]

[memberOfSeries(Type) $\xrightarrow{\text{tex}}$ “memberOfSeries(Type)”]

[UniqueMember $\xrightarrow{\text{tex}}$ “UniqueMember”]

[UniqueMember(Type) $\xrightarrow{\text{tex}}$ “UniqueMember(Type)”]

[SameSeries $\xrightarrow{\text{tex}}$ “SameSeries”]

[A4 $\xrightarrow{\text{tex}}$ “A4”]

[(sx) $\xrightarrow{\text{tex}}$ “(s#1.
)”]

[(px, y) $\xrightarrow{\text{tex}}$ “(p#1.
, #2.
)”]

[SameMember $\xrightarrow{\text{tex}}$ “SameMember”]

[Qclosed(Addition) $\xrightarrow{\text{tex}}$ “Qclosed(Addition)”]

[Qclosed(Multiplication) $\xrightarrow{\text{tex}}$ “Qclosed(Multiplication)”]

[FromCartProd(1) $\xrightarrow{\text{tex}}$ “FromCartProd(1)”]

[FromCartProd(1) $\xrightarrow{\text{tex}}$ “FromCartProd(1)”]

[Max $\xrightarrow{\text{tex}}$ “Max”]

[Numerical $\xrightarrow{\text{tex}}$ “Numerical”]

[NumericalF $\xrightarrow{\text{tex}}$ “NumericalF”]

[Separation2formula(1) $\xrightarrow{\text{tex}}$ “Separation2formula(1)”]

[Separation2formula(2) $\xrightarrow{\text{tex}}$ “Separation2formula(2)”]

[QisClosed(Reciprocal)(ImPLY) $\xrightarrow{\text{tex}}$ “QisClosed(Reciprocal)(ImPLY)”]

[QisClosed(Reciprocal) $\xrightarrow{\text{tex}}$ “QisClosed(Reciprocal)”]

[QisClosed(Negative)(ImPLY) $\xrightarrow{\text{tex}}$ “QisClosed(Negative)(ImPLY)”]

[QisClosed(Negative) $\xrightarrow{\text{tex}}$ “QisClosed(Negative)”]

$[(\text{Adgic})\text{SameR} \xrightarrow{\text{tex}} \text{“}(\text{Adgic})\text{SameR”}]$