

(\*\* MAKROER BEGYNDER \*\*)

[ph<sub>1</sub> ≐ a<sub>Ph</sub>]

[ph<sub>2</sub> ≐ b<sub>Ph</sub>]

[ph<sub>3</sub> ≐ c<sub>Ph</sub>]

[ph<sub>4</sub> ≐ d<sub>Ph</sub>]

[ph<sub>5</sub> ≐ e<sub>Ph</sub>]

[ph<sub>6</sub> ≐ f<sub>Ph</sub>]

[x ∧ y ≐ ≐ ((x ⇒ ≐ (y)n))n]

[x ∨ y ≐ ≐ (x)n ⇒ y]

[x ⇔ y ≐ (x ⇒ y) ∧ (y ⇒ x)]

[x ≠ y ≐ ≐ (x==y)n]

[x ∉ y ≐ ≐ (x ∈ y)n]

[x ⊆ y ≐ ≐ (S1ob): ((S1ob) ∈ x ⇒ (S1ob) ∈ y)]

[{x} ≐ {x, x}]

[x ∪ y ≐ ∪ {{x}, {y}}]

[x ∩ y ≐ {ph ∈ x ∪ y | ph<sub>3</sub> ∈ x ∧ ph<sub>3</sub> ∈ y}]

[⟨x, y⟩ ≐ {{x}, {x, y}}]

[r(x, y) ≐ ⟨x, y⟩ ∈ r]

[ReflRel(r, x) ≐ ≐ (s ∈ x ⇒ r(s, s))]

[SymRel(r, x) ≐ ≐ (s ∈ x ⇒ t ∈ x ⇒ r(s, t) ⇒ r(t, s))]

[TransRel(r, x) ≐

≐ (s, t, u: (s ∈ x ⇒ t ∈ x ⇒ u ∈ x ⇒ r(s, t) ⇒ r(t, u) ⇒ r(s, u)))]

[EqRel(r, x) ≐ ReflRel(r, x) ∧ SymRel(r, x) ∧ TransRel(r, x)]

[BS ≐ bs]

[OBS ≐ bs]

[[x ∈ bs]<sub>r</sub> ≐ {ph ∈ bs | r(ph<sub>1</sub>, x)}]

[bs/r ≐ {ph ∈ P(bs) | Ex<sub>20</sub> ∈ bs ∧ [Ex<sub>20</sub> ∈ bs]<sub>r</sub> == ph<sub>2</sub>}]

[Partition(p, bs) ≐ (≐ (s ∈ p ⇒ s ≠ ∅)) ∧

(≐ (s, t: (s ∈ p ⇒ t ∈ p ⇒ s ≠ t ⇒ s ∩ t == ∅)) ∧

∪ p == bs]

(\*\* EKSISTENS-VARIABLE \*\*)

[x<sup>Ex</sup> ≐ x <sup>r</sup> [x<sub>Ex</sub>]]

[EX<sub>1</sub> ≐ a<sub>Ex</sub>]

[EX<sub>2</sub> ≐ b<sub>Ex</sub>]

[EX<sub>10</sub> ≐ j<sub>Ex</sub>]

[EX<sub>20</sub> ≐ t<sub>Ex</sub>]

[⟨a≐b|x:==t⟩<sub>Ex</sub> ≐ ⟨[a]≐<sup>0</sup>[b]||[x]:==[t]⟩<sub>Ex</sub>]

[⟨a≐<sup>0</sup>b|x:==t⟩<sub>Ex</sub> ≐ λc.x<sup>Ex</sup> ∧ ⟨a≐<sup>1</sup>b|x:==t⟩<sub>Ex</sub>]

$[(a \equiv^1 b | x := t)_{\text{Ex}} \doteq a!x!t!]$

**if**  $b \stackrel{r}{\equiv} [\forall u: v]$  **then**  $F$  **else**

**if**  $b^{\text{Ex}} \wedge b \stackrel{t}{\equiv} x$  **then**  $a \stackrel{t}{\equiv} t$  **else**

$a \stackrel{r}{\equiv} b \wedge (a^t \equiv^* b^t | x := t)_{\text{Ex}}$

$[(a \equiv^* b | x := t)_{\text{Ex}} \doteq b!x!t! \text{If}(a, T, (a^h \equiv^1 b^h | x := t)_{\text{Ex}} \wedge (a^t \equiv^* b^t | x := t)_{\text{Ex}})]$

(\*\*\* AKSIOMATISK SYSTEM \*\*\*)

[Theory SystemQ]

[SystemQ rule MP:  $\Pi A, B: A \Rightarrow B \vdash A \vdash B$ ]

[SystemQ rule Gen:  $\Pi \mathcal{X}, A: A \vdash \forall \mathcal{X}: A$ ]

[SystemQ rule Repetition:  $\Pi A: A \vdash A$ ]

[SystemQ rule Neg:  $\Pi A, B: \dot{\vdash}(B)_n \Rightarrow A \vdash \dot{\vdash}(B)_n \Rightarrow \dot{\vdash}(A)_n \vdash B$ ]

[SystemQ rule Ded:  $\Pi A, B: A \vdash B$ ]

[SystemQ rule ExistIntro:  $\Pi \mathcal{X}, T, A, B: (A \equiv B | \mathcal{X} := T)_{\text{Ex}} \Vdash A \vdash B$ ]

[SystemQ rule Extensionality:  $\Pi \mathcal{X}, \mathcal{Y}: \mathcal{X} == \mathcal{Y} \Leftrightarrow \forall s: (s \in \mathcal{X} \Leftrightarrow s \in \mathcal{Y})$ ]

[SystemQ rule  $\emptyset$ def:  $\Pi S: \dot{\vdash}(S \in \emptyset)_n$ ]

[SystemQ rule PairDef:  $\Pi S, \mathcal{X}, \mathcal{Y}: S \in \{\mathcal{X}, \mathcal{Y}\} \Leftrightarrow S == \mathcal{X} \dot{\vee} S == \mathcal{Y}$ ]

[SystemQ rule UnionDef:  $\Pi S, \mathcal{X}: S \in \cup \mathcal{X} \Leftrightarrow (S \in \text{Ex}_{10} \wedge \text{Ex}_{10} \in \mathcal{X})$ ]

[SystemQ rule PowerDef:  $\Pi S, \mathcal{X}: S \in P(\mathcal{X}) \Leftrightarrow \forall s: (s \in S \Rightarrow s \in \mathcal{X})$ ]

[SystemQ rule SeparationDef:  $\Pi A, B, \mathcal{P}, \mathcal{X}, \mathcal{Z}: \mathcal{P}^{\text{Ph}} \wedge (B \equiv A | \mathcal{P} := \mathcal{Z})_{\text{Ph}} \Vdash \mathcal{Z} \in \{\text{ph} \in \mathcal{X} \mid A\} \Leftrightarrow \mathcal{Z} \in \mathcal{X} \wedge B$ ]

————— RRRRRRRRRRRRRRRR —————

(\*\*\* import fra A.M. \*\*\*)

[SystemQ rule TimesCommutativity(R):  $\Pi FX, FY: R(FX)**R(FY) == R(FY)*R(FX)$ ]

(\*\*\* aksiomer \*\*\*)

[SystemQ rule leqReflexivity:  $\Pi \mathcal{X}: \mathcal{X} <= \mathcal{X}$ ]

[SystemQ rule leqAntisymmetryAxiom:  $\Pi \mathcal{X}, \mathcal{Y}: \mathcal{X} <= \mathcal{Y} \Rightarrow \mathcal{Y} <= \mathcal{X} \Rightarrow \mathcal{X} = \mathcal{Y}$ ]

[SystemQ rule leqTransitivityAxiom:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: \mathcal{X} <= \mathcal{Y} \Rightarrow \mathcal{Y} <= \mathcal{Z} \Rightarrow \mathcal{X} <= \mathcal{Z}$ ]

[SystemQ rule leqTotality:  $\Pi \mathcal{X}, \mathcal{Y}: \mathcal{X} <= \mathcal{Y} \dot{\vee} \mathcal{Y} <= \mathcal{X}$ ]

[SystemQ rule leqAdditionAxiom:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: \mathcal{X} <= \mathcal{Y} \Rightarrow (\mathcal{X} + \mathcal{Z}) <= (\mathcal{Y} + \mathcal{Z})$ ]

[SystemQ rule leqMultiplicationAxiom:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: 0 <= \mathcal{Z} \Rightarrow \mathcal{X} <= \mathcal{Y} \Rightarrow (\mathcal{X} * \mathcal{Z}) <= (\mathcal{Y} * \mathcal{Z})$ ]

[SystemQ rule plusAssociativity:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: (((\mathcal{X} + \mathcal{Y})) + \mathcal{Z}) = (\mathcal{X} + ((\mathcal{Y} + \mathcal{Z})))$ ]

[SystemQ rule plusCommutativity:  $\Pi \mathcal{X}, \mathcal{Y}: (\mathcal{X} + \mathcal{Y}) = (\mathcal{Y} + \mathcal{X})$ ]

[SystemQ rule Negative:  $\Pi \mathcal{X}: (\mathcal{X} + ((-\text{u}\mathcal{X}))) = 0$ ]

[SystemQ rule plus0:  $\Pi \mathcal{X}: (\mathcal{X} + 0) = \mathcal{X}$ ]

[SystemQ rule timesAssociativity:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: (((\mathcal{X} * \mathcal{Y})) * \mathcal{Z}) = (\mathcal{X} * ((\mathcal{Y} * \mathcal{Z})))$ ]

[SystemQ rule timesCommutativity:  $\Pi \mathcal{X}, \mathcal{Y}: (\mathcal{X} * \mathcal{Y}) = (\mathcal{Y} * \mathcal{X})$ ]

[SystemQ rule ReciprocalAxiom:  $\Pi \mathcal{X}: \mathcal{X} \neq 0 \Rightarrow (\mathcal{X} * \text{rec}\mathcal{X}) = 1$ ]

[SystemQ rule times1:  $\Pi \mathcal{X}: (\mathcal{X} * 1) = \mathcal{X}$ ]

[SystemQ rule Distribution:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: (\mathcal{X} * ((\mathcal{Y} + \mathcal{Z}))) = (((\mathcal{X} * \mathcal{Y})) + ((\mathcal{X} * \mathcal{Z})))$ ]

[SystemQ rule 0not1:  $0 \neq 1$ ]

[SystemQ rule EqualityAxiom:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: \mathcal{X} = \mathcal{Y} \Rightarrow \mathcal{X} = \mathcal{Z} \Rightarrow \mathcal{Y} = \mathcal{Z}$ ]

[SystemQ rule EqLeqAxiom:  $\Pi \mathcal{X}, \mathcal{Y}: \mathcal{X} = \mathcal{Y} \Rightarrow \mathcal{X} <= \mathcal{Y}$ ]

[SystemQ rule EqAdditionAxiom:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: \mathcal{X} = \mathcal{Y} \Rightarrow (\mathcal{X} + \mathcal{Z}) = (\mathcal{Y} + \mathcal{Z})$ ]

[SystemQ rule EqMultiplicationAxiom:  $\Pi \mathcal{X}, \mathcal{Y}, \mathcal{Z}: \mathcal{X} = \mathcal{Y} \Rightarrow (\mathcal{X} * \mathcal{Z}) = (\mathcal{Y} * \mathcal{Z})$ ]

[SystemQ rule A4(Axiom):  $\Pi \mathcal{X}, V_1, \mathcal{A}, \mathcal{B}: \langle \mathcal{A} \equiv \mathcal{B} \mid V_1 ::= \mathcal{X} \rangle_{\text{Me}} \Vdash \forall V_1: \mathcal{B} \Rightarrow \mathcal{A}$ ]

(\*\* XX snydeaksiomer \*\*)

[SystemQ rule ==Reflexivity:  $\Pi \text{RX}: \text{RX} == \text{RX}$ ]

[SystemQ rule ==Symmetry:  $\Pi \text{RX}, \text{RY}: \text{RX} == \text{RY} \vdash \text{RY} == \text{RX}$ ]

[SystemQ rule ==Transitivity:  $\Pi \text{RX}, \text{RY}, \text{RZ}: \text{RX} == \text{RY} \vdash \text{RY} == \text{RZ} \vdash \text{RX} == \text{RZ}$ ]

XX ikke 100procent identisk med originalen fra equivalence-relations [SystemQ rule ==Transitivity:  $\Pi \text{RX}, \text{RY}: \text{RX} == \text{RY} \vdash \text{FX} \in \text{RX} \vdash \text{FX} \in \text{RY}$ ]

XX boer bevises ud fra nummer 1 [SystemQ rule SENC2:  $\Pi \text{FX}, \text{RX}, \text{RY}: \text{RX} == \text{RY} \vdash \text{FX} \in \text{RY} \vdash \text{FX} \in \text{RX}$ ]

[SystemQ rule PlusF:  $\Pi \mathcal{M}, \text{FX}, \text{FY}: \text{FX} +_{\text{f}} \text{FY}[\mathcal{M}] = (\text{FX}[\mathcal{M}] + \text{FY}[\mathcal{M}])$ ]

[SystemQ rule From ==:  $\Pi \text{FX}, \text{FY}: \text{R}(\text{FX}) == \text{R}(\text{FY}) \vdash \text{SF}(\text{FX}, \text{FY})$ ]

[SystemQ rule To ==:  $\Pi \text{FX}, \text{FY}: \text{SF}(\text{FX}, \text{FY}) \vdash \text{R}(\text{FX}) == \text{R}(\text{FY})$ ]

[SystemQ rule FromInR:  $\Pi \text{FX}, \text{FY}: \text{FX} \in \text{R}(\text{FY}) \vdash \text{SF}(\text{FX}, \text{FY})$ ]

(\*\* makroer \*\*)

KVANTI

$[\overline{\text{M}}_1 \doteq \overline{\text{(m1)}}] [\overline{\text{M}}_2 \doteq \overline{\text{(m2)}}] [\overline{\text{N}}_1 \doteq \overline{\text{(n1)}}] [\overline{\text{N}}_2 \doteq \overline{\text{(n2)}}] [\overline{\text{N}}_3 \doteq \overline{\text{(n3)}}] [\overline{\epsilon} \doteq \overline{(\epsilon)}]$

$[\overline{\epsilon_1} \doteq \overline{(\epsilon_1)}] [\overline{\epsilon_2} \doteq \overline{(\epsilon_2)}] [\overline{\text{X}}_1 \doteq \overline{\text{(x1)}}] [\overline{\text{X}}_2 \doteq \overline{\text{(x2)}}] [\overline{\text{Y}}_1 \doteq \overline{\text{(y1)}}] [\overline{\text{Y}}_2 \doteq \overline{\text{(y2)}}] [\overline{\text{V}}_1 \doteq \overline{\text{(v1)}}]$

$[\overline{\text{V}}_2 \doteq \overline{\text{(v2)}}] [\overline{\text{V}}_3 \doteq \overline{\text{(v3)}}] [\overline{\text{V}}_4 \doteq \overline{\text{(v4)}}] [\overline{\text{V}}_{2n} \doteq \overline{\text{(v2n)}}] [\overline{\text{FX}} \doteq \overline{\text{(fx)}}] [\overline{\text{FY}} \doteq \overline{\text{(fy)}}]$

$[\overline{\text{FZ}} \doteq \overline{\text{(fz)}}] [\overline{\text{FU}} \doteq \overline{\text{(fu)}}] [\overline{\text{FV}} \doteq \overline{\text{(fv)}}] [\overline{\text{FW}} \doteq \overline{\text{(fw)}}] [\overline{\text{FEP}} \doteq \overline{\text{(fep)}}] [\overline{\text{RX}} \doteq \overline{\text{(rx)}}]$

$[\overline{\text{RY}} \doteq \overline{\text{(ry)}}] [\overline{\text{RZ}} \doteq \overline{\text{(rz)}}] [\overline{\text{RU}} \doteq \overline{\text{(ru)}}] [\overline{\text{(SX)}} \doteq \overline{\text{(sx)}}] [\overline{\text{(SX1)}} \doteq \overline{\text{(sx1)}}] [\overline{\text{(SY)}} \doteq \overline{\text{(sy)}}]$

$[\overline{\text{(SY1)}} \doteq \overline{\text{(sy1)}}] [\overline{\text{(SZ)}} \doteq \overline{\text{(sz)}}] [\overline{\text{(SZ1)}} \doteq \overline{\text{(sz1)}}] [\overline{\text{(SU)}} \doteq \overline{\text{(su)}}] [\overline{\text{(SU1)}} \doteq \overline{\text{(su1)}}]$

$[\overline{\text{FXS}} \doteq \overline{\text{(fxs)}}] [\overline{\text{FYS}} \doteq \overline{\text{(fys)}}] [\overline{\text{(F1)}} \doteq \overline{\text{(f1)}}] [\overline{\text{(F2)}} \doteq \overline{\text{(f2)}}] [\overline{\text{(F3)}} \doteq \overline{\text{(f3)}}] [\overline{\text{(F4)}} \doteq \overline{\text{(f4)}}]$

$[\overline{\text{(OP1)}} \doteq \overline{\text{(op1)}}] [\overline{\text{(OP2)}} \doteq \overline{\text{(op2)}}] [\overline{\text{(R1)}} \doteq \overline{\text{(r1)}}] [\overline{\text{(S1)}} \doteq \overline{\text{(s1)}}] [\overline{\text{(S2)}} \doteq \overline{\text{(s2)}}]$

$[\overline{\text{(EPob)}} \doteq \overline{(\epsilon)}] [\overline{\text{(CRS1ob)}} \doteq \overline{\text{(crs1)}}] [\overline{\text{(F1ob)}} \doteq \overline{\text{(f1)}}] [\overline{\text{(F2ob)}} \doteq \overline{\text{(f2)}}] [\overline{\text{(F3ob)}} \doteq \overline{\text{(f3)}}]$

$[\overline{\text{(F4ob)}} \doteq \overline{\text{(f4)}}] [\overline{\text{(N1ob)}} \doteq \overline{\text{(n1)}}] [\overline{\text{(N2ob)}} \doteq \overline{\text{(n2)}}] [\overline{\text{(OP1ob)}} \doteq \overline{\text{(op1)}}]$

$[\overline{\text{(OP2ob)}} \doteq \overline{\text{(op2)}}] [\overline{\text{(R1ob)}} \doteq \overline{\text{(r1)}}] [\overline{\text{(S1ob)}} \doteq \overline{\text{(s1)}}] [\overline{\text{(S2ob)}} \doteq \overline{\text{(s2)}}]$

$[(fx) \leq_f (fy) \doteq (fx) <_f (fy) \dot{\vee} SF((fx), (fy))]$

$[Ex3 \doteq c_{Ex}]$

$[\exists(v1): a \doteq \dot{\neg}(\forall(v1): \dot{\neg}(a)n)n]$

$[x <<== y \doteq x << y \dot{\vee} x == y]$

$[(-1) \doteq (-u1)]$

$[2 \doteq (1 + 1)]$

$[3 \doteq (2 + 1)]$

$[1/2 \doteq rec2]$

$[1/3 \doteq rec3]$

$[2/3 \doteq (2 * 1/3)]$

$[x < y \doteq x <= y \wedge x \neq y]$

$[x \neq y \doteq \dot{\neg}(x = y)n]$

$[(x - y) \doteq (x + (-uy))]$

$[00 \doteq R(0f)]$

$[01 \doteq R(1f)]$

$[x!! == y \doteq \dot{\neg}(x == y)n]$

**(\*\*\* REGELLEMMER \*\*\*)**

**(\*\*\* UDSAGNSLOGIK \*\*\*)**

**[SystemQ lemma ToNegatedImPLY:  $\Pi A, B: A \vdash \dot{\neg}(B)n \vdash \dot{\neg}((A \Rightarrow B)n)$ ]**

**SystemQ proof of ToNegatedImPLY:**

|      |  |   |   |
|------|--|---|---|
| L01: | Block $\gg$  | Begin   | ; |
| L02: | Arbitrary $\gg$  | $A, B$  | ; |
| L03: | Premise $\gg$  | $A$   | ; |
| L04: | Premise $\gg$  | $\dot{\neg}(B)n$  | ; |
| L05: | Premise $\gg$  | $\dot{\neg}(\dot{\neg}((A \Rightarrow B)n)n)$   | ; |
| L06: | RemoveDoubleNeg $\triangleright$ L05 $\gg$                               | $A \Rightarrow B$   | ; |
| L07: | MP $\triangleright$ L06 $\triangleright$ L03 $\gg$                       | $B$   | ; |
| L08: | FromContradiction $\triangleright$ L07 $\triangleright$<br>L04 $\gg$     | $\dot{\neg}((A \Rightarrow B)n)$  | ; |
| L09: | Block $\gg$  | End   | ; |
| L10: | Arbitrary $\gg$  | $A, B$  | ; |
| L11: | Ded $\triangleright$ L09 $\gg$   | $A \Rightarrow \dot{\neg}(B)n \Rightarrow \dot{\neg}(\dot{\neg}((A \Rightarrow B)n)n) \Rightarrow \dot{\neg}((A \Rightarrow B)n)$ | ; |
| L12: | Premise $\gg$  | $A$   | ; |
| L13: | Premise $\gg$  | $\dot{\neg}(B)n$  | ; |
| L14: | MP2 $\triangleright$ L11 $\triangleright$ L12 $\triangleright$ L13 $\gg$ | $\dot{\neg}(\dot{\neg}((A \Rightarrow B)n)n) \Rightarrow \dot{\neg}((A \Rightarrow B)n)$  | ; |
| L15: | AutoImPLY $\gg$  | $\dot{\neg}(\dot{\neg}((A \Rightarrow B)n)n) \Rightarrow \dot{\neg}(\dot{\neg}((A \Rightarrow B)n)n)$                             | ; |
| L16: | Neg $\triangleright$ L14 $\triangleright$ L15 $\gg$                      | $\dot{\neg}((A \Rightarrow B)n)$  | □ |

**[SystemQ lemma TND:  $\Pi A: A \dot{\vee} \dot{\neg}(A)n$ ]**

**SystemQ proof of TND:**

|      |                                       |   |   |
|------|---------------------------------------|---|---|
| L01: | Arbitrary $\gg$                       | $A$   | ; |
| L02: | AutoImPLY $\gg$                       | $\dot{\neg}(A)n \Rightarrow \dot{\neg}(A)n$ | ; |
| L03: | Repetition $\triangleright$ L02 $\gg$ | $A \dot{\vee} \dot{\neg}(A)n$               | □ |

**[SystemQ lemma FromNegations:  $\Pi A, B: A \Rightarrow B \vdash \dot{\neg}(A)n \Rightarrow B \vdash B$ ]**

SystemQ **proof of** FromNegations:

|      |   |   |   |
|------|---|---|---|
| L01: | Arbitrary $\gg$   | $\mathcal{A}, \mathcal{B}$                          | ; |
| L02: | Premise $\gg$   | $\mathcal{A} \Rightarrow \mathcal{B}$               | ; |
| L03: | Premise $\gg$   | $\dot{\neg}(\mathcal{A})_n \Rightarrow \mathcal{B}$ | ; |
| L04: | TND $\gg$   | $\mathcal{A} \dot{\vee} \dot{\neg}(\mathcal{A})_n$  | ; |
| L05: | FromDisjuncts $\triangleright$ L04 $\triangleright$ L02 $\triangleright$<br>L03 $\gg$ | $\mathcal{B}$                                       | □ |

[SystemQ **lemma** prop lemma imply negation:  $\Pi \mathcal{A}: \mathcal{A} \Rightarrow \dot{\neg}(\mathcal{A})_n \vdash \dot{\neg}(\mathcal{A})_n$ ]

SystemQ **proof of** prop lemma imply negation:

|      |   |   |   |
|------|---|---|---|
| L01: | Arbitrary $\gg$   | $\mathcal{A}$   | ; |
| L02: | Premise $\gg$   | $\mathcal{A} \Rightarrow \dot{\neg}(\mathcal{A})_n$               | ; |
| L03: | AutoImPLY $\gg$   | $\dot{\neg}(\mathcal{A})_n \Rightarrow \dot{\neg}(\mathcal{A})_n$ | ; |
| L04: | TND $\gg$   | $\mathcal{A} \dot{\vee} \dot{\neg}(\mathcal{A})_n$                | ; |
| L05: | FromDisjuncts $\triangleright$ L04 $\triangleright$ L02 $\triangleright$<br>L03 $\gg$ | $\dot{\neg}(\mathcal{A})_n$                                       | □ |

[SystemQ **lemma** From3Disjuncts:  $\Pi \mathcal{A}, \mathcal{B}, \mathcal{C}, \mathcal{D}: \mathcal{A} \dot{\vee} \mathcal{B} \dot{\vee} \mathcal{C} \vdash \mathcal{A} \Rightarrow \mathcal{D} \vdash \mathcal{B} \Rightarrow \mathcal{D} \vdash \mathcal{C} \Rightarrow \mathcal{D}$ ]

SystemQ **proof of** From3Disjuncts:

|      |   |   |   |
|------|---|---|---|
| L01: | Block $\gg$   | Begin   | ; |
| L02: | Arbitrary $\gg$   | $\mathcal{A}, \mathcal{B}, \mathcal{C}, \mathcal{D}$  | ; |
| L03: | Premise $\gg$   | $\mathcal{A} \dot{\vee} \mathcal{B} \dot{\vee} \mathcal{C}$   | ; |
| L04: | Premise $\gg$   | $\mathcal{B} \Rightarrow \mathcal{D}$   | ; |
| L05: | Premise $\gg$   | $\mathcal{C} \Rightarrow \mathcal{D}$   | ; |
| L06: | Premise $\gg$   | $\dot{\neg}(\mathcal{A})_n$   | ; |
| L07: | Repetition $\triangleright$ L03 $\gg$   | $\dot{\neg}(\mathcal{A})_n \Rightarrow (\mathcal{B} \dot{\vee} \mathcal{C})$  | ; |
| L08: | MP $\triangleright$ L07 $\triangleright$ L06 $\gg$  | $\mathcal{B} \dot{\vee} \mathcal{C}$  | ; |
| L09: | FromDisjuncts $\triangleright$ L08 $\triangleright$ L04 $\triangleright$<br>L05 $\gg$         | $\mathcal{D}$   | ; |
| L10: | Block $\gg$   | End   | ; |
| L11: | Arbitrary $\gg$   | $\mathcal{A}, \mathcal{B}, \mathcal{C}, \mathcal{D}$  | ; |
| L12: | Ded $\triangleright$ L10 $\gg$  | $\mathcal{A} \dot{\vee} \mathcal{B} \dot{\vee} \mathcal{C} \Rightarrow (\mathcal{B} \Rightarrow \mathcal{D}) \Rightarrow (\mathcal{C} \Rightarrow \mathcal{D}) \Rightarrow \dot{\neg}(\mathcal{A})_n \Rightarrow \mathcal{D}$ | ; |
| L13: | AutoImPLY $\gg$   | $(\mathcal{A} \Rightarrow \mathcal{D}) \Rightarrow \mathcal{A} \Rightarrow \mathcal{D}$   | ; |
| L14: | Premise $\gg$   | $\mathcal{A} \dot{\vee} \mathcal{B} \dot{\vee} \mathcal{C}$   | ; |
| L15: | Premise $\gg$   | $\mathcal{A} \Rightarrow \mathcal{D}$   | ; |
| L16: | Premise $\gg$   | $\mathcal{B} \Rightarrow \mathcal{D}$   | ; |
| L17: | Premise $\gg$   | $\mathcal{C} \Rightarrow \mathcal{D}$   | ; |
| L18: | MP3 $\triangleright$ L12 $\triangleright$ L14 $\triangleright$ L16 $\triangleright$ L17 $\gg$ | $\dot{\neg}(\mathcal{A})_n \Rightarrow \mathcal{D}$   | ; |
| L19: | MP $\triangleright$ L13 $\triangleright$ L15 $\gg$  | $\mathcal{A} \Rightarrow \mathcal{D}$   | ; |
| L20: | FromNegations $\triangleright$ L19 $\triangleright$ L18 $\gg$                                 | $\mathcal{D}$   | □ |

[SystemQ **lemma** NegateDisjunct1:  $\Pi \mathcal{A}, \mathcal{B}: \mathcal{A} \dot{\vee} \mathcal{B} \vdash \dot{\neg}(\mathcal{A})_n \vdash \mathcal{B}$ ]

SystemQ **proof of** NegateDisjunct1:

|      |                                       |   |   |
|------|---------------------------------------|---|---|
| L01: | Arbitrary $\gg$                       | $\mathcal{A}, \mathcal{B}$                          | ; |
| L02: | Premise $\gg$                         | $\mathcal{A} \dot{\vee} \mathcal{B}$                | ; |
| L03: | Premise $\gg$                         | $\dot{\neg}(\mathcal{A})_n$                         | ; |
| L04: | Repetition $\triangleright$ L02 $\gg$ | $\dot{\neg}(\mathcal{A})_n \Rightarrow \mathcal{B}$ | ; |

L05: MP  $\triangleright$  L04  $\triangleright$  L03  $\gg$   $\mathcal{B}$  □

[SystemQ lemma NegateDisjunct2:  $\Pi A, \mathcal{B}: A \dot{\vee} \mathcal{B} \vdash \dot{\neg}(\mathcal{B})_n \vdash A$ ]

SystemQ proof of NegateDisjunct2:

L01: Arbitrary  $\gg$   $A, \mathcal{B}$  ;  
L02: Premise  $\gg$   $A \dot{\vee} \mathcal{B}$  ;  
L03: Premise  $\gg$   $\dot{\neg}(\mathcal{B})_n$  ;  
L04: Repetition  $\triangleright$  L02  $\gg$   $\dot{\neg}(\mathcal{A})_n \Rightarrow \mathcal{B}$  ;  
L05: NegativeMT  $\triangleright$  L04  $\triangleright$  L03  $\gg$   $A$  □

(\*\*\*)

[SystemQ lemma ExpandDisjuncts:  $\Pi A, \mathcal{B}, \mathcal{C}, \mathcal{D}: A \dot{\vee} \mathcal{B} \vdash \mathcal{C} \dot{\vee} \mathcal{D} \vdash \mathcal{B} \dot{\vee} \mathcal{D} \dot{\vee} (A \dot{\wedge} \mathcal{C})$ ]

SystemQ proof of ExpandDisjuncts:

L01: Block  $\gg$  Begin ;  
L02: Arbitrary  $\gg$   $A, \mathcal{B}, \mathcal{C}, \mathcal{D}$  ;  
L03: Premise  $\gg$   $A \dot{\vee} \mathcal{B}$  ;  
L04: Premise  $\gg$   $\mathcal{C} \dot{\vee} \mathcal{D}$  ;  
L05: Premise  $\gg$   $\dot{\neg}(\mathcal{B})_n$  ;  
L06: Premise  $\gg$   $\dot{\neg}(\mathcal{D})_n$  ;  
L07: NegateDisjunct2  $\triangleright$  L03  $\triangleright$  L05  $\gg$   $A$  ;  
L08: NegateDisjunct2  $\triangleright$  L04  $\triangleright$  L06  $\gg$   $\mathcal{C}$  ;  
L09: JoinConjuncts  $\triangleright$  L07  $\triangleright$  L08  $\gg$   $A \dot{\wedge} \mathcal{C}$  ;  
L10: Block  $\gg$  End ;  
L11: Arbitrary  $\gg$   $A, \mathcal{B}, \mathcal{C}, \mathcal{D}$  ;  
L12: Ded  $\triangleright$  L10  $\gg$   $A \dot{\vee} \mathcal{B} \Rightarrow \mathcal{C} \dot{\vee} \mathcal{D} \Rightarrow \dot{\neg}(\mathcal{B})_n \Rightarrow \dot{\neg}(\mathcal{D})_n \Rightarrow A \dot{\wedge} \mathcal{C}$  ;  
L13: Premise  $\gg$   $A \dot{\vee} \mathcal{B}$  ;  
L14: Premise  $\gg$   $\mathcal{C} \dot{\vee} \mathcal{D}$  ;  
L15: MP2  $\triangleright$  L12  $\triangleright$  L13  $\triangleright$  L14  $\gg$   $\dot{\neg}(\mathcal{B})_n \Rightarrow \dot{\neg}(\mathcal{D})_n \Rightarrow A \dot{\wedge} \mathcal{C}$  ;  
L16: Repetition  $\triangleright$  L15  $\gg$   $\mathcal{B} \dot{\vee} \mathcal{D} \dot{\vee} (A \dot{\wedge} \mathcal{C})$  □

[SystemQ lemma From2 \* 2Disjuncts:  $\Pi A, \mathcal{B}, \mathcal{C}, \mathcal{D}, \mathcal{E}: A \dot{\vee} \mathcal{B} \vdash \mathcal{C} \dot{\vee} \mathcal{D} \vdash A \Rightarrow \mathcal{C} \Rightarrow \mathcal{E} \vdash A \Rightarrow \mathcal{D} \Rightarrow \mathcal{E} \vdash \mathcal{B} \Rightarrow \mathcal{C} \Rightarrow \mathcal{E} \vdash \mathcal{B} \Rightarrow \mathcal{D} \Rightarrow \mathcal{E} \vdash \mathcal{E}$ ]

SystemQ proof of From2 \* 2Disjuncts:

L01: Block  $\gg$  Begin ;  
L02: Arbitrary  $\gg$   $A, \mathcal{B}, \mathcal{C}, \mathcal{D}, \mathcal{E}$  ;  
L03: Premise  $\gg$   $\mathcal{C} \dot{\vee} \mathcal{D}$  ;  
L04: Premise  $\gg$   $A \Rightarrow \mathcal{C} \Rightarrow \mathcal{E}$  ;  
L05: Premise  $\gg$   $A \Rightarrow \mathcal{D} \Rightarrow \mathcal{E}$  ;  
L06: Premise  $\gg$   $A$  ;  
L07: MP  $\triangleright$  L04  $\triangleright$  L06  $\gg$   $\mathcal{C} \Rightarrow \mathcal{E}$  ;  
L08: MP  $\triangleright$  L05  $\triangleright$  L06  $\gg$   $\mathcal{D} \Rightarrow \mathcal{E}$  ;  
L09: FromDisjuncts  $\triangleright$  L03  $\triangleright$  L07  $\triangleright$  L08  $\gg$   $\mathcal{E}$  ;  
L10: Block  $\gg$  End ;  
L11: Block  $\gg$  Begin ;  
L12: Arbitrary  $\gg$   $A, \mathcal{B}, \mathcal{C}, \mathcal{D}, \mathcal{E}$  ;  
L13: Premise  $\gg$   $A \dot{\vee} \mathcal{B}$  ;

|      |   |   |           |
|------|---|---|-----------|
| L14: | Premise $\gg$   | $C \dot{\vee} D$  | ;         |
| L15: | Premise $\gg$   | $B \Rightarrow C \Rightarrow \mathcal{E}$   | ;         |
| L16: | Premise $\gg$   | $B \Rightarrow D \Rightarrow \mathcal{E}$   | ;         |
| L17: | Premise $\gg$   | $\dot{\neg}(A)_n$   | ;         |
| L18: | NegateDisjunct1 $\triangleright$ L13 $\triangleright$ L17 $\gg$   | $B$   | ;         |
| L19: | MP $\triangleright$ L15 $\triangleright$ L18 $\gg$  | $C \Rightarrow \mathcal{E}$   | ;         |
| L20: | MP $\triangleright$ L16 $\triangleright$ L18 $\gg$  | $D \Rightarrow \mathcal{E}$   | ;         |
| L21: | FromDisjuncts $\triangleright$ L14 $\triangleright$ L19 $\triangleright$<br>L20 $\gg$                                 | $\mathcal{E}$   | ;         |
| L22: | Block $\gg$   | End   | ;         |
| L23: | Arbitrary $\gg$   | $A, B, C, D, \mathcal{E}$   | ;         |
| L24: | Ded $\triangleright$ L10 $\gg$  | $C \dot{\vee} D \Rightarrow (A \Rightarrow C \Rightarrow \mathcal{E}) \Rightarrow$<br>$(A \Rightarrow D \Rightarrow \mathcal{E}) \Rightarrow A \Rightarrow \mathcal{E}$   | ;         |
| L25: | Ded $\triangleright$ L22 $\gg$  | $A \dot{\vee} B \Rightarrow C \dot{\vee} D \Rightarrow (B \Rightarrow$<br>$C \Rightarrow \mathcal{E}) \Rightarrow (B \Rightarrow D \Rightarrow \mathcal{E}) \Rightarrow$<br>$\dot{\neg}(A)_n \Rightarrow \mathcal{E}$ | ;         |
| L26: | Premise $\gg$   | $A \dot{\vee} B$  | ;         |
| L27: | Premise $\gg$   | $C \dot{\vee} D$  | ;         |
| L28: | Premise $\gg$   | $A \Rightarrow C \Rightarrow \mathcal{E}$   | ;         |
| L29: | Premise $\gg$   | $A \Rightarrow D \Rightarrow \mathcal{E}$   | ;         |
| L30: | Premise $\gg$   | $B \Rightarrow C \Rightarrow \mathcal{E}$   | ;         |
| L31: | Premise $\gg$   | $B \Rightarrow D \Rightarrow \mathcal{E}$   | ;         |
| L32: | MP3 $\triangleright$ L24 $\triangleright$ L27 $\triangleright$ L28 $\triangleright$ L29 $\gg$                         | $A \Rightarrow \mathcal{E}$   | ;         |
| L33: | MP4 $\triangleright$ L25 $\triangleright$ L26 $\triangleright$ L27 $\triangleright$<br>L30 $\triangleright$ L31 $\gg$ | $\dot{\neg}(A)_n \Rightarrow \mathcal{E}$   | ;         |
| L34: | FromNegations $\triangleright$ L32 $\triangleright$ L33 $\gg$   | $\mathcal{E}$   | $\square$ |

(\*\*\*) SAME-F (\*\*\*) XX-am

(\*\*\*) R-AFDELINGEN (\*\*\*) XX-am

(\*\*\*\*\*)

[SystemQ lemma FromNegatedImPLY:  $\Pi A, B: \dot{\neg}((A \Rightarrow B))_n \vdash A \wedge \dot{\neg}(B)_n]$

SystemQ proof of FromNegatedImPLY:

|      |  |   |           |
|------|--|---|-----------|
| L01: | Block $\gg$  | Begin   | ;         |
| L02: | Arbitrary $\gg$                                    | $A, B$  | ;         |
| L03: | Premise $\gg$                                      | $A \Rightarrow \dot{\neg}(\dot{\neg}(B)_n)_n$                                 | ;         |
| L04: | Premise $\gg$                                      | $A$   | ;         |
| L05: | MP $\triangleright$ L03 $\triangleright$ L04 $\gg$ | $\dot{\neg}(\dot{\neg}(B)_n)_n$   | ;         |
| L06: | RemoveDoubleNeg $\triangleright$ L05 $\gg$         | $B$   | ;         |
| L07: | Block $\gg$  | End   | ;         |
| L08: | Arbitrary $\gg$                                    | $A, B$  | ;         |
| L03: | Ded $\triangleright$ L07 $\gg$                     | $(A \Rightarrow \dot{\neg}(\dot{\neg}(B)_n)_n) \Rightarrow (A \Rightarrow B)$ | ;         |
| L04: | Premise $\gg$                                      | $\dot{\neg}((A \Rightarrow B))_n$   | ;         |
| L05: | MT $\triangleright$ L03 $\triangleright$ L04 $\gg$ | $\dot{\neg}((A \Rightarrow \dot{\neg}(\dot{\neg}(B)_n)_n))_n$                 | ;         |
| L09: | Repetition $\triangleright$ L05 $\gg$              | $A \wedge \dot{\neg}(B)_n$  | $\square$ |

(\*\*\*)

[SystemQ lemma FromNegated(2 \* ImPLY):  $\Pi A, B, C: \dot{\neg}((A \Rightarrow B \Rightarrow C))_n \vdash A \wedge B \wedge \dot{\neg}(C)_n]$

SystemQ **proof of** FromNegated(2 \* Imply):

|      |   |   |           |
|------|---|---|-----------|
| L01: | Arbitrary $\gg$   | $\mathcal{A}, \mathcal{B}, \mathcal{C}$                                       | ;         |
| L02: | Premise $\gg$   | $\dot{\neg}((\mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{C}))_n$ | ;         |
| L03: | FromNegatedImply $\triangleright$ L02 $\gg$                   | $\mathcal{A} \wedge \dot{\neg}((\mathcal{B} \Rightarrow \mathcal{C}))_n$      | ;         |
| L04: | FirstConjunct $\triangleright$ L03 $\gg$                      | $\mathcal{A}$   | ;         |
| L05: | SecondConjunct $\triangleright$ L03 $\gg$                     | $\dot{\neg}((\mathcal{B} \Rightarrow \mathcal{C}))_n$                         | ;         |
| L06: | FromNegatedImply $\triangleright$ L05 $\gg$                   | $\mathcal{B} \wedge \dot{\neg}(\mathcal{C})_n$                                | ;         |
| L07: | FirstConjunct $\triangleright$ L06 $\gg$                      | $\mathcal{B}$   | ;         |
| L08: | SecondConjunct $\triangleright$ L06 $\gg$                     | $\dot{\neg}(\mathcal{C})_n$   | ;         |
| L09: | JoinConjuncts $\triangleright$ L04 $\triangleright$ L07 $\gg$ | $\mathcal{A} \wedge \mathcal{B}$  | ;         |
| L10: | JoinConjuncts $\triangleright$ L09 $\triangleright$ L08 $\gg$ | $\mathcal{A} \wedge \mathcal{B} \wedge \dot{\neg}(\mathcal{C})_n$             | $\square$ |

[SystemQ **lemma** FromNegatedOr:  $\Pi \mathcal{A}, \mathcal{B}: \dot{\neg}((\mathcal{A} \dot{\vee} \mathcal{B}))_n \vdash \dot{\neg}(\mathcal{A})_n \wedge \dot{\neg}(\mathcal{B})_n$ ]

SystemQ **proof of** FromNegatedOr:

|      |   |   |           |
|------|---|---|-----------|
| L01: | Arbitrary $\gg$                             | $\mathcal{A}, \mathcal{B}$  | ;         |
| L02: | Premise $\gg$                               | $\dot{\neg}((\mathcal{A} \dot{\vee} \mathcal{B}))_n$              | ;         |
| L03: | Repetition $\triangleright$ L02 $\gg$       | $\dot{\neg}(\dot{\neg}(\mathcal{A})_n \Rightarrow \mathcal{B})_n$ | ;         |
| L04: | FromNegatedImply $\triangleright$ L03 $\gg$ | $\dot{\neg}(\mathcal{A})_n \wedge \dot{\neg}(\mathcal{B})_n$      | $\square$ |

[SystemQ **rule** InductionAxiom:  $\Pi V_1, \mathcal{A}, \mathcal{B}, \mathcal{C}: \langle \mathcal{B} \equiv \mathcal{A} | V_1 := 0 \rangle_{\text{Me}} \vdash \langle \mathcal{C} \equiv \mathcal{A} | V_1 := 1 \rangle_{\text{Me}} \vdash \mathcal{B} \Rightarrow \forall V_1: (\mathcal{A} \Rightarrow \mathcal{C}) \Rightarrow \forall V_1: \mathcal{A}$ ]

[SystemQ **rule** LessMinus1(N):  $\Pi \mathcal{M}, \mathcal{N}: \text{Nat}(\mathcal{M}) \vdash \text{Nat}(\mathcal{N}) \vdash \mathcal{M} < (\mathcal{N} + 1) \vdash \mathcal{M} \leq \mathcal{N}$ ]

[SystemQ **rule** Nonnegative(N):  $\Pi \mathcal{M}: \text{Nat}(\mathcal{M}) \vdash 0 \leq \mathcal{M}$ ]

[SystemQ **rule** Cauchy:  $\Pi V_1, V_2, \mathcal{N}, \epsilon, \text{FX}: \forall \epsilon: \exists \mathcal{N}: \forall V_1, V_2: (0 < \epsilon \Rightarrow \mathcal{N} \leq V_1 \Rightarrow \mathcal{N} \leq V_2 \Rightarrow |(\text{FX}[V_1] - \text{FX}[V_2])| < \epsilon)$ ]

[SystemQ **lemma** JoinConjuncts(2conditions):  $\Pi \mathcal{A}, \mathcal{B}, \mathcal{C}, \mathcal{D}: \mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{C} \vdash \mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{D} \vdash \mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{C} \wedge \mathcal{D}$ ]

SystemQ **proof of** JoinConjuncts(2conditions):

|      |  |  |           |
|------|--|--|-----------|
| L01: | Block $\gg$  | Begin  | ;         |
| L02: | Arbitrary $\gg$  | $\mathcal{A}, \mathcal{B}, \mathcal{C}, \mathcal{D}$   | ;         |
| L03: | Premise $\gg$  | $\mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{C}$  | ;         |
| L04: | Premise $\gg$  | $\mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{D}$  | ;         |
| L05: | Premise $\gg$  | $\mathcal{A}$  | ;         |
| L06: | Premise $\gg$  | $\mathcal{B}$  | ;         |
| L07: | MP2 $\triangleright$ L03 $\triangleright$ L05 $\triangleright$ L06 $\gg$ | $\mathcal{C}$  | ;         |
| L08: | MP2 $\triangleright$ L04 $\triangleright$ L05 $\triangleright$ L06 $\gg$ | $\mathcal{D}$  | ;         |
| L09: | JoinConjuncts $\triangleright$ L07 $\triangleright$ L08 $\gg$            | $\mathcal{C} \wedge \mathcal{D}$   | ;         |
| L10: | Block $\gg$  | End  | ;         |
| L11: | Arbitrary $\gg$  | $\mathcal{A}, \mathcal{B}, \mathcal{C}, \mathcal{D}$   | ;         |
| L03: | Ded $\triangleright$ L10 $\gg$   | $(\mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{C}) \Rightarrow (\mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{D}) \Rightarrow \mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{C} \wedge \mathcal{D}$ | ;         |
| L04: | Premise $\gg$  | $\mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{C}$  | ;         |
| L05: | Premise $\gg$  | $\mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{D}$  | ;         |
| L12: | MP2 $\triangleright$ L03 $\triangleright$ L04 $\triangleright$ L05 $\gg$ | $\mathcal{A} \Rightarrow \mathcal{B} \Rightarrow \mathcal{C} \wedge \mathcal{D}$   | $\square$ |



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[SystemQ **lemma** FromNegatedAnd:  $\Pi A, B: \dot{\neg}((A \dot{\wedge} B))_n \vdash A \vdash \dot{\neg}(B)_n$ ]

SystemQ **proof of** FromNegatedAnd:

|      |  |   |   |
|------|--|---|---|
| L01: | Arbitrary $\gg$                                    | $A, B$  | ; |
| L02: | Premise $\gg$                                      | $\dot{\neg}((A \dot{\wedge} B))_n$                          | ; |
| L03: | Premise $\gg$                                      | $A$   | ; |
| L04: | Repetition $\triangleright$ L02 $\gg$              | $\dot{\neg}(\dot{\neg}((A \Rightarrow \dot{\neg}(B))_n))_n$ | ; |
| L05: | RemoveDoubleNeg $\triangleright$ L04 $\gg$         | $A \Rightarrow \dot{\neg}(B)_n$                             | ; |
| L06: | MP $\triangleright$ L05 $\triangleright$ L03 $\gg$ | $\dot{\neg}(B)_n$   | □ |

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[SystemQ **lemma** ToNegatedOr:  $\Pi A, B: \dot{\neg}(A)_n \dot{\wedge} \dot{\neg}(B)_n \vdash \dot{\neg}((A \dot{\vee} B))_n$ ]

SystemQ **proof of** ToNegatedOr:

|      |  |   |   |
|------|--|---|---|
| L01: | Block $\gg$  | Begin   | ; |
| L02: | Arbitrary $\gg$  | $A, B$  | ; |
| L03: | Premise $\gg$  | $\dot{\neg}(A)_n \dot{\wedge} \dot{\neg}(B)_n$  | ; |
| L04: | Premise $\gg$  | $A \dot{\vee} B$  | ; |
| L05: | FirstConjunct $\triangleright$ L03 $\gg$                             | $\dot{\neg}(A)_n$   | ; |
| L06: | SecondConjunct $\triangleright$ L03 $\gg$                            | $\dot{\neg}(B)_n$   | ; |
| L07: | NegateDisjunct1 $\triangleright$ L04 $\triangleright$ L05 $\gg$      | $B$   | ; |
| L08: | FromContradiction $\triangleright$ L07 $\triangleright$<br>L06 $\gg$ | $\dot{\neg}((A \dot{\vee} B))_n$  | ; |
| L09: | Block $\gg$  | End   | ; |
| L10: | Arbitrary $\gg$  | $A, B$  | ; |
| L03: | Ded $\triangleright$ L09 $\gg$                                       | $\dot{\neg}(A)_n \dot{\wedge} \dot{\neg}(B)_n \Rightarrow A \dot{\vee} B \Rightarrow$<br>$\dot{\neg}((A \dot{\vee} B))_n$ | ; |
| L04: | Premise $\gg$  | $\dot{\neg}(A)_n \dot{\wedge} \dot{\neg}(B)_n$  | ; |
| L05: | MP $\triangleright$ L03 $\triangleright$ L04 $\gg$                   | $A \dot{\vee} B \Rightarrow \dot{\neg}((A \dot{\vee} B))_n$   | ; |
| L11: | prop lemma imply negation $\triangleright$<br>L05 $\gg$              | $\dot{\neg}((A \dot{\vee} B))_n$  | □ |

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[SystemQ **rule** NextXS(UpperBound):  $\Pi M: UB(01//02**(xs[\mathcal{M}]++us[\mathcal{M}]), S(xs[\mathcal{M}+1]) == xs[\mathcal{M}])$ ]

[SystemQ **rule** NextXS(NoUpperBound):  $\Pi M: \dot{\neg}(UB(01//02**(xs[\mathcal{M}]++us[\mathcal{M}]), S(xs[\mathcal{M}+1]) == 01//02**(xs[\mathcal{M}]+us[\mathcal{M}]))$ ]

[SystemQ **rule** NextUS(UpperBound):  $\Pi M: UB(01//02**(xs[\mathcal{M}]++us[\mathcal{M}]), S(us[\mathcal{M}+1]) == 01//02**(xs[\mathcal{M}]+us[\mathcal{M}]))$ ]

[SystemQ **rule** NextUS(NoUpperBound):  $\Pi M: \dot{\neg}(UB(01//02**(xs[\mathcal{M}]++us[\mathcal{M}]), S(us[\mathcal{M}+1]) == us[\mathcal{M}]))$ ]

[SystemQ **rule** US0:  $us[0] == xs[0] + 01$ ]

[SystemQ **rule** ExpZero:  $\Pi M, \mathcal{X}: \mathcal{M} = 0 \vdash \mathcal{X}(\text{exp})\mathcal{M} = 1$ ]

[SystemQ **rule** ExpPositive:  $\Pi M, \mathcal{X}: 0 < \mathcal{M} \vdash \mathcal{X}(\text{exp})\mathcal{M} = (\mathcal{X}*\mathcal{X}(\text{exp}))((\mathcal{M}-1))$ ]

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[SystemQ **rule** BSzero:  $\Pi M, \mathcal{N}: \mathcal{N} = 0 \vdash BS(\mathcal{M}, \mathcal{N}) = 1/2(\text{exp})\mathcal{M}$ ]

[SystemQ rule BSpositive:  $\Pi \mathcal{M}, \mathcal{N}: 0 < \mathcal{N} \vdash \text{BS}(\mathcal{M}, \mathcal{N}) = (1/2(\text{exp})((\mathcal{M} + \mathcal{N}) + \text{BS}(\mathcal{M}, (\mathcal{N} - 1))))$ ]

[SystemQ rule USteelescope(Zero):  $\Pi \mathcal{M}, \mathcal{N}: \mathcal{N} = 0 \vdash \text{USteelescope}(\mathcal{M}, \mathcal{N}) = |(\text{us}[\mathcal{M}] - \text{us}[(\mathcal{M} + 1)])|$ ]

[SystemQ rule USteelescope(Positive):  $\Pi \mathcal{M}, \mathcal{N}: 0 < \mathcal{N} \vdash \text{USteelescope}(\mathcal{M}, \mathcal{N}) = |(|(\text{us}[(\mathcal{M} + \mathcal{N})] - \text{us}[(\mathcal{M} + ((\mathcal{N} + 1))])|) + \text{USteelescope}(\mathcal{M}, (\mathcal{N} - 1)))|$   
 $(x) \doteq (x)$

[SystemQ rule EqAddition(R):  $\text{IF } X, Y, Z: \text{R}(X) = \text{R}(Y) \vdash \text{R}(X) + \text{R}(Z) = \text{R}(Y) + \text{R}(Z)$ ]

[SystemQ rule PlusCommutativity(R):  $\text{IF } X, Y: \text{R}(X) ++ \text{R}(Y) == \text{R}(Y) ++ \text{R}(X)$ ]

[SystemQ rule PlusAssociativity(R):  $\text{IF } X, Y, Z: \text{R}(X) ++ \text{R}(Y) ++ \text{R}(Z) == \text{R}(X) ++ (\text{R}(Y) ++ \text{R}(Z))$ ]

[SystemQ rule PlusAssociativity(R)XX:  $\text{IF } X, Y, Z: \text{R}(X +_f Y +_f Z) == \text{R}(X +_f (Y +_f Z))$ ]

[SystemQ rule Plus0(R):  $\text{IF } X: \text{R}(X) + +00 == \text{R}(X)$ ]

[SystemQ rule Negative(R):  $\Pi \mathcal{M}, \mathcal{F}: \text{R}(\mathcal{F}) + +(- - \text{R}(\mathcal{F})) == 00$ ]

[SystemQ rule TimesAssociativity(R):  $\text{IF } X, Y, Z: \text{R}(X) ** \text{R}(Y) ** \text{R}(Z) == \text{R}(X) ** (\text{R}(Y) ** \text{R}(Z))$ ]

[SystemQ rule Times1(R):  $\text{IF } X: \text{R}(X) * *01 == \text{R}(X)$ ]

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## Priority table

### Preassociative

[kvanti], [base], [bracket \* end bracket], [big bracket \* end bracket], [ \$ \* \$ ],  
**[flush left** [\*], [x], [y], [z], [[\*  $\bowtie$  \*]], [[\*  $\xrightarrow{*}$  \*]], [pyk], [tex], [name], [prio], [\*], [T],  
 [if(\*, \*, \*)], [[\*  $\xrightarrow{*}$  \*]], [val], [claim], [ $\perp$ ], [f(\*)], [(\*)<sup>I</sup>], [F], [0], [1], [2], [3], [4], [5], [6],  
 [7], [8], [9], [0], [1], [2], [3], [4], [5], [6], [7], [8], [9], [a], [b], [c], [d], [e], [f], [g], [h], [i], [j],  
 [k], [l], [m], [n], [o], [p], [q], [r], [s], [t], [u], [v], [w], [(\*)<sup>M</sup>], [If(\*, \*, \*)],  
 [array{\*} \* end array], [l], [c], [r], [empty], [( \* | \* := \* )], [ $\mathcal{M}(*)$ ], [ $\tilde{\mathcal{U}}(*)$ ], [ $\mathcal{U}(*)$ ],  
 $\mathcal{U}^M(*)$ , [**apply**(\*, \*)], [**apply**<sub>1</sub>(\*, \*)], [identifier(\*)], [identifier<sub>1</sub>(\*, \*)], [array-  
 plus(\*, \*)], [array-remove(\*, \*, \*)], [array-put(\*, \*, \*, \*)], [array-add(\*, \*, \*, \*, \*)],  
 [bit(\*, \*)], [bit<sub>1</sub>(\*, \*)], [rack], ["vector"], ["bibliography"], ["dictionary"],  
 ["body"], ["codex"], ["expansion"], ["code"], ["cache"], ["diagnose"], ["pyk"],  
 ["tex"], ["texname"], ["value"], ["message"], ["macro"], ["definition"],  
 ["unpack"], ["claim"], ["priority"], ["lambda"], ["apply"], ["true"], ["if"],  
 ["quote"], ["proclaim"], ["define"], ["introduce"], ["hide"], ["pre"], ["post"],  
 $\mathcal{E}(*, *, *)$ ,  $\mathcal{E}_2(*, *, *, *, *)$ ,  $\mathcal{E}_3(*, *, *, *)$ ,  $\mathcal{E}_4(*, *, *, *)$ , [**lookup**(\*, \*, \*)],  
**[abstract**(\*, \*, \*, \*)], [[\*]], [ $\mathcal{M}(*, *, *)$ ], [ $\mathcal{M}_2(*, *, *, *)$ ], [ $\mathcal{M}^(*, *, *)$ ], [macro],  
 $s_0$ , [**zip**(\*, \*)], [**assoc**<sub>1</sub>(\*, \*, \*)], [(\*)<sup>P</sup>], [self], [[\*  $\doteq$  \*]], [[\*  $\doteq$  \*]], [[\*  $\doteq$  \*]],  
 [[\*  $\stackrel{\text{pyk}}{=}$  \*]], [[\*  $\stackrel{\text{tex}}{=}$  \*]], [[\*  $\stackrel{\text{name}}{=}$  \*]], [**Priority table**[\*]], [ $\tilde{\mathcal{M}}_1$ ], [ $\tilde{\mathcal{M}}_2(*)$ ], [ $\tilde{\mathcal{M}}_3(*)$ ],

$[\tilde{\mathcal{M}}_4(*, *, *, *)], [\tilde{\mathcal{M}}(*, *, *)], [\tilde{\mathcal{Q}}(*, *, *)], [\tilde{\mathcal{Q}}_2(*, *, *)], [\tilde{\mathcal{Q}}_3(*, *, *, *)], [\tilde{\mathcal{Q}}^*(*, *, *)],$   
 $[(*)], [(*)], [\text{display}(*)], [\text{statement}(*)], [(*)^+], [(*)^-], [\text{aspect}(*, *)],$   
 $[\text{aspect}(*, *, *)], [(\langle * \rangle)], [\text{tuple}_1(*)], [\text{tuple}_2(*)], [\text{let}_2(*, *)], [\text{let}_1(*, *)],$   
 $[(*)^{\text{claim}}], [\text{checker}], [\text{check}(*, *)], [\text{check}_2(*, *, *)], [\text{check}_3(*, *, *, *)],$   
 $[\text{check}^*(*, *)], [\text{check}_2^*(*, *, *)], [(*)^+], [(*)^-], [(*)^\circ], [\text{msg}], [(*)^{\text{msg}}], [\text{<stmt>}],$   
 $[\text{stmt}], [(*)^{\text{stmt}}], [\text{HeadNil}'], [\text{HeadPair}'], [\text{Transitivity}'], [\perp], [\text{Contra}'], [\text{T}_E],$   
 $[\mathcal{L}_1], [*, [\mathcal{A}], [\mathcal{B}], [\mathcal{C}], [\mathcal{D}], [\mathcal{E}], [\mathcal{F}], [\mathcal{G}], [\mathcal{H}], [\mathcal{I}], [\mathcal{J}], [\mathcal{K}], [\mathcal{L}], [\mathcal{M}], [\mathcal{N}], [\mathcal{O}], [\mathcal{P}], [\mathcal{Q}],$   
 $[\mathcal{R}], [\mathcal{S}], [\mathcal{T}], [\mathcal{U}], [\mathcal{V}], [\mathcal{W}], [\mathcal{X}], [\mathcal{Y}], [\mathcal{Z}], [( * | * := * )], [( * * | * := * )], [\emptyset], [\text{Remainder}],$   
 $[(*)^\vee], [\text{intro}(*, *, *, *)], [\text{intro}(*, *, *)], [\text{error}(*, *)], [\text{error}_2(*, *)], [\text{proof}(*, *, *)],$   
 $[\text{proof}_2(*, *)], [\mathcal{S}(*, *)], [\mathcal{S}^I(*, *)], [\mathcal{S}^\triangleright(*, *)], [\mathcal{S}^\triangleleft(*, *, *)], [\mathcal{S}^E(*, *)], [\mathcal{S}^F(*, *, *)],$   
 $[\mathcal{S}^+(*, *)], [\mathcal{S}_1^+(*, *, *)], [\mathcal{S}^-(*, *)], [\mathcal{S}_1^-(*, *, *)], [\mathcal{S}^*(*, *)], [\mathcal{S}_1^*(*, *, *)],$   
 $[\mathcal{S}_2^*(*, *, *, *)], [\mathcal{S}^\circledast(*, *)], [\mathcal{S}_1^\circledast(*, *, *)], [\mathcal{S}^+(*, *)], [\mathcal{S}_1^+(*, *, *, *)], [\mathcal{S}^{\text{H}}(*, *)],$   
 $[\mathcal{S}_1^{\text{H}}(*, *, *, *)], [\mathcal{S}^{\text{i.e.}}(*, *)], [\mathcal{S}_1^{\text{i.e.}}(*, *, *, *)], [\mathcal{S}_2^{\text{i.e.}}(*, *, *, *, *)], [\mathcal{S}^\vee(*, *)],$   
 $[\mathcal{S}_1^\vee(*, *, *, *)], [\mathcal{S}^{\text{i}}(*, *)], [\mathcal{S}_1^{\text{i}}(*, *, *)], [\mathcal{S}_2^{\text{i}}(*, *, *, *)], [\mathcal{T}(*)], [\text{claims}(*, *, *)],$   
 $[\text{claims}_2(*, *, *)], [\text{<proof>}], [\text{proof}], [[\text{Lemma } * : *]], [[\text{Proof of } * : *]],$   
 $[[ * \text{ lemma } * : * ]], [[ * \text{ antilemma } * : * ]], [[ * \text{ rule } * : * ]], [[ * \text{ antirule } * : * ]],$   
 $[\text{verifier}], [\mathcal{V}_1(*)], [\mathcal{V}_2(*, *)], [\mathcal{V}_3(*, *, *, *)], [\mathcal{V}_4(*, *)], [\mathcal{V}_5(*, *, *, *)], [\mathcal{V}_6(*, *, *, *)],$   
 $[\mathcal{V}_7(*, *, *, *)], [\text{Cut}(*, *)], [\text{Head}_\oplus(*)], [\text{Tail}_\oplus(*)], [\text{rule}_1(*, *)], [\text{rule}(*, *)],$   
 $[\text{Rule tactic}], [\text{Plus}(*, *)], [[\text{Theory } *]], [\text{theory}_2(*, *)], [\text{theory}_3(*, *)],$   
 $[\text{theory}_4(*, *, *)], [\text{HeadNil}''], [\text{HeadPair}''], [\text{Transitivity}''], [\text{Contra}''], [\text{HeadNil}],$   
 $[\text{HeadPair}], [\text{Transitivity}], [\text{Contra}], [\text{T}_E], [\text{ragged right}],$   
 $[\text{ragged right expansion }], [\text{parm}(*, *, *)], [\text{parm}^*(*, *, *)], [\text{inst}(*, *)],$   
 $[\text{inst}^*(*, *)], [\text{occur}(*, *, *)], [\text{occur}^*(*, *, *)], [\text{unify}(* = *, *)], [\text{unify}^*( * = *, *)],$   
 $[\text{unify}_2(* = *, *)], [\mathcal{L}_a], [\mathcal{L}_b], [\mathcal{L}_c], [\mathcal{L}_d], [\mathcal{L}_e], [\mathcal{L}_f], [\mathcal{L}_g], [\mathcal{L}_h], [\mathcal{L}_i], [\mathcal{L}_j], [\mathcal{L}_k], [\mathcal{L}_l], [\mathcal{L}_m],$   
 $[\mathcal{L}_n], [\mathcal{L}_o], [\mathcal{L}_p], [\mathcal{L}_q], [\mathcal{L}_r], [\mathcal{L}_s], [\mathcal{L}_t], [\mathcal{L}_u], [\mathcal{L}_v], [\mathcal{L}_w], [\mathcal{L}_x], [\mathcal{L}_y], [\mathcal{L}_z], [\mathcal{L}_A], [\mathcal{L}_B], [\mathcal{L}_C],$   
 $[\mathcal{L}_D], [\mathcal{L}_E], [\mathcal{L}_F], [\mathcal{L}_G], [\mathcal{L}_H], [\mathcal{L}_I], [\mathcal{L}_J], [\mathcal{L}_K], [\mathcal{L}_L], [\mathcal{L}_M], [\mathcal{L}_N], [\mathcal{L}_O], [\mathcal{L}_P], [\mathcal{L}_Q], [\mathcal{L}_R],$   
 $[\mathcal{L}_S], [\mathcal{L}_T], [\mathcal{L}_U], [\mathcal{L}_V], [\mathcal{L}_W], [\mathcal{L}_X], [\mathcal{L}_Y], [\mathcal{L}_Z], [\mathcal{L}_?], [\text{Reflexivity}], [\text{Reflexivity}_1],$   
 $[\text{Commutativity}], [\text{Commutativity}_1], [\text{<tactic>}], [\text{tactic}], [(*)^{\text{tactic}}], [\mathcal{P}(*, *, *)],$   
 $[\mathcal{P}^*(*, *, *)], [\text{p}_0], [\text{conclude}_1(*, *)], [\text{conclude}_2(*, *, *)], [\text{conclude}_3(*, *, *, *)],$   
 $[\text{conclude}_4(*, *)], [\text{check}], [(*)^{\circ}], [\text{RootVisible}(*)], [\mathcal{A}], [\mathcal{R}], [\mathcal{C}], [\mathcal{T}], [\mathcal{L}], [\{ * \}], [\bar{*}],$   
 $[a], [b], [c], [d], [e], [f], [g], [h], [i], [j], [k], [l], [m], [n], [o], [p], [q], [r], [s], [t], [u], [v],$   
 $[w], [x], [y], [z], [( * \equiv * | * := * )], [( * \equiv^0 * | * := * )], [( * \equiv^1 * | * := * )], [( * \equiv^* * | * := * )],$   
 $[\text{Ded}(*, *)], [\text{Ded}_0(*, *)], [\text{Ded}_1(*, *, *)], [\text{Ded}_2(*, *, *)], [\text{Ded}_3(*, *, *, *)],$   
 $[\text{Ded}_4(*, *, *, *)], [\text{Ded}_4^*(*, *, *, *)], [\text{Ded}_5(*, *, *)], [\text{Ded}_6(*, *, *, *)],$   
 $[\text{Ded}_6^*(*, *, *, *)], [\text{Ded}_7(*, *)], [\text{Ded}_8(*, *)], [\text{Ded}_8^*(*, *)], [\text{S}], [\text{Neg}], [\text{MP}], [\text{Gen}],$   
 $[\text{Ded}], [\text{S}_1], [\text{S}_2], [\text{S}_3], [\text{S}_4], [\text{S}_5], [\text{S}_6], [\text{S}_7], [\text{S}_8], [\text{S}_9], [\text{Repetition}], [\text{A1}'], [\text{A2}'], [\text{A4}'],$   
 $[\text{A5}'], [\text{Prop 3.2a}], [\text{Prop 3.2b}], [\text{Prop 3.2c}], [\text{Prop 3.2d}], [\text{Prop 3.2e}_1], [\text{Prop 3.2e}_2],$   
 $[\text{Prop 3.2e}], [\text{Prop 3.2f}_1], [\text{Prop 3.2f}_2], [\text{Prop 3.2f}], [\text{Prop 3.2g}_1], [\text{Prop 3.2g}_2],$   
 $[\text{Prop 3.2g}], [\text{Prop 3.2h}_1], [\text{Prop 3.2h}_2], [\text{Prop 3.2h}], [\text{Block}_1(*, *, *)], [\text{Block}_2(*, *)],$   
 $[\text{UniqueMember}], [\text{UniqueMember}(\text{Type})], [\text{SameSeries}], [\text{A4}], [\text{SameMember}],$   
 $[\text{Qclosed}(\text{Addition})], [\text{Qclosed}(\text{Multiplication})], [\text{FromCartProd}(1)],$   
 $[\text{Irule fromCartProd}(2)], [\text{constantRationalSeries}(*)], [\text{cartProd}(*, *)], [\text{Power}(*)],$   
 $[\text{binaryUnion}(*, *)], [\text{SetOfRationalSeries}], [\text{IsSubset}(*, *)], [(p*, *)], [(s*)],$   
 $[(\cdot \cdot \cdot)], [\text{Objekt-var}], [\text{Ex-var}], [\text{Ph-var}], [\text{Værdi}], [\text{Variabel}], [\text{Op}(*, *)], [\text{Op}(*, *, *)],$   
 $[* \equiv *], [\text{ContainsEmpty}(*)], [\text{Nat}(*)], [\text{Dedu}(*, *)], [\text{Dedu}_0(*, *)],$

[Dedu<sub>s</sub>(\* , \* , \*)], [Dedu<sub>1</sub>(\* , \* , \*)], [Dedu<sub>2</sub>(\* , \* , \*)], [Dedu<sub>3</sub>(\* , \* , \* , \*)],  
 [Dedu<sub>4</sub>(\* , \* , \* , \*)], [Dedu<sub>4</sub><sup>\*</sup>(\* , \* , \* , \*)], [Dedu<sub>5</sub>(\* , \* , \*)], [Dedu<sub>6</sub>(\* , \* , \* , \*)],  
 [Dedu<sub>6</sub><sup>\*</sup>(\* , \* , \* , \*)], [Dedu<sub>7</sub>(\* , \*)], [Dedu<sub>8</sub>(\* , \*)], [Dedu<sub>8</sub><sup>\*</sup>(\* , \*)], [EX<sub>1</sub>], [EX<sub>2</sub>], [EX<sub>3</sub>],  
 [EX<sub>10</sub>], [EX<sub>20</sub>], [\*<sub>EX</sub>], [\*<sup>EX</sup>], [(\*<sub>≡</sub> \* | \* :<sub>≡</sub> \*)<sub>EX</sub>], [(\*)<sub>≡<sup>0</sup> \* | \* :<sub>≡</sub> \*)<sub>EX</sub>],  
 [(\*)<sub>≡<sup>1</sup> \* | \* :<sub>≡</sub> \*)<sub>EX</sub>], [(\*)<sub>≡<sup>\*</sup> \* | \* :<sub>≡</sub> \*)<sub>EX</sub>], [ph<sub>1</sub>], [ph<sub>2</sub>], [ph<sub>3</sub>], [\*<sub>Ph</sub>], [\*<sup>Ph</sup>],  
 [(\*)<sub>≡ \* | \* :<sub>≡</sub> \*)<sub>Ph</sub>], [(\*)<sub>≡<sup>0</sup> \* | \* :<sub>≡</sub> \*)<sub>Ph</sub>], [(\*)<sub>≡<sup>1</sup> \* | \* :<sub>≡</sub> \*)<sub>Ph</sub>],  
 [(\*)<sub>≡<sup>\*</sup> \* | \* :<sub>≡</sub> \*)<sub>Ph</sub>], [(\*)<sub>≡ \* | \* :<sub>≡</sub> \*)<sub>Me</sub>], [(\*)<sub>≡<sup>1</sup> \* | \* :<sub>≡</sub> \*)<sub>Me</sub>],  
 [(\*)<sub>≡<sup>\*</sup> \* | \* :<sub>≡</sub> \*)<sub>Me</sub>], [bs], [OBS], [BS], [∅], [SystemQ], [MP], [Gen], [Repetition],  
 [Neg], [Ded], [ExistIntro], [Extensionality], [∅def], [PairDef], [UnionDef],  
 [PowerDef], [SeparationDef], [AddDoubleNeg], [RemoveDoubleNeg],  
 [AndCommutativity], [AutoImPLY], [Contrapositive], [FirstConjunct],  
 [SecondConjunct], [FromContradiction], [FromDisjuncts], [IffCommutativity],  
 [IffFirst], [IffSecond], [ImPLYTransitivity], [JoinConjuncts], [MP2], [MP3], [MP4],  
 [MP5], [MT], [NegativeMT], [Technicality], [Weakening], [WeakenOr1],  
 [WeakenOr2], [Formula2Pair], [Pair2Formula], [Formula2Union],  
 [Union2Formula], [Formula2Sep], [Sep2Formula], [Formula2Power],  
 [SubsetInPower], [HelperPowerIsSub], [PowerIsSub],  
 [(Switch)HelperPowerIsSub], [(Switch)PowerIsSub], [ToSetEquality],  
 [HelperToSetEquality(t)], [ToSetEquality(t)], [HelperFromSetEquality],  
 [FromSetEquality], [HelperReflexivity], [Reflexivity], [HelperSymmetry],  
 [Symmetry], [HelperTransitivity], [Transitivity], [ERisReflexive],  
 [ERisSymmetric], [ERisTransitive], [∅isSubset], [HelperMemberNot∅],  
 [MemberNot∅], [HelperUnique∅], [Unique∅], [= Reflexivity], [= Symmetry],  
 [Helper == Transitivity], [= Transitivity], [HelperTransferNotEq],  
 [TransferNotEq], [HelperPairSubset], [Helper(2)PairSubset], [PairSubset],  
 [SamePair], [SameSingleton], [UnionSubset], [SameUnion], [SeparationSubset],  
 [SameSeparation], [SameBinaryUnion], [IntersectionSubset], [SameIntersection],  
 [AutoMember], [HelperEqSysNot∅], [EqSysNot∅], [HelperEqSubset],  
 [EqSubset], [HelperEqNecessary], [EqNecessary], [HelperNoneEqNecessary],  
 [Helper(2)NoneEqNecessary], [NoneEqNecessary], [EqClassIsSubset],  
 [EqClassesAreDisjoint], [AllDisjoint], [AllDisjointImPLY], [BSsubset],  
 [Union(BS/R)subset], [UnionIdentity], [EqSysIsPartition], [(x1)], [(x2)], [(y1)],  
 [(y2)], [(v1)], [(v2)], [(v3)], [(v4)], [(v2n)], [(m1)], [(m2)], [(n1)], [(n2)], [(n3)], [(ε)],  
 [(ε)<sub>1</sub>], [(ε)<sub>2</sub>], [(fep)], [(fx)], [(fy)], [(fz)], [(fu)], [(fv)], [(fw)], [(rx)], [(ry)], [(rz)],  
 [(ru)], [(sx)], [(sx1)], [(sy)], [(sy1)], [(sz)], [(sz1)], [(su)], [(su1)], [(fxs)], [(fys)],  
 [(crs1)], [(f1)], [(f2)], [(f3)], [(f4)], [(op1)], [(op2)], [(r1)], [(s1)], [(s2)], [X<sub>1</sub>], [X<sub>2</sub>],  
 [Y<sub>1</sub>], [Y<sub>2</sub>], [V<sub>1</sub>], [V<sub>2</sub>], [V<sub>3</sub>], [V<sub>4</sub>], [V<sub>2n</sub>], [M<sub>1</sub>], [M<sub>2</sub>], [N<sub>1</sub>], [N<sub>2</sub>], [N<sub>3</sub>], [ε], [ε<sub>1</sub>], [ε<sub>2</sub>],  
 [FX], [FY], [FZ], [FU], [FV], [FW], [FEP], [RX], [RY], [RZ], [RU], [(SX)], [(SX1)],  
 [(SY)], [(SY1)], [(SZ)], [(SZ1)], [(SU)], [(SU1)], [FXS], [FYS], [(F1)], [(F2)], [(F3)],  
 [(F4)], [(OP1)], [(OP2)], [(R1)], [(S1)], [(S2)], [(EPob)], [(CRS1ob)], [(F1ob)],  
 [(F2ob)], [(F3ob)], [(F4ob)], [(N1ob)], [(N2ob)], [(OP1ob)], [(OP2ob)], [(R1ob)],  
 [(S1ob)], [(S2ob)], [ph<sub>4</sub>], [ph<sub>5</sub>], [ph<sub>6</sub>], [NAT], [RATIONAL<sub>S</sub>ERIES], [SERIES],  
 [SetOfReals], [SetOfFxs], [N], [Q], [X], [xs], [xaF], [ysF], [us], [usFoelge], [0], [1],  
 [(-1)], [2], [3], [1/2], [1/3], [2/3], [0f], [1f], [00], [01], [(- - 01)], [02], [01/02],  
 [PlusAssociativity(R)], [PlusAssociativity(R)XX], [Plus0(R)], [Negative(R)],  
 [Times1(R)], [lessAddition(R)], [PlusCommutativity(R)],</sub></sub></sub></sub></sub></sub></sub></sub></sub></sub>

[LeqAntisymmetry(R)], [LeqTransitivity(R)], [leqAddition(R)],  
 [Distribution(R)], [A4(Axiom)], [InductionAxiom], [EqualityAxiom],  
 [EqLeqAxiom], [EqAdditionAxiom], [EqMultiplicationAxiom],  
 [QisClosed(Reciprocal)(ImPLY)], [QisClosed(Reciprocal)],  
 [QisClosed(Negative)(ImPLY)], [QisClosed(Negative)], [leqReflexivity],  
 [leqAntisymmetryAxiom], [leqTransitivityAxiom], [leqTotality],  
 [leqAdditionAxiom], [leqMultiplicationAxiom], [plusAssociativity],  
 [plusCommutativity], [Negative], [plus0], [timesAssociativity],  
 [timesCommutativity], [ReciprocalAxiom], [times1], [Distribution], [0not1],  
 [lemma eqLeq(R)], [TimesAssociativity(R)], [TimesCommutativity(R)],  
 [(Adgic)SameR], [Separation2formula(1)], [Separation2formula(2)], [Cauchy],  
 [PlusF], [ReciprocalF], [From ==], [To ==], [FromInR], [PlusR(Sym)],  
 [ReciprocalR(Axiom)], [LessMinus1(N)], [Nonnegative(N)], [US0],  
 [NextXS(UpperBound)], [NextXS(NoUpperBound)], [NextUS(UpperBound)],  
 [NextUS(NoUpperBound)], [ExpZero], [ExpPositive], [ExpZero(R)],  
 [ExpPositive(R)], [BSzero], [BSpositive], [UStelescope(Zero)],  
 [UStelescope(Positive)], [EqAddition(R)], [FromLimit], [ToUpperBound],  
 [FromUpperBound], [USisUpperBound], [0not1(R)], [ExpUnbounded(R)],  
 [FromLeq(Advanced)(N)], [FromLeastUpperBound], [ToLeastUpperBound],  
 [XSisNotUpperBound], [ysFGreater], [ysFLess], [SmallInverse], [NatType],  
 [RationalType], [SeriesType], [Max], [Numerical], [NumericalF],  
 [MemberOfSeries(ImPLY)], [JoinConjuncts(2conditions)],  
 [prop lemma imply negation], [TND], [FromNegatedImPLY], [ToNegatedImPLY],  
 [FromNegated(2 \* ImPLY)], [FromNegatedAnd], [FromNegatedOr],  
 [ToNegatedOr], [FromNegations], [From3Disjuncts], [From2 \* 2Disjuncts],  
 [NegateDisjunct1], [NegateDisjunct2], [ExpandDisjuncts], [SENC1], [SENC2],  
 [LessLeq(R)], [MemberOfSeries], [memberOfSeries(Type)];

### Preassociative

[\*-{\*}], [\* /indexintro(\*, \*, \*, \*)], [\* /intro(\*, \*, \*)], [\* /bothintro(\*, \*, \*, \*, \*)],  
 [\* /nameintro(\*, \*, \*, \*)], [\*'], [\* [\* ]], [\* [\* →]], [\* [\* ⇒]], [\* 0], [\* 1], [0b], [\* -color (\*)],  
 [\* -color\* (\*)], [\*<sup>H</sup>], [\*<sup>T</sup>], [\*<sup>U</sup>], [\*<sup>h</sup>], [\*<sup>t</sup>], [\*<sup>s</sup>], [\*<sup>c</sup>], [\*<sup>d</sup>], [\*<sup>a</sup>], [\*<sup>C</sup>], [\*<sup>M</sup>], [\*<sup>B</sup>], [\*<sup>f</sup>], [\*<sup>i</sup>],  
 [\*<sup>d</sup>], [\*<sup>R</sup>], [\*<sup>0</sup>], [\*<sup>1</sup>], [\*<sup>2</sup>], [\*<sup>3</sup>], [\*<sup>4</sup>], [\*<sup>5</sup>], [\*<sup>6</sup>], [\*<sup>7</sup>], [\*<sup>8</sup>], [\*<sup>9</sup>], [\*<sup>E</sup>], [\*<sup>V</sup>], [\*<sup>C</sup>], [\*<sup>C\*</sup>],  
 [\*hide];

### Preassociative

[“ \* ”], [], [(\*)<sup>t</sup>], [string(\*) + \*], [string(\*) ++ \*], [  
 \*], [ \*], [! \*], [“ \* ”], [# \*], [\$ \*], [% \*], [& \*], [’ \*], [(\*)], [() \*], [\*\*], [+ \*], [ \*], [- \*], [ . \* ], [ / \* ],  
 [0 \*], [1 \*], [2 \*], [3 \*], [4 \*], [5 \*], [6 \*], [7 \*], [8 \*], [9 \*], [: \*], [; \*], [< \*], [= \*], [> \*], [? \*],  
 [@ \*], [A \*], [B \*], [C \*], [D \*], [E \*], [F \*], [G \*], [H \*], [I \*], [J \*], [K \*], [L \*], [M \*], [N \*],  
 [O \*], [P \*], [Q \*], [R \*], [S \*], [T \*], [U \*], [V \*], [W \*], [X \*], [Y \*], [Z \*], [[ \* ], [\ \* ], [ ] \*], [ ^ \* ],  
 [ \_ \* ], [ ‘ \* ], [ a \* ], [ b \* ], [ c \* ], [ d \* ], [ e \* ], [ f \* ], [ g \* ], [ h \* ], [ i \* ], [ j \* ], [ k \* ], [ l \* ], [ m \* ], [ n \* ], [ o \* ],  
 [ p \* ], [ q \* ], [ r \* ], [ s \* ], [ t \* ], [ u \* ], [ v \* ], [ w \* ], [ x \* ], [ y \* ], [ z \* ], [ { \* }, [ | \* }, [ } \* ], [ ~ \* ],  
 [Preassociative \*; \*], [Postassociative \*; \*], [[ \* ], \*], [priority \* end],  
 [newline \*], [macro newline \*], [MacroIndent(\*)];

### Preassociative

[\* ’ \*], [\* ‘ \*];

### Preassociative

[\*(exp)\*];

**Preassociative**

[\*], [R(\*)], [— — R(\*)], [rec\*];

**Preassociative**

[\*/\*], [\* ∩ \*], [\*[\*]];

**Preassociative**

[∪\*], [\* ∪ \*], [P(\*)];

**Preassociative**

[{\*}], [StateExpand(\*, \*, \*)], [extractSeries(\*)], [SetOfSeries(\*)], [— — Macro(\*)],  
[ExpandList(\*, \*, \*)], [\*\* Macro(\*)], [++ Macro(\*)], [ << Macro(\*)],  
[|Macro(\*)], [01//Macro(\*)], [UB(\*, \*)], [LUB(\*, \*)], [BS(\*, \*)],  
[USteleScope(\*, \*)], [(\*)], [lf \* |], [lr \* |], [Limit(\*, \*)], [Union(\*)],  
[IsOrderedPair(\*, \*, \*)], [IsRelation(\*, \*, \*)], [isFunction(\*, \*, \*)], [IsSeries(\*, \*)],  
[IsNatural(\*, \*)], [OrderedPair(\*, \*)], [TypeNat(\*)], [TypeNat0(\*)],  
[TypeRational(\*)], [TypeRational0(\*)], [TypeSeries(\*, \*)], [Typeseries0(\*, \*)];

**Preassociative**

[{\* \*}], [(<\* \*)], [(—u\*)], [—f\*], [(— — \*)], [lf/\*], [01//temp\*];

**Preassociative**

[\* (\*, \*)], [RefRel(\*, \*)], [SymRel(\*, \*)], [TransRel(\*, \*)], [EqRel(\*, \*)], [[\* ∈ \*]<sub>\*</sub>],  
[Partition(\*, \*)];

**Preassociative**

[\* · \*], [\* ·<sub>0</sub> \*], [(\*\* \*\*)], [\* \*<sub>f</sub> \*], [\*\*\* \*];

**Preassociative**

[\* + \*], [\* +<sub>0</sub> \*], [\* +<sub>1</sub> \*], [\* — \*], [\* —<sub>0</sub> \*], [\* —<sub>1</sub> \*], [(\* + \*)], [(\* — \*)], [\* +<sub>f</sub> \*],  
[\* —<sub>f</sub> \*], [\* + + \*], [R(\*) — — R(\*)];

**Preassociative**

[\* ∈ \*];

**Preassociative**

[| \* |], [if(\*, \*, \*)], [Max(\*, \*)], [Max(\*, \*)];

**Preassociative**

[\* = \*], [\* ≠ \*], [\* ≤ \*], [\* < \*], [\* <<sub>f</sub> \*], [\* ≤<sub>f</sub> \*], [SF(\*, \*)], [\* == \*],  
[\*!! == \*], [\* << \*], [\* << == \*];

**Preassociative**

[\* ∪ {\*}], [\* ∪ \*], [\* \{\*}];

**Postassociative**

[\* ·<sub>B</sub> \*], [\* ·<sub>D</sub> \*], [\* ·<sub>C</sub> \*], [\* ·<sub>P</sub> \*], [\* ·<sub>Q</sub> \*], [\* ·<sub>R</sub> \*], [\* +<sub>2</sub> \*], [\* :: \*], [\* +<sub>2</sub> \* \*];

**Postassociative**

[\* \*];

**Preassociative**

[\*  $\overset{B}{\approx}$  \*], [\*  $\overset{D}{\approx}$  \*], [\*  $\overset{C}{\approx}$  \*], [\*  $\overset{P}{\approx}$  \*], [\*  $\overset{Q}{\approx}$  \*], [\* = \*], [\*  $\overset{+}{\rightarrow}$  \*], [\*  $\overset{t}{\leftarrow}$  \*], [\*  $\overset{t^*}{\leftarrow}$  \*], [\*  $\overset{r}{\leftarrow}$  \*],  
[\* ∈<sub>t</sub> \*], [\* ⊆<sub>T</sub> \*], [\*  $\overset{T}{=}$  \*], [\*  $\overset{s}{=}$  \*], [\* free in \*], [\* free in<sup>\*</sup> \*], [\* free for \* in \*],  
[\* free for<sup>\*</sup> \* in \*], [\* ∈<sub>c</sub> \*], [\* < \*], [\* <<sub>f</sub> \*], [\* ≤<sub>f</sub> \*], [\* = \*], [\* ≠ \*], [\*<sup>var</sup>],  
[\* #<sup>0</sup> \*], [\* #<sup>1</sup> \*], [\* #<sup>\*</sup> \*], [\* == \*], [\* ⊆ \*];

**Preassociative**

[¬\*], [¬ (\* )n], [\* ∉ \*], [\* ≠ \*];

**Preassociative**

$[* \wedge *], [* \ddot{\wedge} *], [* \tilde{\wedge} *], [* \wedge_c *], [* \dot{\wedge} *];$

**Preassociative**

$[* \vee *], [* \parallel *], [* \ddot{\vee} *];$

**Postassociative**

$[* \dot{\vee} *];$

**Preassociative**

$[\exists *: *], [\forall *: *], [\forall_{\text{obj}} *: *], [\exists *: *];$

**Postassociative**

$[* \dot{\Rightarrow} *], [* \Rightarrow *], [* \Leftrightarrow *], [* \dot{\Leftrightarrow} *];$

**Preassociative**

$[\{\text{ph} \in * \mid *\}];$

**Postassociative**

$[* : *], [* \text{ spy } *], [* ! *];$

**Preassociative**

$[* \left\{ \begin{array}{c} * \\ * \end{array} \right.];$

**Preassociative**

$[\lambda *. *], [\Lambda *. *], [\Lambda *], [\text{if } * \text{ then } * \text{ else } *], [\text{let } * = * \text{ in } *], [\text{let } * \ddot{=} * \text{ in } *];$

**Preassociative**

$[* \# *];$

**Preassociative**

$[* \uparrow], [* \triangleright], [* \vee], [* \uparrow], [* \neg], [* *];$

**Preassociative**

$[* @ *], [* \triangleright *], [* \blacktriangleright *], [* \gg *], [* \triangleright *];$

**Postassociative**

$[* \vdash *], [* \dashv *], [* \text{ i.e. } *];$

**Preassociative**

$[\forall *: *], [\prod *: *];$

**Postassociative**

$[* \oplus *];$

**Postassociative**

$[* *];$

**Preassociative**

$[* \text{ proves } *];$

**Preassociative**

$[* \text{ proof of } * : *], [\text{Line } * : * \gg *; *], [\text{Last line } * \gg * \square],$   
 $[\text{Line } * : \text{Premise } \gg *; *], [\text{Line } * : \text{Side-condition } \gg *; *], [\text{Arbitrary } \gg *; *],$   
 $[\text{Local } \gg * = *; *], [\text{Begin } *; * : \text{End}; *], [\text{Last block line } * \gg *; *],$   
 $[\text{Arbitrary } \gg *; *];$

**Postassociative**

$[* \mid *];$

**Postassociative**

$[* , *], [* [* ] *];$

**Preassociative**

$[* \& *];$

## Preassociative

[\*\\\*], [\* linebreak[4] \*], [\*\\\*]; **End table**

## A Pyk definitioner

[UniqueMember  $\xrightarrow{\text{pyk}}$  “lemma uniqueMember”]  
[UniqueMember(Type)  $\xrightarrow{\text{pyk}}$  “lemma uniqueMember(Type)”]  
[SameSeries  $\xrightarrow{\text{pyk}}$  “lemma sameSeries”]  
[A4  $\xrightarrow{\text{pyk}}$  “lemma a4”]  
[SameMember  $\xrightarrow{\text{pyk}}$  “lemma sameMember”]  
[Qclosed(Addition)  $\xrightarrow{\text{pyk}}$  “1rule Qclosed(Addition)”]  
[Qclosed(Multiplication)  $\xrightarrow{\text{pyk}}$  “1rule Qclosed(Multiplication)”]  
[FromCartProd(1)  $\xrightarrow{\text{pyk}}$  “1rule fromCartProd(1)”]  
[1rule fromCartProd(2)  $\xrightarrow{\text{pyk}}$  “1rule fromCartProd(2)”]  
[constantRationalSeries(\*)  $\xrightarrow{\text{pyk}}$  “constantRationalSeries( ” )”]  
[cartProd(\*)  $\xrightarrow{\text{pyk}}$  “cartProd( ” , ” )”]  
[Power(\*)  $\xrightarrow{\text{pyk}}$  “P( ” )”]  
[binaryUnion(\*, \*)  $\xrightarrow{\text{pyk}}$  “binaryUnion( ” , ” )”]  
[SetOfRationalSeries  $\xrightarrow{\text{pyk}}$  “setOfRationalSeries”]  
[IsSubset(\*, \*)  $\xrightarrow{\text{pyk}}$  “isSubset( ” , ” )”]  
[(p\*, \*)  $\xrightarrow{\text{pyk}}$  “(p ” , ” )”]  
[(s\*)  $\xrightarrow{\text{pyk}}$  “(s ” )”]  
[(...)  $\xrightarrow{\text{pyk}}$  “cdots”]  
[Objekt-var  $\xrightarrow{\text{pyk}}$  “object-var”]  
[Ex-var  $\xrightarrow{\text{pyk}}$  “ex-var”]  
[Ph-var  $\xrightarrow{\text{pyk}}$  “ph-var”]  
[Værdi  $\xrightarrow{\text{pyk}}$  “vaerdi”]  
[Variabel  $\xrightarrow{\text{pyk}}$  “variabel”]  
[Op(\*)  $\xrightarrow{\text{pyk}}$  “op ” end op”]  
[Op(\*, \*)  $\xrightarrow{\text{pyk}}$  “op2 ” comma ” end op2”]  
[\* ::= \*  $\xrightarrow{\text{pyk}}$  “define-equal ” comma ” end equal”]  
[ContainsEmpty(\*)  $\xrightarrow{\text{pyk}}$  “contains-empty ” end empty”]  
[Nat(\*)  $\xrightarrow{\text{pyk}}$  “Nat( ” )”]  
[Dedu(\*, \*)  $\xrightarrow{\text{pyk}}$  “1deduction ” conclude ” end 1deduction”]  
[Dedu<sub>0</sub>(\*, \*)  $\xrightarrow{\text{pyk}}$  “1deduction zero ” conclude ” end 1deduction”]  
[Dedu<sub>s</sub>(\*, \*, \*)  $\xrightarrow{\text{pyk}}$  “1deduction side ” conclude ” condition ” end 1deduction”]



$[\text{Dedu}_1(*, *, *) \xrightarrow{\text{pyk}} \text{"1deduction one " conclude " condition " end 1deduction"}]$   
 $[\text{Dedu}_2(*, *, *) \xrightarrow{\text{pyk}} \text{"1deduction two " conclude " condition " end 1deduction"}]$   
 $[\text{Dedu}_3(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction three " conclude " condition " bound " end 1deduction"}]$   
 $[\text{Dedu}_4(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction four " conclude " condition " bound " end 1deduction"}]$   
 $[\text{Dedu}_4^*(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction four star " conclude " condition " bound " end 1deduction"}]$   
 $[\text{Dedu}_5(*, *, *) \xrightarrow{\text{pyk}} \text{"1deduction five " condition " bound " end 1deduction"}]$   
 $[\text{Dedu}_6(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction six " conclude " exception " bound " end 1deduction"}]$   
 $[\text{Dedu}_6^*(*, *, *, *) \xrightarrow{\text{pyk}} \text{"1deduction six star " conclude " exception " bound " end 1deduction"}]$   
 $[\text{Dedu}_7(*) \xrightarrow{\text{pyk}} \text{"1deduction seven " end 1deduction"}]$   
 $[\text{Dedu}_8(*, *) \xrightarrow{\text{pyk}} \text{"1deduction eight " bound " end 1deduction"}]$   
 $[\text{Dedu}_8^*(*, *) \xrightarrow{\text{pyk}} \text{"1deduction eight star " bound " end 1deduction"}]$   
 $[\text{Ex}_1 \xrightarrow{\text{pyk}} \text{"ex1"}]$   
 $[\text{Ex}_2 \xrightarrow{\text{pyk}} \text{"ex2"}]$   
 $[\text{Ex}_3 \xrightarrow{\text{pyk}} \text{"ex3"}]$   
 $[\text{Ex}_{10} \xrightarrow{\text{pyk}} \text{"ex10"}]$   
 $[\text{Ex}_{20} \xrightarrow{\text{pyk}} \text{"ex20"}]$   
 $[\text{*Ex} \xrightarrow{\text{pyk}} \text{"existential var " end var"}]$   
 $[\text{*Ex} \xrightarrow{\text{pyk}} \text{" " is existential var"}]$   
 $[\langle * \equiv * \mid * := * \rangle_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"exist-sub " is " where " is " end sub"}]$   
 $[\langle * \equiv^0 * \mid * := * \rangle_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"exist-sub0 " is " where " is " end sub"}]$   
 $[\langle * \equiv^1 * \mid * := * \rangle_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"exist-sub1 " is " where " is " end sub"}]$   
 $[\langle * \equiv * * \mid * := * \rangle_{\text{Ex}} \xrightarrow{\text{pyk}} \text{"exist-sub* " is " where " is " end sub"}]$   
 $[\text{ph}_1 \xrightarrow{\text{pyk}} \text{"ph1"}]$   
 $[\text{ph}_2 \xrightarrow{\text{pyk}} \text{"ph2"}]$   
 $[\text{ph}_3 \xrightarrow{\text{pyk}} \text{"ph3"}]$   
 $[\text{*Ph} \xrightarrow{\text{pyk}} \text{"placeholder-var " end var"}]$   
 $[\text{*Ph} \xrightarrow{\text{pyk}} \text{" " is placeholder-var"}]$   
 $[\langle * \equiv * \mid * := * \rangle_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"ph-sub " is " where " is " end sub"}]$   
 $[\langle * \equiv^0 * \mid * := * \rangle_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"ph-sub0 " is " where " is " end sub"}]$   
 $[\langle * \equiv^1 * \mid * := * \rangle_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"ph-sub1 " is " where " is " end sub"}]$   
 $[\langle * \equiv * * \mid * := * \rangle_{\text{Ph}} \xrightarrow{\text{pyk}} \text{"ph-sub* " is " where " is " end sub"}]$

$[(\equiv * | * := *)_{\text{Me}} \xrightarrow{\text{pyk}} \text{“meta-sub ” is ” where ” is ” end sub”}]$   
 $[(\equiv^1 * | * := *)_{\text{Me}} \xrightarrow{\text{pyk}} \text{“meta-sub1 ” is ” where ” is ” end sub”}]$   
 $[(\equiv * * | * := *)_{\text{Me}} \xrightarrow{\text{pyk}} \text{“meta-sub* ” is ” where ” is ” end sub”}]$   
 $[\text{bs} \xrightarrow{\text{pyk}} \text{“var big set”}]$   
 $[\text{OBS} \xrightarrow{\text{pyk}} \text{“object big set”}]$   
 $[\mathcal{BS} \xrightarrow{\text{pyk}} \text{“meta big set”}]$   
 $[\emptyset \xrightarrow{\text{pyk}} \text{“zermelo empty set”}]$   
 $[\text{SystemQ} \xrightarrow{\text{pyk}} \text{“system Q”}]$   
 $[\text{MP} \xrightarrow{\text{pyk}} \text{“1rule mp”}]$   
 $[\text{Gen} \xrightarrow{\text{pyk}} \text{“1rule gen”}]$   
 $[\text{Repetition} \xrightarrow{\text{pyk}} \text{“1rule repetition”}]$   
 $[\text{Neg} \xrightarrow{\text{pyk}} \text{“1rule ad absurdum”}]$   
 $[\text{Ded} \xrightarrow{\text{pyk}} \text{“1rule deduction”}]$   
 $[\text{ExistIntro} \xrightarrow{\text{pyk}} \text{“1rule exist intro”}]$   
 $[\text{Extensionality} \xrightarrow{\text{pyk}} \text{“axiom extensionality”}]$   
 $[\emptyset\text{def} \xrightarrow{\text{pyk}} \text{“axiom empty set”}]$   
 $[\text{PairDef} \xrightarrow{\text{pyk}} \text{“axiom pair definition”}]$   
 $[\text{UnionDef} \xrightarrow{\text{pyk}} \text{“axiom union definition”}]$   
 $[\text{PowerDef} \xrightarrow{\text{pyk}} \text{“axiom power definition”}]$   
 $[\text{SeparationDef} \xrightarrow{\text{pyk}} \text{“axiom separation definition”}]$   
 $[\text{AddDoubleNeg} \xrightarrow{\text{pyk}} \text{“prop lemma add double neg”}]$   
 $[\text{RemoveDoubleNeg} \xrightarrow{\text{pyk}} \text{“prop lemma remove double neg”}]$   
 $[\text{AndCommutativity} \xrightarrow{\text{pyk}} \text{“prop lemma and commutativity”}]$   
 $[\text{AutoImply} \xrightarrow{\text{pyk}} \text{“prop lemma auto imply”}]$   
 $[\text{Contrapositive} \xrightarrow{\text{pyk}} \text{“prop lemma contrapositive”}]$   
 $[\text{FirstConjunct} \xrightarrow{\text{pyk}} \text{“prop lemma first conjunct”}]$   
 $[\text{SecondConjunct} \xrightarrow{\text{pyk}} \text{“prop lemma second conjunct”}]$   
 $[\text{FromContradiction} \xrightarrow{\text{pyk}} \text{“prop lemma from contradiction”}]$   
 $[\text{FromDisjuncts} \xrightarrow{\text{pyk}} \text{“prop lemma from disjuncts”}]$   
 $[\text{IffCommutativity} \xrightarrow{\text{pyk}} \text{“prop lemma iff commutativity”}]$   
 $[\text{IffFirst} \xrightarrow{\text{pyk}} \text{“prop lemma iff first”}]$   
 $[\text{IffSecond} \xrightarrow{\text{pyk}} \text{“prop lemma iff second”}]$   
 $[\text{ImplyTransitivity} \xrightarrow{\text{pyk}} \text{“prop lemma imply transitivity”}]$   
 $[\text{JoinConjuncts} \xrightarrow{\text{pyk}} \text{“prop lemma join conjuncts”}]$   
 $[\text{MP2} \xrightarrow{\text{pyk}} \text{“prop lemma mp2”}]$

[MP3  $\xrightarrow{\text{pyk}}$  “prop lemma mp3”]  
 [MP4  $\xrightarrow{\text{pyk}}$  “prop lemma mp4”]  
 [MP5  $\xrightarrow{\text{pyk}}$  “prop lemma mp5”]  
 [MT  $\xrightarrow{\text{pyk}}$  “prop lemma mt”]  
 [NegativeMT  $\xrightarrow{\text{pyk}}$  “prop lemma negative mt”]  
 [Technicality  $\xrightarrow{\text{pyk}}$  “prop lemma technicality”]  
 [Weakening  $\xrightarrow{\text{pyk}}$  “prop lemma weakening”]  
 [WeakenOr1  $\xrightarrow{\text{pyk}}$  “prop lemma weaken or first”]  
 [WeakenOr2  $\xrightarrow{\text{pyk}}$  “prop lemma weaken or second”]  
 [Formula2Pair  $\xrightarrow{\text{pyk}}$  “lemma formula2pair”]  
 [Pair2Formula  $\xrightarrow{\text{pyk}}$  “lemma pair2formula”]  
 [Formula2Union  $\xrightarrow{\text{pyk}}$  “lemma formula2union”]  
 [Union2Formula  $\xrightarrow{\text{pyk}}$  “lemma union2formula”]  
 [Formula2Sep  $\xrightarrow{\text{pyk}}$  “lemma formula2separation”]  
 [Sep2Formula  $\xrightarrow{\text{pyk}}$  “lemma separation2formula”]  
 [Formula2Power  $\xrightarrow{\text{pyk}}$  “lemma formula2power”]  
 [SubsetInPower  $\xrightarrow{\text{pyk}}$  “lemma subset in power set”]  
 [HelperPowerIsSub  $\xrightarrow{\text{pyk}}$  “lemma power set is subset0”]  
 [PowerIsSub  $\xrightarrow{\text{pyk}}$  “lemma power set is subset”]  
 [(Switch)HelperPowerIsSub  $\xrightarrow{\text{pyk}}$  “lemma power set is subset0-switch”]  
 [(Switch)PowerIsSub  $\xrightarrow{\text{pyk}}$  “lemma power set is subset-switch”]  
 [ToSetEquality  $\xrightarrow{\text{pyk}}$  “lemma set equality suff condition”]  
 [HelperToSetEquality(t)  $\xrightarrow{\text{pyk}}$  “lemma set equality suff condition(t)0”]  
 [ToSetEquality(t)  $\xrightarrow{\text{pyk}}$  “lemma set equality suff condition(t)”]  
 [HelperFromSetEquality  $\xrightarrow{\text{pyk}}$  “lemma set equality skip quantifier”]  
 [FromSetEquality  $\xrightarrow{\text{pyk}}$  “lemma set equality nec condition”]  
 [HelperReflexivity  $\xrightarrow{\text{pyk}}$  “lemma reflexivity0”]  
 [Reflexivity  $\xrightarrow{\text{pyk}}$  “lemma reflexivity”]  
 [HelperSymmetry  $\xrightarrow{\text{pyk}}$  “lemma symmetry0”]  
 [Symmetry  $\xrightarrow{\text{pyk}}$  “lemma symmetry”]  
 [HelperTransitivity  $\xrightarrow{\text{pyk}}$  “lemma transitivity0”]  
 [Transitivity  $\xrightarrow{\text{pyk}}$  “lemma transitivity”]  
 [ERisReflexive  $\xrightarrow{\text{pyk}}$  “lemma er is reflexive”]  
 [ERisSymmetric  $\xrightarrow{\text{pyk}}$  “lemma er is symmetric”]  
 [ERisTransitive  $\xrightarrow{\text{pyk}}$  “lemma er is transitive”]

$[\text{ØisSubset} \xrightarrow{\text{pyk}} \text{“lemma empty set is subset”}]$   
 $[\text{HelperMemberNotØ} \xrightarrow{\text{pyk}} \text{“lemma member not empty0”}]$   
 $[\text{MemberNotØ} \xrightarrow{\text{pyk}} \text{“lemma member not empty”}]$   
 $[\text{HelperUniqueØ} \xrightarrow{\text{pyk}} \text{“lemma unique empty set0”}]$   
 $[\text{UniqueØ} \xrightarrow{\text{pyk}} \text{“lemma unique empty set”}]$   
 $[\text{== Reflexivity} \xrightarrow{\text{pyk}} \text{“lemma ==Reflexivity”}]$   
 $[\text{== Symmetry} \xrightarrow{\text{pyk}} \text{“lemma ==Symmetry”}]$   
 $[\text{Helper==Transitivity} \xrightarrow{\text{pyk}} \text{“lemma ==Transitivity0”}]$   
 $[\text{== Transitivity} \xrightarrow{\text{pyk}} \text{“lemma ==Transitivity”}]$   
 $[\text{HelperTransferNotEq} \xrightarrow{\text{pyk}} \text{“lemma transfer ~is0”}]$   
 $[\text{TransferNotEq} \xrightarrow{\text{pyk}} \text{“lemma transfer ~is”}]$   
 $[\text{HelperPairSubset} \xrightarrow{\text{pyk}} \text{“lemma pair subset0”}]$   
 $[\text{Helper(2)PairSubset} \xrightarrow{\text{pyk}} \text{“lemma pair subset1”}]$   
 $[\text{PairSubset} \xrightarrow{\text{pyk}} \text{“lemma pair subset”}]$   
 $[\text{SamePair} \xrightarrow{\text{pyk}} \text{“lemma same pair”}]$   
 $[\text{SameSingleton} \xrightarrow{\text{pyk}} \text{“lemma same singleton”}]$   
 $[\text{UnionSubset} \xrightarrow{\text{pyk}} \text{“lemma union subset”}]$   
 $[\text{SameUnion} \xrightarrow{\text{pyk}} \text{“lemma same union”}]$   
 $[\text{SeparationSubset} \xrightarrow{\text{pyk}} \text{“lemma separation subset”}]$   
 $[\text{SameSeparation} \xrightarrow{\text{pyk}} \text{“lemma same separation”}]$   
 $[\text{SameBinaryUnion} \xrightarrow{\text{pyk}} \text{“lemma same binary union”}]$   
 $[\text{IntersectionSubset} \xrightarrow{\text{pyk}} \text{“lemma intersection subset”}]$   
 $[\text{SameIntersection} \xrightarrow{\text{pyk}} \text{“lemma same intersection”}]$   
 $[\text{AutoMember} \xrightarrow{\text{pyk}} \text{“lemma auto member”}]$   
 $[\text{HelperEqSysNotØ} \xrightarrow{\text{pyk}} \text{“lemma eq-system not empty0”}]$   
 $[\text{EqSysNotØ} \xrightarrow{\text{pyk}} \text{“lemma eq-system not empty”}]$   
 $[\text{HelperEqSubset} \xrightarrow{\text{pyk}} \text{“lemma eq subset0”}]$   
 $[\text{EqSubset} \xrightarrow{\text{pyk}} \text{“lemma eq subset”}]$   
 $[\text{HelperEqNecessary} \xrightarrow{\text{pyk}} \text{“lemma equivalence nec condition0”}]$   
 $[\text{EqNecessary} \xrightarrow{\text{pyk}} \text{“lemma equivalence nec condition”}]$   
 $[\text{HelperNoneEqNecessary} \xrightarrow{\text{pyk}} \text{“lemma none-equivalence nec condition0”}]$   
 $[\text{Helper(2)NoneEqNecessary} \xrightarrow{\text{pyk}} \text{“lemma none-equivalence nec condition1”}]$   
 $[\text{NoneEqNecessary} \xrightarrow{\text{pyk}} \text{“lemma none-equivalence nec condition”}]$   
 $[\text{EqClassIsSubset} \xrightarrow{\text{pyk}} \text{“lemma equivalence class is subset”}]$   
 $[\text{EqClassesAreDisjoint} \xrightarrow{\text{pyk}} \text{“lemma equivalence classes are disjoint”}]$

$[\text{AllDisjoint} \xrightarrow{\text{pyk}} \text{“lemma all disjoint”}]$   
 $[\text{AllDisjointImPLY} \xrightarrow{\text{pyk}} \text{“lemma all disjoint-imply”}]$   
 $[\text{BSsubset} \xrightarrow{\text{pyk}} \text{“lemma bs subset union(bs/r)”}]$   
 $[\text{Union(BS/R)subset} \xrightarrow{\text{pyk}} \text{“lemma union(bs/r) subset bs”}]$   
 $[\text{UnionIdentity} \xrightarrow{\text{pyk}} \text{“lemma union(bs/r) is bs”}]$   
 $[\text{EqSysIsPartition} \xrightarrow{\text{pyk}} \text{“theorem eq-system is partition”}]$   
 $[(x1) \xrightarrow{\text{pyk}} \text{“var x1”}]$   
 $[(x2) \xrightarrow{\text{pyk}} \text{“var x2”}]$   
 $[(y1) \xrightarrow{\text{pyk}} \text{“var y1”}]$   
 $[(y2) \xrightarrow{\text{pyk}} \text{“var y2”}]$   
 $[(v1) \xrightarrow{\text{pyk}} \text{“var v1”}]$   
 $[(v2) \xrightarrow{\text{pyk}} \text{“var v2”}]$   
 $[(v3) \xrightarrow{\text{pyk}} \text{“var v3”}]$   
 $[(v4) \xrightarrow{\text{pyk}} \text{“var v4”}]$   
 $[(v2n) \xrightarrow{\text{pyk}} \text{“var v2n”}]$   
 $[(m1) \xrightarrow{\text{pyk}} \text{“var m1”}]$   
 $[(m2) \xrightarrow{\text{pyk}} \text{“var m2”}]$   
 $[(n1) \xrightarrow{\text{pyk}} \text{“var n1”}]$   
 $[(n2) \xrightarrow{\text{pyk}} \text{“var n2”}]$   
 $[(n3) \xrightarrow{\text{pyk}} \text{“var n3”}]$   
 $[(\epsilon) \xrightarrow{\text{pyk}} \text{“var ep”}]$   
 $[(\epsilon)_1 \xrightarrow{\text{pyk}} \text{“var ep1”}]$   
 $[(\epsilon)_2 \xrightarrow{\text{pyk}} \text{“var ep2”}]$   
 $[(fep) \xrightarrow{\text{pyk}} \text{“var fep”}]$   
 $[(fx) \xrightarrow{\text{pyk}} \text{“var fx”}]$   
 $[(fy) \xrightarrow{\text{pyk}} \text{“var fy”}]$   
 $[(fz) \xrightarrow{\text{pyk}} \text{“var fz”}]$   
 $[(fu) \xrightarrow{\text{pyk}} \text{“var fu”}]$   
 $[(fv) \xrightarrow{\text{pyk}} \text{“var fv”}]$   
 $[(fw) \xrightarrow{\text{pyk}} \text{“var fw”}]$   
 $[(rx) \xrightarrow{\text{pyk}} \text{“var rx”}]$   
 $[(ry) \xrightarrow{\text{pyk}} \text{“var ry”}]$   
 $[(rz) \xrightarrow{\text{pyk}} \text{“var rz”}]$   
 $[(ru) \xrightarrow{\text{pyk}} \text{“var ru”}]$   
 $[(sx) \xrightarrow{\text{pyk}} \text{“var sx”}]$

$[(sx1) \xrightarrow{\text{pyk}} \text{“var sx1”}]$   
 $[(sy) \xrightarrow{\text{pyk}} \text{“var sy”}]$   
 $[(sy1) \xrightarrow{\text{pyk}} \text{“var sy1”}]$   
 $[(sz) \xrightarrow{\text{pyk}} \text{“var sz”}]$   
 $[(sz1) \xrightarrow{\text{pyk}} \text{“var sz1”}]$   
 $[(su) \xrightarrow{\text{pyk}} \text{“var su”}]$   
 $[(su1) \xrightarrow{\text{pyk}} \text{“var su1”}]$   
 $[(fxs) \xrightarrow{\text{pyk}} \text{“var fxs”}]$   
 $[(fys) \xrightarrow{\text{pyk}} \text{“var fys”}]$   
 $[(crs1) \xrightarrow{\text{pyk}} \text{“var crs1”}]$   
 $[(f1) \xrightarrow{\text{pyk}} \text{“var f1”}]$   
 $[(f2) \xrightarrow{\text{pyk}} \text{“var f2”}]$   
 $[(f3) \xrightarrow{\text{pyk}} \text{“var f3”}]$   
 $[(f4) \xrightarrow{\text{pyk}} \text{“var f4”}]$   
 $[(op1) \xrightarrow{\text{pyk}} \text{“var op1”}]$   
 $[(op2) \xrightarrow{\text{pyk}} \text{“var op2”}]$   
 $[(r1) \xrightarrow{\text{pyk}} \text{“var r1”}]$   
 $[(s1) \xrightarrow{\text{pyk}} \text{“var s1”}]$   
 $[(s2) \xrightarrow{\text{pyk}} \text{“var s2”}]$   
 $[X_1 \xrightarrow{\text{pyk}} \text{“meta x1”}]$   
 $[X_2 \xrightarrow{\text{pyk}} \text{“meta x2”}]$   
 $[Y_1 \xrightarrow{\text{pyk}} \text{“meta y1”}]$   
 $[Y_2 \xrightarrow{\text{pyk}} \text{“meta y2”}]$   
 $[V_1 \xrightarrow{\text{pyk}} \text{“meta v1”}]$   
 $[V_2 \xrightarrow{\text{pyk}} \text{“meta v2”}]$   
 $[V_3 \xrightarrow{\text{pyk}} \text{“meta v3”}]$   
 $[V_4 \xrightarrow{\text{pyk}} \text{“meta v4”}]$   
 $[V_{2n} \xrightarrow{\text{pyk}} \text{“meta v2n”}]$   
 $[M_1 \xrightarrow{\text{pyk}} \text{“meta m1”}]$   
 $[M_2 \xrightarrow{\text{pyk}} \text{“meta m2”}]$   
 $[N_1 \xrightarrow{\text{pyk}} \text{“meta n1”}]$   
 $[N_2 \xrightarrow{\text{pyk}} \text{“meta n2”}]$   
 $[N_3 \xrightarrow{\text{pyk}} \text{“meta n3”}]$   
 $[\epsilon \xrightarrow{\text{pyk}} \text{“meta ep”}]$   
 $[\epsilon 1 \xrightarrow{\text{pyk}} \text{“meta ep1”}]$

$[\epsilon 2 \xrightarrow{\text{pyk}} \text{“meta ep2”}]$   
 $[\text{FX} \xrightarrow{\text{pyk}} \text{“meta fx”}]$   
 $[\text{FY} \xrightarrow{\text{pyk}} \text{“meta fy”}]$   
 $[\text{FZ} \xrightarrow{\text{pyk}} \text{“meta fz”}]$   
 $[\text{FU} \xrightarrow{\text{pyk}} \text{“meta fu”}]$   
 $[\text{FV} \xrightarrow{\text{pyk}} \text{“meta fv”}]$   
 $[\text{FW} \xrightarrow{\text{pyk}} \text{“meta fw”}]$   
 $[\text{FEP} \xrightarrow{\text{pyk}} \text{“meta fep”}]$   
 $[\text{RX} \xrightarrow{\text{pyk}} \text{“meta rx”}]$   
 $[\text{RY} \xrightarrow{\text{pyk}} \text{“meta ry”}]$   
 $[\text{RZ} \xrightarrow{\text{pyk}} \text{“meta rz”}]$   
 $[\text{RU} \xrightarrow{\text{pyk}} \text{“meta ru”}]$   
 $[(\text{SX}) \xrightarrow{\text{pyk}} \text{“meta sx”}]$   
 $[(\text{SX1}) \xrightarrow{\text{pyk}} \text{“meta sx1”}]$   
 $[(\text{SY}) \xrightarrow{\text{pyk}} \text{“meta sy”}]$   
 $[(\text{SY1}) \xrightarrow{\text{pyk}} \text{“meta sy1”}]$   
 $[(\text{SZ}) \xrightarrow{\text{pyk}} \text{“meta sz”}]$   
 $[(\text{SZ1}) \xrightarrow{\text{pyk}} \text{“meta sz1”}]$   
 $[(\text{SU}) \xrightarrow{\text{pyk}} \text{“meta su”}]$   
 $[(\text{SU1}) \xrightarrow{\text{pyk}} \text{“meta su1”}]$   
 $[\text{FXS} \xrightarrow{\text{pyk}} \text{“meta fxs”}]$   
 $[\text{FYS} \xrightarrow{\text{pyk}} \text{“meta fys”}]$   
 $[(\text{F1}) \xrightarrow{\text{pyk}} \text{“meta f1”}]$   
 $[(\text{F2}) \xrightarrow{\text{pyk}} \text{“meta f2”}]$   
 $[(\text{F3}) \xrightarrow{\text{pyk}} \text{“meta f3”}]$   
 $[(\text{F4}) \xrightarrow{\text{pyk}} \text{“meta f4”}]$   
 $[(\text{OP1}) \xrightarrow{\text{pyk}} \text{“meta op1”}]$   
 $[(\text{OP2}) \xrightarrow{\text{pyk}} \text{“meta op2”}]$   
 $[(\text{R1}) \xrightarrow{\text{pyk}} \text{“meta r1”}]$   
 $[(\text{S1}) \xrightarrow{\text{pyk}} \text{“meta s1”}]$   
 $[(\text{S2}) \xrightarrow{\text{pyk}} \text{“meta s2”}]$   
 $[(\text{EPob}) \xrightarrow{\text{pyk}} \text{“object ep”}]$   
 $[(\text{CRS1ob}) \xrightarrow{\text{pyk}} \text{“object crs1”}]$   
 $[(\text{F1ob}) \xrightarrow{\text{pyk}} \text{“object f1”}]$   
 $[(\text{F2ob}) \xrightarrow{\text{pyk}} \text{“object f2”}]$

[(F3ob)  $\xrightarrow{\text{pyk}}$  “object f3”]  
 [(F4ob)  $\xrightarrow{\text{pyk}}$  “object f4”]  
 [(N1ob)  $\xrightarrow{\text{pyk}}$  “object n1”]  
 [(N2ob)  $\xrightarrow{\text{pyk}}$  “object n2”]  
 [(OP1ob)  $\xrightarrow{\text{pyk}}$  “object op1”]  
 [(OP2ob)  $\xrightarrow{\text{pyk}}$  “object op2”]  
 [(R1ob)  $\xrightarrow{\text{pyk}}$  “object r1”]  
 [(S1ob)  $\xrightarrow{\text{pyk}}$  “object s1”]  
 [(S2ob)  $\xrightarrow{\text{pyk}}$  “object s2”]  
 [ph<sub>4</sub>  $\xrightarrow{\text{pyk}}$  “ph4”]  
 [ph<sub>5</sub>  $\xrightarrow{\text{pyk}}$  “ph5”]  
 [ph<sub>6</sub>  $\xrightarrow{\text{pyk}}$  “ph6”]  
 [NAT  $\xrightarrow{\text{pyk}}$  “NAT”]  
 [RATIONAL<sub>S</sub>SERIES  $\xrightarrow{\text{pyk}}$  “RATIONAL\_SERIES”]  
 [SERIES  $\xrightarrow{\text{pyk}}$  “SERIES”]  
 [SetOfReals  $\xrightarrow{\text{pyk}}$  “setOfReals”]  
 [SetOfFxs  $\xrightarrow{\text{pyk}}$  “setOfFxs”]  
 [N  $\xrightarrow{\text{pyk}}$  “N”]  
 [Q  $\xrightarrow{\text{pyk}}$  “Q”]  
 [X  $\xrightarrow{\text{pyk}}$  “X”]  
 [xs  $\xrightarrow{\text{pyk}}$  “xs”]  
 [xaF  $\xrightarrow{\text{pyk}}$  “xsF”]  
 [ysF  $\xrightarrow{\text{pyk}}$  “ysF”]  
 [us  $\xrightarrow{\text{pyk}}$  “us”]  
 [usFoelge  $\xrightarrow{\text{pyk}}$  “usF”]  
 [0  $\xrightarrow{\text{pyk}}$  “0”]  
 [1  $\xrightarrow{\text{pyk}}$  “1”]  
 [(-1)  $\xrightarrow{\text{pyk}}$  “(-1)”]  
 [2  $\xrightarrow{\text{pyk}}$  “2”]  
 [3  $\xrightarrow{\text{pyk}}$  “3”]  
 [1/2  $\xrightarrow{\text{pyk}}$  “1/2”]  
 [1/3  $\xrightarrow{\text{pyk}}$  “1/3”]  
 [2/3  $\xrightarrow{\text{pyk}}$  “2/3”]  
 [0f  $\xrightarrow{\text{pyk}}$  “0f”]  
 [1f  $\xrightarrow{\text{pyk}}$  “1f”]



$[00 \xrightarrow{\text{pyk}} \text{"00"}]$   
 $[01 \xrightarrow{\text{pyk}} \text{"01"}]$   
 $[(- - 01) \xrightarrow{\text{pyk}} \text{"(-01)"}]$   
 $[02 \xrightarrow{\text{pyk}} \text{"02"}]$   
 $[01//02 \xrightarrow{\text{pyk}} \text{"01//02"}]$   
 $[\text{PlusAssociativity}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma plusAssociativity}(\text{R})"]$   
 $[\text{PlusAssociativity}(\text{R})\text{XX} \xrightarrow{\text{pyk}} \text{"lemma plusAssociativity}(\text{R})\text{XX}"]$   
 $[\text{Plus0}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma plus0}(\text{R})"]$   
 $[\text{Negative}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma negative}(\text{R})"]$   
 $[\text{Times1}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma times1}(\text{R})"]$   
 $[\text{lessAddition}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma lessAddition}(\text{R})"]$   
 $[\text{PlusCommutativity}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma plusCommutativity}(\text{R})"]$   
 $[\text{LeqAntisymmetry}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma leqAntisymmetry}(\text{R})"]$   
 $[\text{LeqTransitivity}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma leqTransitivity}(\text{R})"]$   
 $[\text{leqAddition}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma leqAddition}(\text{R})"]$   
 $[\text{Distribution}(\text{R}) \xrightarrow{\text{pyk}} \text{"lemma distribution}(\text{R})"]$   
 $[\text{A4}(\text{Axiom}) \xrightarrow{\text{pyk}} \text{"axiom a4"}]$   
 $[\text{InductionAxiom} \xrightarrow{\text{pyk}} \text{"axiom induction"}]$   
 $[\text{EqualityAxiom} \xrightarrow{\text{pyk}} \text{"axiom equality"}]$   
 $[\text{EqLeqAxiom} \xrightarrow{\text{pyk}} \text{"axiom eqLeq"}]$   
 $[\text{EqAdditionAxiom} \xrightarrow{\text{pyk}} \text{"axiom eqAddition"}]$   
 $[\text{EqMultiplicationAxiom} \xrightarrow{\text{pyk}} \text{"axiom eqMultiplication"}]$   
 $[\text{QisClosed}(\text{Reciprocal})(\text{Imply}) \xrightarrow{\text{pyk}} \text{"axiom QisClosed}(\text{reciprocal})"]$   
 $[\text{QisClosed}(\text{Reciprocal}) \xrightarrow{\text{pyk}} \text{"lemma QisClosed}(\text{reciprocal})"]$   
 $[\text{QisClosed}(\text{Negative})(\text{Imply}) \xrightarrow{\text{pyk}} \text{"axiom QisClosed}(\text{negative})"]$   
 $[\text{QisClosed}(\text{Negative}) \xrightarrow{\text{pyk}} \text{"lemma QisClosed}(\text{negative})"]$   
 $[\text{leqReflexivity} \xrightarrow{\text{pyk}} \text{"axiom leqReflexivity"}]$   
 $[\text{leqAntisymmetryAxiom} \xrightarrow{\text{pyk}} \text{"axiom leqAntisymmetry"}]$   
 $[\text{leqTransitivityAxiom} \xrightarrow{\text{pyk}} \text{"axiom leqTransitivity"}]$   
 $[\text{leqTotality} \xrightarrow{\text{pyk}} \text{"axiom leqTotality"}]$   
 $[\text{leqAdditionAxiom} \xrightarrow{\text{pyk}} \text{"axiom leqAddition"}]$   
 $[\text{leqMultiplicationAxiom} \xrightarrow{\text{pyk}} \text{"axiom leqMultiplication"}]$   
 $[\text{plusAssociativity} \xrightarrow{\text{pyk}} \text{"axiom plusAssociativity"}]$   
 $[\text{plusCommutativity} \xrightarrow{\text{pyk}} \text{"axiom plusCommutativity"}]$   
 $[\text{Negative} \xrightarrow{\text{pyk}} \text{"axiom negative"}]$

[plus0  $\xrightarrow{\text{pyk}}$  “axiom plus0”]  
 [timesAssociativity  $\xrightarrow{\text{pyk}}$  “axiom timesAssociativity”]  
 [timesCommutativity  $\xrightarrow{\text{pyk}}$  “axiom timesCommutativity”]  
 [ReciprocalAxiom  $\xrightarrow{\text{pyk}}$  “axiom reciprocal”]  
 [times1  $\xrightarrow{\text{pyk}}$  “axiom times1”]  
 [Distribution  $\xrightarrow{\text{pyk}}$  “axiom distribution”]  
 [0not1  $\xrightarrow{\text{pyk}}$  “axiom 0not1”]  
 [lemma eqLeq(R)  $\xrightarrow{\text{pyk}}$  “lemma eqLeq(R)”]  
 [TimesAssociativity(R)  $\xrightarrow{\text{pyk}}$  “lemma timesAssociativity(R)”]  
 [TimesCommutativity(R)  $\xrightarrow{\text{pyk}}$  “lemma timesCommutativity(R)”]  
 [(Adgic)SameR  $\xrightarrow{\text{pyk}}$  “1rule adhoc sameR”]  
 [Separation2formula(1)  $\xrightarrow{\text{pyk}}$  “lemma separation2formula(1)”]  
 [Separation2formula(2)  $\xrightarrow{\text{pyk}}$  “lemma separation2formula(2)”]  
 [Cauchy  $\xrightarrow{\text{pyk}}$  “axiom cauchy”]  
 [PlusF  $\xrightarrow{\text{pyk}}$  “axiom plusF”]  
 [ReciprocalF  $\xrightarrow{\text{pyk}}$  “axiom reciprocalF”]  
 [From ==  $\xrightarrow{\text{pyk}}$  “1rule from==”]  
 [To ==  $\xrightarrow{\text{pyk}}$  “1rule to==”]  
 [FromInR  $\xrightarrow{\text{pyk}}$  “1rule fromInR”]  
 [PlusR(Sym)  $\xrightarrow{\text{pyk}}$  “lemma plusR(Sym)”]  
 [ReciprocalR(Axiom)  $\xrightarrow{\text{pyk}}$  “axiom reciprocalR”]  
 [LessMinus1(N)  $\xrightarrow{\text{pyk}}$  “1rule lessMinus1(N)”]  
 [Nonnegative(N)  $\xrightarrow{\text{pyk}}$  “axiom nonnegative(N)”]  
 [US0  $\xrightarrow{\text{pyk}}$  “axiom US0”]  
 [NextXS(UpperBound)  $\xrightarrow{\text{pyk}}$  “1rule nextXS(upperBound)”]  
 [NextXS(NoUpperBound)  $\xrightarrow{\text{pyk}}$  “1rule nextXS(noUpperBound)”]  
 [NextUS(UpperBound)  $\xrightarrow{\text{pyk}}$  “1rule nextUS(upperBound)”]  
 [NextUS(NoUpperBound)  $\xrightarrow{\text{pyk}}$  “1rule nextUS(noUpperBound)”]  
 [ExpZero  $\xrightarrow{\text{pyk}}$  “1rule expZero”]  
 [ExpPositive  $\xrightarrow{\text{pyk}}$  “1rule expPositive”]  
 [ExpZero(R)  $\xrightarrow{\text{pyk}}$  “1rule expZero(R)”]  
 [ExpPositive(R)  $\xrightarrow{\text{pyk}}$  “1rule expPositive(R)”]  
 [BSzero  $\xrightarrow{\text{pyk}}$  “1rule base(1/2)Sum zero”]  
 [BSpositive  $\xrightarrow{\text{pyk}}$  “1rule base(1/2)Sum positive”]  
 [UStescope(Zero)  $\xrightarrow{\text{pyk}}$  “1rule UStescope zero”]

[UStelescope(Positive)  $\xrightarrow{\text{pyk}}$  “1rule UStelescope positive”]  
 [EqAddition(R)  $\xrightarrow{\text{pyk}}$  “1rule adhoc eqAddition(R)”]  
 [FromLimit  $\xrightarrow{\text{pyk}}$  “1rule fromLimit”]  
 [ToUpperBound  $\xrightarrow{\text{pyk}}$  “1rule toUpperBound”]  
 [FromUpperBound  $\xrightarrow{\text{pyk}}$  “1rule fromUpperBound”]  
 [USisUpperBound  $\xrightarrow{\text{pyk}}$  “axiom USisUpperBound”]  
 [0not1(R)  $\xrightarrow{\text{pyk}}$  “axiom 0not1(R)”]  
 [ExpUnbounded(R)  $\xrightarrow{\text{pyk}}$  “1rule expUnbounded”]  
 [FromLeq(Advanced)(N)  $\xrightarrow{\text{pyk}}$  “1rule fromLeq(Advanced)(N)”]  
 [FromLeastUpperBound  $\xrightarrow{\text{pyk}}$  “1rule fromLeastUpperBound”]  
 [ToLeastUpperBound  $\xrightarrow{\text{pyk}}$  “1rule toLeastUpperBound”]  
 [XSisNotUpperBound  $\xrightarrow{\text{pyk}}$  “axiom XSisNotUpperBound”]  
 [ysFGreater  $\xrightarrow{\text{pyk}}$  “axiom ysFGreater”]  
 [ysFLess  $\xrightarrow{\text{pyk}}$  “axiom ysFLess”]  
 [SmallInverse  $\xrightarrow{\text{pyk}}$  “1rule smallInverse”]  
 [NatType  $\xrightarrow{\text{pyk}}$  “axiom natType”]  
 [RationalType  $\xrightarrow{\text{pyk}}$  “axiom rationalType”]  
 [SeriesType  $\xrightarrow{\text{pyk}}$  “axiom seriesType”]  
 [Max  $\xrightarrow{\text{pyk}}$  “axiom max”]  
 [Numerical  $\xrightarrow{\text{pyk}}$  “axiom numerical”]  
 [NumericalF  $\xrightarrow{\text{pyk}}$  “axiom numericalF”]  
 [MemberOfSeries(ImPLY)  $\xrightarrow{\text{pyk}}$  “axiom memberOfSeries”]  
 [JoinConjuncts(2conditions)  $\xrightarrow{\text{pyk}}$  “prop lemma doubly conditioned join conjuncts”]  
 [prop lemma imply negation  $\xrightarrow{\text{pyk}}$  “prop lemma imply negation”]  
 [TND  $\xrightarrow{\text{pyk}}$  “prop lemma tertium non datur”]  
 [FromNegatedImPLY  $\xrightarrow{\text{pyk}}$  “prop lemma from negated imply”]  
 [ToNegatedImPLY  $\xrightarrow{\text{pyk}}$  “prop lemma to negated imply”]  
 [FromNegated(2 \* ImPLY)  $\xrightarrow{\text{pyk}}$  “prop lemma from negated double imply”]  
 [FromNegatedAnd  $\xrightarrow{\text{pyk}}$  “prop lemma from negated and”]  
 [FromNegatedOr  $\xrightarrow{\text{pyk}}$  “prop lemma from negated or”]  
 [ToNegatedOr  $\xrightarrow{\text{pyk}}$  “prop lemma to negated or”]  
 [FromNegations  $\xrightarrow{\text{pyk}}$  “prop lemma from negations”]  
 [From3Disjuncts  $\xrightarrow{\text{pyk}}$  “prop lemma from three disjuncts”]  
 [From2 \* 2Disjuncts  $\xrightarrow{\text{pyk}}$  “prop lemma from two times two disjuncts”]

[NegateDisjunct1  $\xrightarrow{\text{pyk}}$  “prop lemma negate first disjunct”]  
 [NegateDisjunct2  $\xrightarrow{\text{pyk}}$  “prop lemma negate second disjunct”]  
 [ExpandDisjuncts  $\xrightarrow{\text{pyk}}$  “prop lemma expand disjuncts”]  
 [SENC1  $\xrightarrow{\text{pyk}}$  “lemma set equality nec condition(1)”]  
 [SENC2  $\xrightarrow{\text{pyk}}$  “lemma set equality nec condition(2)”]  
 [LessLeq(R)  $\xrightarrow{\text{pyk}}$  “lemma lessLeq(R)”]  
 [MemberOfSeries  $\xrightarrow{\text{pyk}}$  “lemma memberOfSeries”]  
 [memberOfSeries(Type)  $\xrightarrow{\text{pyk}}$  “lemma memberOfSeries(Type)”]  
 [\* (exp) \*  $\xrightarrow{\text{pyk}}$  “ $n \wedge m$ ”]  
 [R(\*)  $\xrightarrow{\text{pyk}}$  “R(  $n$  )”]  
 [– – R(\*)  $\xrightarrow{\text{pyk}}$  “–R(  $n$  )”]  
 [rec\*  $\xrightarrow{\text{pyk}}$  “1/  $n$ ”]  
 [\* / \*  $\xrightarrow{\text{pyk}}$  “eq-system of  $n$  modulo  $m$ ”]  
 [\*  $\cap$  \*  $\xrightarrow{\text{pyk}}$  “intersection  $n$  comma  $m$  end intersection”]  
 [\* [\*]  $\xrightarrow{\text{pyk}}$  “[  $n$  ;  $m$  ]”]  
 [ $\cup$ \*  $\xrightarrow{\text{pyk}}$  “union  $n$  end union”]  
 [\*  $\cup$  \*  $\xrightarrow{\text{pyk}}$  “binary-union  $n$  comma  $m$  end union”]  
 [P(\*)  $\xrightarrow{\text{pyk}}$  “power  $n$  end power”]  
 [{\*}  $\xrightarrow{\text{pyk}}$  “zermelo singleton  $n$  end singleton”]  
 [StateExpand(\*, \*, \*)  $\xrightarrow{\text{pyk}}$  “stateExpand(  $n$  ,  $m$  ,  $k$  )”]  
 [extractSeries(\*)  $\xrightarrow{\text{pyk}}$  “extractSeries(  $n$  )”]  
 [SetOfSeries(\*)  $\xrightarrow{\text{pyk}}$  “setOfSeries(  $n$  )”]  
 [– – Macro(\*)  $\xrightarrow{\text{pyk}}$  “–Macro(  $n$  )”]  
 [ExpandList(\*, \*, \*)  $\xrightarrow{\text{pyk}}$  “expandList(  $n$  ,  $m$  ,  $k$  )”]  
 [\* \* Macro(\*)  $\xrightarrow{\text{pyk}}$  “\*\*Macro(  $n$  )”]  
 [+ + Macro(\*)  $\xrightarrow{\text{pyk}}$  “++Macro(  $n$  )”]  
 [<< Macro(\*)  $\xrightarrow{\text{pyk}}$  “<<Macro(  $n$  )”]  
 [||Macro(\*)  $\xrightarrow{\text{pyk}}$  “||Macro(  $n$  )”]  
 [01//Macro(\*)  $\xrightarrow{\text{pyk}}$  “01//Macro(  $n$  )”]  
 [UB(\*, \*)  $\xrightarrow{\text{pyk}}$  “upperBound(  $n$  ,  $m$  )”]  
 [LUB(\*, \*)  $\xrightarrow{\text{pyk}}$  “leastUpperBound(  $n$  ,  $m$  )”]  
 [BS(\*, \*)  $\xrightarrow{\text{pyk}}$  “base(1/2)Sum(  $n$  ,  $m$  )”]  
 [USteelescope(\*, \*)  $\xrightarrow{\text{pyk}}$  “USteelescope(  $n$  ,  $m$  )”]  
 [(\*)  $\xrightarrow{\text{pyk}}$  “(  $n$  )”]  
 [|f \* |  $\xrightarrow{\text{pyk}}$  “|f  $n$  |”]

$[|r * | \xrightarrow{\text{pyk}} \text{"|r " |"}]$   
 $[\text{Limit}(*, *) \xrightarrow{\text{pyk}} \text{"limit( " , " )"}]$   
 $[\text{Union}(*, *) \xrightarrow{\text{pyk}} \text{"U( " )"}]$   
 $[\text{IsOrderedPair}(*, *, *) \xrightarrow{\text{pyk}} \text{"isOrderedPair( " , " , " )"}]$   
 $[\text{IsRelation}(*, *, *) \xrightarrow{\text{pyk}} \text{"isRelation( " , " , " )"}]$   
 $[\text{isFunction}(*, *, *) \xrightarrow{\text{pyk}} \text{"isFunction( " , " , " )"}]$   
 $[\text{IsSeries}(*, *) \xrightarrow{\text{pyk}} \text{"isSeries( " , " )"}]$   
 $[\text{IsNatural}(*, *) \xrightarrow{\text{pyk}} \text{"isNatural( " )"}]$   
 $[\text{OrderedPair}(*, *) \xrightarrow{\text{pyk}} \text{"(o " , " )"}]$   
 $[\text{TypeNat}(*, *) \xrightarrow{\text{pyk}} \text{"typeNat( " )"}]$   
 $[\text{TypeNat0}(*, *) \xrightarrow{\text{pyk}} \text{"typeNat0( " )"}]$   
 $[\text{TypeRational}(*, *) \xrightarrow{\text{pyk}} \text{"typeRational( " )"}]$   
 $[\text{TypeRational0}(*, *) \xrightarrow{\text{pyk}} \text{"typeRational0( " )"}]$   
 $[\text{TypeSeries}(*, *) \xrightarrow{\text{pyk}} \text{"typeSeries( " , " )"}]$   
 $[\text{Typeseries0}(*, *) \xrightarrow{\text{pyk}} \text{"typeSeries0( " , " )"}]$   
 $[\{*, *\} \xrightarrow{\text{pyk}} \text{"zermelo pair " comma " end pair"}]$   
 $[\langle *, *\rangle \xrightarrow{\text{pyk}} \text{"zermelo ordered pair " comma " end pair"}]$   
 $[(-u*) \xrightarrow{\text{pyk}} \text{"- "}]$   
 $[-f* \xrightarrow{\text{pyk}} \text{"-f "}]$   
 $[(- - *) \xrightarrow{\text{pyk}} \text{"-- "}]$   
 $[1f/* \xrightarrow{\text{pyk}} \text{"1f/ "}]$   
 $[01//temp* \xrightarrow{\text{pyk}} \text{"01// "}]$   
 $[*(*, *) \xrightarrow{\text{pyk}} \text{" " is related to " under "}]$   
 $[\text{ReffRel}(*, *) \xrightarrow{\text{pyk}} \text{" " is reflexive relation in "}]$   
 $[\text{SymRel}(*, *) \xrightarrow{\text{pyk}} \text{" " is symmetric relation in "}]$   
 $[\text{TransRel}(*, *) \xrightarrow{\text{pyk}} \text{" " is transitive relation in "}]$   
 $[\text{EqRel}(*, *) \xrightarrow{\text{pyk}} \text{" " is equivalence relation in "}]$   
 $[[* \in *]_* \xrightarrow{\text{pyk}} \text{"equivalence class of " in " modulo "}]$   
 $[\text{Partition}(*, *) \xrightarrow{\text{pyk}} \text{" " is partition of "}]$   
 $[(***) \xrightarrow{\text{pyk}} \text{" " * "}]$   
 $[* *f * \xrightarrow{\text{pyk}} \text{" " *f "}]$   
 $[* * ** \xrightarrow{\text{pyk}} \text{" " ** "}]$   
 $[(* + *) \xrightarrow{\text{pyk}} \text{" " + "}]$   
 $[(* - *) \xrightarrow{\text{pyk}} \text{" " - "}]$   
 $[* +f * \xrightarrow{\text{pyk}} \text{" " +f "}]$

$[* -_f * \xrightarrow{\text{pyk}} \text{" -f "}]$   
 $[* + + * \xrightarrow{\text{pyk}} \text{" ++ "}]$   
 $[\text{R}(* ) - - \text{R}(* ) \xrightarrow{\text{pyk}} \text{"R( ) -- R( )"}]$   
 $[* \in * \xrightarrow{\text{pyk}} \text{" in0 "}]$   
 $[| * | \xrightarrow{\text{pyk}} \text{" | "}]$   
 $[\text{if}(*, *, *) \xrightarrow{\text{pyk}} \text{"if( , , )"}]$   
 $[\text{Max}(*, *) \xrightarrow{\text{pyk}} \text{"max( , )"}]$   
 $[\text{Max}(*, *) \xrightarrow{\text{pyk}} \text{"maxR( , )"}]$   
 $[* = * \xrightarrow{\text{pyk}} \text{" = "}]$   
 $[* \neq * \xrightarrow{\text{pyk}} \text{" != "}]$   
 $[* \leq * \xrightarrow{\text{pyk}} \text{" \leq "}]$   
 $[* < * \xrightarrow{\text{pyk}} \text{" < "}]$   
 $[* <_f * \xrightarrow{\text{pyk}} \text{" <_f "}]$   
 $[* \leq_f * \xrightarrow{\text{pyk}} \text{" \leq_f "}]$   
 $[\text{SF}(*, *) \xrightarrow{\text{pyk}} \text{" sameF "}]$   
 $[* == * \xrightarrow{\text{pyk}} \text{" == "}]$   
 $[* !! == * \xrightarrow{\text{pyk}} \text{" !! == "}]$   
 $[* << * \xrightarrow{\text{pyk}} \text{" << "}]$   
 $[* << == * \xrightarrow{\text{pyk}} \text{" << == "}]$   
 $[* == * \xrightarrow{\text{pyk}} \text{" zermelo is "}]$   
 $[* \subseteq * \xrightarrow{\text{pyk}} \text{" is subset of "}]$   
 $[\dot{\neg} (* ) \xrightarrow{\text{pyk}} \text{"not0 "}]$   
 $[* \notin * \xrightarrow{\text{pyk}} \text{" zermelo ~in "}]$   
 $[* \neq * \xrightarrow{\text{pyk}} \text{" zermelo ~is "}]$   
 $[* \wedge * \xrightarrow{\text{pyk}} \text{" and0 "}]$   
 $[* \vee * \xrightarrow{\text{pyk}} \text{" or0 "}]$   
 $[\exists *: * \xrightarrow{\text{pyk}} \text{"exist0 " indeed "}]$   
 $[* \Leftrightarrow * \xrightarrow{\text{pyk}} \text{" iff "}]$   
 $[\{\text{ph} \in * \mid *\} \xrightarrow{\text{pyk}} \text{"the set of ph in " such that " end set"}]$   
 $[\text{kvanti} \xrightarrow{\text{pyk}} \text{"kvanti"}]$   
 $)^{\mathbf{P}}$

## B T<sub>E</sub>X definitioner

[kvanti <sup>tex</sup> ≡ “kvanti”]

[( $\cdots$ ) <sup>tex</sup> ≡ “(\cdots{ })”]

[Objekt-var <sup>tex</sup> ≡ “\texttt{Objekt-var}”]

[Ex-var <sup>tex</sup> ≡ “\texttt{Ex-var}”]

[Ph-var <sup>tex</sup> ≡ “\texttt{Ph-var}”]

[Værdi <sup>tex</sup> ≡ “\texttt{V\ae{ }rdi}”]

[Variabel <sup>tex</sup> ≡ “\texttt{Variabel}”]

[Op(x) <sup>tex</sup> ≡ “Op(#1.  
)”]

[Op(x, y) <sup>tex</sup> ≡ “Op(#1.  
, #2.  
)”]

[ $x \doteq y$  <sup>tex</sup> ≡ “#1.  
\mathrel {\ddot{=} } #2.”]

[ContainsEmpty(x) <sup>tex</sup> ≡ “ContainsEmpty(#1.  
)”]

[Dedu(x, y) <sup>tex</sup> ≡ “  
Dedu(#1.  
, #2.  
)”]

[Dedu<sub>0</sub>(x, y) <sup>tex</sup> ≡ “  
Dedu\_0(#1.  
, #2.  
)”]

[Dedu<sub>s</sub>(x, y, z) <sup>tex</sup> ≡ “Dedu\_{s}(#1.  
, #2.  
, #3.  
)”]

[Dedu<sub>1</sub>(x, y, z) <sup>tex</sup> ≡ “  
Dedu\_1(#1.  
, #2.  
)”]

, #3.  
)”]

[Dedu<sub>2</sub>(x, y, z)  $\stackrel{\text{tex}}{=} “$   
Dedu\_2(#1.

, #2.  
, #3.  
)”]

[Dedu<sub>3</sub>(x, y, z, u)  $\stackrel{\text{tex}}{=} “$   
Dedu\_3(#1.

, #2.  
, #3.  
, #4.  
)”]

[Dedu<sub>4</sub>(x, y, z, u)  $\stackrel{\text{tex}}{=} “$   
Dedu\_4(#1.

, #2.  
, #3.  
, #4.  
)”]

[Dedu<sub>4</sub><sup>\*</sup>(x, y, z, u)  $\stackrel{\text{tex}}{=} “$   
Dedu\_4<sup>\*</sup>(#1.

, #2.  
, #3.  
, #4.  
)”]

[Dedu<sub>5</sub>(x, y, z)  $\stackrel{\text{tex}}{=} “$   
Dedu\_5(#1.

, #2.  
, #3.  
)”]

[Dedu<sub>6</sub>(p, c, e, b)  $\stackrel{\text{tex}}{=} “$   
Dedu\_6(#1.

, #2.  
, #3.  
, #4.  
)”]

[Dedu<sub>6</sub><sup>\*</sup>(p, c, e, b)  $\stackrel{\text{tex}}{=} “$   
Dedu\_6<sup>\*</sup>(#1.

, #2.  
, #3.



, #4.  
)”]

[Dedu<sub>7</sub>(p) <sup>tex</sup> ≡ “  
Dedu\_7(#1.  
)”]

[Dedu<sub>8</sub>(p, b) <sup>tex</sup> ≡ “  
Dedu\_8(#1.  
, #2.  
)”]

[Dedu<sub>8</sub><sup>\*</sup>(p, b) <sup>tex</sup> ≡ “  
Dedu\_8^\*(#1.  
, #2.  
)”]

[EX<sub>1</sub> <sup>tex</sup> ≡ “EX\_{1}”]

[EX<sub>2</sub> <sup>tex</sup> ≡ “EX\_{2}”]

[EX<sub>10</sub> <sup>tex</sup> ≡ “EX\_{10}”]

[EX<sub>20</sub> <sup>tex</sup> ≡ “EX\_{20}”]

[x<sub>EX</sub> <sup>tex</sup> ≡ “#1.  
\_{EX}”]

[x<sup>EX</sup> <sup>tex</sup> ≡ “#1.  
^\_{EX}”]

[(x≡y|z:=u)<sub>EX</sub> <sup>tex</sup> ≡ “\langle #1.  
{\equiv} #2.  
| #3.  
{:=} #4.  
\rangle\_{EX} ”]

[(x≡<sup>0</sup>y|z:=u)<sub>EX</sub> <sup>tex</sup> ≡ “\langle #1.  
{\equiv}^0 #2.  
| #3.  
{:=} #4.  
\rangle\_{EX} ”]

[(x≡<sup>1</sup>y|z:=u)<sub>EX</sub> <sup>tex</sup> ≡ “\langle #1.  
{\equiv}^1 #2.  
| #3.  
{:=} #4.  
\rangle\_{EX} ”]

$\langle x \equiv *y | z := u \rangle_{\text{Ex}} \stackrel{\text{tex}}{=} \backslash\langle \#1.$   
 $\{\backslash\text{equiv}\}^{\wedge *} \#2.$   
 $| \#3.$   
 $\{:=\} \#4.$   
 $\rangle_{\text{range}_{\{\text{Ex}\}}} \text{ ”}$

$[\text{ph}_1 \stackrel{\text{tex}}{=} \text{“ph}_{\{1\}}\text{”}]$

$[\text{ph}_2 \stackrel{\text{tex}}{=} \text{“ph}_{\{2\}}\text{”}]$

$[\text{ph}_3 \stackrel{\text{tex}}{=} \text{“ph}_{\{3\}}\text{”}]$

$[\text{ph}_4 \stackrel{\text{tex}}{=} \text{“ph}_{\{4\}}\text{”}]$

$[\text{ph}_5 \stackrel{\text{tex}}{=} \text{“ph}_{\{5\}}\text{”}]$

$[\text{ph}_6 \stackrel{\text{tex}}{=} \text{“ph}_{\{6\}}\text{”}]$

$[*_{\text{Ph}} \stackrel{\text{tex}}{=} \text{“\#1.}$   
 $\text{-}\{\text{Ph}\} \text{ ”}]$

$[x^{\text{Ph}} \stackrel{\text{tex}}{=} \text{“\#1.}$   
 $\wedge \{\text{Ph}\} \text{”}]$

$\langle x \equiv y | z := u \rangle_{\text{Ph}} \stackrel{\text{tex}}{=} \backslash\langle \#1.$   
 $\{\backslash\text{equiv}\} \#2.$   
 $| \#3.$   
 $\{:=\} \#4.$   
 $\rangle_{\text{range}_{\{\text{Ph}\}}} \text{ ”}$

$\langle x \equiv^0 y | z := u \rangle_{\text{Ph}} \stackrel{\text{tex}}{=} \backslash\langle \#1.$   
 $\{\backslash\text{equiv}\}^{\wedge 0} \#2.$   
 $| \#3.$   
 $\{:=\} \#4.$   
 $\rangle_{\text{range}_{\{\text{Ph}\}}} \text{ ”}$

$\langle x \equiv^1 y | z := u \rangle_{\text{Ph}} \stackrel{\text{tex}}{=} \backslash\langle \#1.$   
 $\{\backslash\text{equiv}\}^{\wedge 1} \#2.$   
 $| \#3.$   
 $\{:=\} \#4.$   
 $\rangle_{\text{range}_{\{\text{Ph}\}}} \text{ ”}$

$\langle x \equiv *y | z := u \rangle_{\text{Ph}} \stackrel{\text{tex}}{=} \backslash\langle \#1.$   
 $\{\backslash\text{equiv}\}^{\wedge *} \#2.$   
 $| \#3.$   
 $\{:=\} \#4.$   
 $\rangle_{\text{range}_{\{\text{Ph}\}}} \text{ ”}$

[bs <sup>tex</sup> ≡ “\mathsf {bs}”]

[OBS <sup>tex</sup> ≡ “ \mathsf {OBS}”]

[BS <sup>tex</sup> ≡ “{\cal BS}”]

[∅ <sup>tex</sup> ≡ “\mathrm{\O}”]

[SystemQ <sup>tex</sup> ≡ “SystemQ”]

[MP <sup>tex</sup> ≡ “MP”]

[Gen <sup>tex</sup> ≡ “Gen”]

[Repetition <sup>tex</sup> ≡ “Repetition”]

[Neg <sup>tex</sup> ≡ “Neg”]

[Ded <sup>tex</sup> ≡ “Ded”]

[ExistIntro <sup>tex</sup> ≡ “ExistIntro”]

[Extensionality <sup>tex</sup> ≡ “Extensionality”]

[∅def <sup>tex</sup> ≡ “\O{}def”]

[PairDef <sup>tex</sup> ≡ “PairDef”]

[UnionDef <sup>tex</sup> ≡ “UnionDef”]

[PowerDef <sup>tex</sup> ≡ “PowerDef”]

[SeparationDef <sup>tex</sup> ≡ “SeparationDef”]

[AddDoubleNeg <sup>tex</sup> ≡ “AddDoubleNeg”]

[RemoveDoubleNeg <sup>tex</sup> ≡ “RemoveDoubleNeg”]

[AndCommutativity <sup>tex</sup> ≡ “AndCommutativity”]

[AutoImply <sup>tex</sup> ≡ “AutoImply”]

[Contrapositive <sup>tex</sup> ≡ “Contrapositive”]

[FirstConjunct <sup>tex</sup> ≡ “FirstConjunct”]

[SecondConjunct <sup>tex</sup> ≡ “SecondConjunct”]

[FromContradiction <sup>tex</sup> ≡ “FromContradiction”]

[FromDisjuncts  $\stackrel{\text{tex}}{=} \text{“FromDisjuncts”}$ ]  
 [IffCommutativity  $\stackrel{\text{tex}}{=} \text{“IffCommutativity”}$ ]  
 [IffFirst  $\stackrel{\text{tex}}{=} \text{“IffFirst”}$ ]  
 [IffSecond  $\stackrel{\text{tex}}{=} \text{“IffSecond”}$ ]  
 [ImplyTransitivity  $\stackrel{\text{tex}}{=} \text{“ImplyTransitivity”}$ ]  
 [JoinConjuncts  $\stackrel{\text{tex}}{=} \text{“JoinConjuncts”}$ ]  
 [MP2  $\stackrel{\text{tex}}{=} \text{“MP2”}$ ]  
 [MP3  $\stackrel{\text{tex}}{=} \text{“MP3”}$ ]  
 [MP4  $\stackrel{\text{tex}}{=} \text{“MP4”}$ ]  
 [MP5  $\stackrel{\text{tex}}{=} \text{“MP5”}$ ]  
 [MT  $\stackrel{\text{tex}}{=} \text{“MT”}$ ]  
 [NegativeMT  $\stackrel{\text{tex}}{=} \text{“NegativeMT”}$ ]  
 [Technicality  $\stackrel{\text{tex}}{=} \text{“Technicality”}$ ]  
 [Weakening  $\stackrel{\text{tex}}{=} \text{“Weakening”}$ ]  
 [WeakenOr1  $\stackrel{\text{tex}}{=} \text{“WeakenOr1”}$ ]  
 [WeakenOr2  $\stackrel{\text{tex}}{=} \text{“WeakenOr2”}$ ]  
 [Pair2Formula  $\stackrel{\text{tex}}{=} \text{“Pair2Formula”}$ ]  
 [Formula2Pair  $\stackrel{\text{tex}}{=} \text{“Formula2Pair”}$ ]  
 [Union2Formula  $\stackrel{\text{tex}}{=} \text{“Union2Formula”}$ ]  
 [Formula2Union  $\stackrel{\text{tex}}{=} \text{“Formula2Union”}$ ]  
 [Formula2Power  $\stackrel{\text{tex}}{=} \text{“Formula2Power”}$ ]  
 [Sep2Formula  $\stackrel{\text{tex}}{=} \text{“Sep2Formula”}$ ]  
 [Formula2Sep  $\stackrel{\text{tex}}{=} \text{“Formula2Sep”}$ ]  
 [SubsetInPower  $\stackrel{\text{tex}}{=} \text{“SubsetInPower”}$ ]  
 [HelperPowerIsSub  $\stackrel{\text{tex}}{=} \text{“HelperPowerIsSub”}$ ]

[PowerIsSub  $\stackrel{\text{tex}}{\equiv}$  “PowerIsSub”]

[(Switch)HelperPowerIsSub  $\stackrel{\text{tex}}{\equiv}$  “(Switch)HelperPowerIsSub”]

[(Switch)PowerIsSub  $\stackrel{\text{tex}}{\equiv}$  “(Switch)PowerIsSub”]

[ToSetEquality  $\stackrel{\text{tex}}{\equiv}$  “ToSetEquality”]

[HelperToSetEquality(t)  $\stackrel{\text{tex}}{\equiv}$  “HelperToSetEquality(t)”]

[ToSetEquality(t)  $\stackrel{\text{tex}}{\equiv}$  “ToSetEquality(t)”]

[HelperFromSetEquality  $\stackrel{\text{tex}}{\equiv}$  “HelperFromSetEquality”]

[FromSetEquality  $\stackrel{\text{tex}}{\equiv}$  “FromSetEquality”]

[HelperReflexivity  $\stackrel{\text{tex}}{\equiv}$  “HelperReflexivity”]

[Reflexivity  $\stackrel{\text{tex}}{\equiv}$  “Reflexivity”]

[HelperSymmetry  $\stackrel{\text{tex}}{\equiv}$  “HelperSymmetry”]

[Symmetry  $\stackrel{\text{tex}}{\equiv}$  “Symmetry”]

[HelperTransitivity  $\stackrel{\text{tex}}{\equiv}$  “HelperTransitivity”]

[Transitivity  $\stackrel{\text{tex}}{\equiv}$  “Transitivity”],

[ERisReflexive  $\stackrel{\text{tex}}{\equiv}$  “ERisReflexive”]

[ERisSymmetric  $\stackrel{\text{tex}}{\equiv}$  “ERisSymmetric”]

[ERisTransitive  $\stackrel{\text{tex}}{\equiv}$  “ERisTransitive”]

[ $\emptyset$ isSubset  $\stackrel{\text{tex}}{\equiv}$  “ $\emptyset$ isSubset”]

[HelperMemberNot $\emptyset$   $\stackrel{\text{tex}}{\equiv}$  “HelperMemberNot $\emptyset$ ”]

[MemberNot $\emptyset$   $\stackrel{\text{tex}}{\equiv}$  “MemberNot $\emptyset$ ”]

[HelperUnique $\emptyset$   $\stackrel{\text{tex}}{\equiv}$  “HelperUnique $\emptyset$ ”]

[Unique $\emptyset$   $\stackrel{\text{tex}}{\equiv}$  “Unique $\emptyset$ ”]

[== Reflexivity  $\stackrel{\text{tex}}{\equiv}$  “==\!{}Reflexivity”]

[== Symmetry  $\stackrel{\text{tex}}{\equiv}$  “==\!{}Symmetry”]

[Helper == Transitivity  $\stackrel{\text{tex}}{\equiv}$  “Helper\!{}==\!{}Transitivity”]

[ $\equiv$ Transitivity  $\stackrel{\text{tex}}{=} \text{"\{\}=\!\{\}$ Transitivity"]

[HelperTransferNotEq  $\stackrel{\text{tex}}{=} \text{"HelperTransferNotEq"}$ ]

[TransferNotEq  $\stackrel{\text{tex}}{=} \text{"TransferNotEq"}$ ]

[HelperPairSubset  $\stackrel{\text{tex}}{=} \text{"HelperPairSubset"}$ ]

[Helper(2)PairSubset  $\stackrel{\text{tex}}{=} \text{"Helper(2)PairSubset"}$ ]

[PairSubset  $\stackrel{\text{tex}}{=} \text{"PairSubset"}$ ]

[SamePair  $\stackrel{\text{tex}}{=} \text{"SamePair"}$ ]

[SameSingleton  $\stackrel{\text{tex}}{=} \text{"SameSingleton"}$ ]

[UnionSubset  $\stackrel{\text{tex}}{=} \text{"UnionSubset"}$ ]

[SameUnion  $\stackrel{\text{tex}}{=} \text{"SameUnion"}$ ]

[SeparationSubset  $\stackrel{\text{tex}}{=} \text{"SeparationSubset"}$ ]

[SameSeparation  $\stackrel{\text{tex}}{=} \text{"SameSeparation"}$ ]

[SameBinaryUnion  $\stackrel{\text{tex}}{=} \text{"SameBinaryUnion"}$ ]

[IntersectionSubset  $\stackrel{\text{tex}}{=} \text{"IntersectionSubset"}$ ]

[SameIntersection  $\stackrel{\text{tex}}{=} \text{"SameIntersection"}$ ]

[AutoMember  $\stackrel{\text{tex}}{=} \text{"AutoMember"}$ ]

[HelperEqSysNot $\emptyset$   $\stackrel{\text{tex}}{=} \text{"HelperEqSysNot\O\}"}$ ]

[EqSysNot $\emptyset$   $\stackrel{\text{tex}}{=} \text{"EqSysNot\O\}"}$ ]

[HelperEqSubset  $\stackrel{\text{tex}}{=} \text{"HelperEqSubset"}$ ]

[EqSubset  $\stackrel{\text{tex}}{=} \text{"EqSubset"}$ ]

[EqNecessary  $\stackrel{\text{tex}}{=} \text{"EqNecessary"}$ ]

[HelperEqNecessary  $\stackrel{\text{tex}}{=} \text{"HelperEqNecessary"}$ ]

[HelperNoneEqNecessary  $\stackrel{\text{tex}}{=} \text{"HelperNoneEqNecessary"}$ ]

[Helper(2)NoneEqNecessary  $\stackrel{\text{tex}}{=} \text{"Helper(2)NoneEqNecessary"}$ ]

[NoneEqNecessary  $\stackrel{\text{tex}}{=} \text{"NoneEqNecessary"}$ ]

[EqClassIsSubset  $\stackrel{\text{tex}}{=} \text{“EqClassIsSubset”}$ ]

[EqClassesAreDisjoint  $\stackrel{\text{tex}}{=} \text{“EqClassesAreDisjoint”}$ ]

[AllDisjoint  $\stackrel{\text{tex}}{=} \text{“AllDisjoint”}$ ]

[AllDisjointImply  $\stackrel{\text{tex}}{=} \text{“AllDisjointImply”}$ ]

[BSsubset  $\stackrel{\text{tex}}{=} \text{“BSsubset”}$ ]

[Union(BS/R)subset  $\stackrel{\text{tex}}{=} \text{“Union(BS/R)subset”}$ ]

[UnionIdentity  $\stackrel{\text{tex}}{=} \text{“UnionIdentity”}$ ]

[EqSysIsPartition  $\stackrel{\text{tex}}{=} \text{“EqSysIsPartition”}$ ]

[x/y  $\stackrel{\text{tex}}{=} \text{“\#1.}$   
 $\text{/ \#2.”}$ ]

[x  $\cap$  y  $\stackrel{\text{tex}}{=} \text{“\#1.}$   
 $\backslash\text{cap \#2.”}$ ]

[ $\cup$ x  $\stackrel{\text{tex}}{=} \text{“\backslashcup \#1.”}$ ]

[x  $\cup$  y  $\stackrel{\text{tex}}{=} \text{“\#1.}$   
 $\backslash\text{mathrel{\backslashcup} \#2.”}$ ]

[P(x)  $\stackrel{\text{tex}}{=} \text{“P(\#1.}$   
 $\text{)”}$ ]

[{x}  $\stackrel{\text{tex}}{=} \text{“\{\#1.}$   
 $\backslash\text{”}$ ]

[{x, y}  $\stackrel{\text{tex}}{=} \text{“\{\#1.}$   
 $\text{\#2.}$   
 $\backslash\text{”}$ ]

[ $\langle$ x, y $\rangle$   $\stackrel{\text{tex}}{=} \text{“\langle \#1.}$   
 $\text{\#2.}$   
 $\backslash\text{rangle”}$ ],

[x  $\in$  y  $\stackrel{\text{tex}}{=} \text{“\#1.}$   
 $\backslash\text{mathrel{\backslashin} \#2.”}$ ]

[z(x, y)  $\stackrel{\text{tex}}{=} \text{“\#3.}$   
 $\text{(\#1.}$   
 $\text{\#2.}$   
 $\text{)”}$ ]

[RefRel( $r, x$ )  $\stackrel{\text{tex}}{\equiv}$  “RefRel(#1.  
, #2.  
)”]

[SymRel( $r, x$ )  $\stackrel{\text{tex}}{\equiv}$  “SymRel(#1.  
, #2.  
)”]

[TransRel( $r, x$ )  $\stackrel{\text{tex}}{\equiv}$  “TransRel(#1.  
, #2.  
)”]

[EqRel( $r, x$ )  $\stackrel{\text{tex}}{\equiv}$  “EqRel(#1.  
, #2.  
)”]

[ $[x \in \text{bs}]_r$   $\stackrel{\text{tex}}{\equiv}$  “[#1.  
 $\backslash\mathrel{\in}$  #2.  
]\_{#3.  
}”]

[Partition( $x, y$ )  $\stackrel{\text{tex}}{\equiv}$  “Partition(#1.  
, #2.  
)”]

[ $x == y$   $\stackrel{\text{tex}}{\equiv}$  “#1.  
 $\backslash!\mathrel{==}$  #2.”]

[ $x \subseteq y$   $\stackrel{\text{tex}}{\equiv}$  “#1.  
 $\backslash\mathrel{\subseteq}$  #2.”]

[ $\dot{\neg}(x)_n$   $\stackrel{\text{tex}}{\equiv}$  “ $\backslash\dot{\neg}$ , (#1.  
)\_n”]

[ $x \notin y$   $\stackrel{\text{tex}}{\equiv}$  “#1.  
 $\backslash\mathrel{\notin}$  #2.”]

[ $x \neq y$   $\stackrel{\text{tex}}{\equiv}$  “#1.  
 $\backslash\mathrel{\neq}$  #2.”]

[ $x \dot{\wedge} y$   $\stackrel{\text{tex}}{\equiv}$  “#1.  
 $\backslash\mathrel{\dot{\wedge}}$  #2.”]

[ $x \dot{\vee} y$   $\stackrel{\text{tex}}{\equiv}$  “#1.  
 $\backslash\mathrel{\dot{\vee}}$  #2.”]

[ $x \dot{\leftrightarrow} y$   $\stackrel{\text{tex}}{\equiv}$  “#1.  
 $\backslash\mathrel{\dot{\leftrightarrow}}$  #2.”]



[{ph ∈ x | a} <sup>tex</sup> “ \{ ph \mathrel{\in} #1.  
\mid #2.  
\}”]

[x ⇒ y <sup>tex</sup> “(i#1.  
\Rightarrow #2.  
i”]

[Nat(x) <sup>tex</sup> “Nat(#1.  
)”]

[(x≡y|z:=u)<sub>Me</sub> <sup>tex</sup> “\langle #1.  
\equiv #2.  
| #3.  
{:=} #4.  
\rangle\_{Me}”]

[(x≡<sup>1</sup>y|z:=u)<sub>Me</sub> <sup>tex</sup> “\langle #1.  
\equiv<sup>1</sup> #2.  
| #3.  
{:=} #4.  
\rangle\_{Me} ”]

[(x≡\*y|z:=u)<sub>Me</sub> <sup>tex</sup> “\langle #1.  
\equiv\* #2.  
| #3.  
{:=} #4.  
\rangle\_{Me} ”]

[∃x:y <sup>tex</sup> “  
\exists #1.  
\colon #2.”]

[(x1) <sup>tex</sup> “(x1)”]

[(x2) <sup>tex</sup> “(x2)”]

[(y1) <sup>tex</sup> “(y1)”]

[(y2) <sup>tex</sup> “(y2)”]

[(v1) <sup>tex</sup> “(v1)”]

[(v2) <sup>tex</sup> “(v2)”]

[(v3) <sup>tex</sup> “(v3)”]

[(v4) <sup>tex</sup> “(v4)”]

$[(v2n) \stackrel{\text{tex}}{=} "(v2n)"]$

$[(n1) \stackrel{\text{tex}}{=} "(n1)"]$

$[(n2) \stackrel{\text{tex}}{=} "(n2)"]$

$[(n3) \stackrel{\text{tex}}{=} "(n3)"]$

$[(m1) \stackrel{\text{tex}}{=} "(m1)"]$

$[(m2) \stackrel{\text{tex}}{=} "(m2)"]$

$[(\epsilon) \stackrel{\text{tex}}{=} "(\backslash\epsilonpsilon)"]$

$[(\epsilon)_1 \stackrel{\text{tex}}{=} "(\backslash\epsilonpsilon)_{-}\{1\}"]$

$[(\epsilon 2) \stackrel{\text{tex}}{=} "(\backslash\epsilonpsilon 2)"]$

$[(fx) \stackrel{\text{tex}}{=} "(fx)"]$

$[(fy) \stackrel{\text{tex}}{=} "(fy)"]$

$[(fz) \stackrel{\text{tex}}{=} "(fz)"]$

$[(fu) \stackrel{\text{tex}}{=} "(fu)"]$

$[(fv) \stackrel{\text{tex}}{=} "(fv)"]$

$[(fw) \stackrel{\text{tex}}{=} "(fw)"]$

$[(fep) \stackrel{\text{tex}}{=} "(fep)"]$

$[(rx) \stackrel{\text{tex}}{=} "(rx)"]$

$[(ry) \stackrel{\text{tex}}{=} "(ry)"]$

$[(rz) \stackrel{\text{tex}}{=} "(rz)"]$

$[(ru) \stackrel{\text{tex}}{=} "(ru)"]$

$[(sx) \stackrel{\text{tex}}{=} "(sx)"]$

$[(sx1) \stackrel{\text{tex}}{=} "(sx1)"]$

$[(sy) \stackrel{\text{tex}}{=} "(sy)"]$

$[(sy1) \stackrel{\text{tex}}{=} "(sy1)"]$

$[(sz) \stackrel{\text{tex}}{=} "(sz)"]$

$[(sz1) \stackrel{\text{tex}}{=} "(sz1)"]$

$[(su) \stackrel{\text{tex}}{=} "(su)"]$

$[(su1) \stackrel{\text{tex}}{=} "(su1)"]$

$[(fxs) \stackrel{\text{tex}}{=} "(fxs)"]$

$[(fys) \stackrel{\text{tex}}{=} "(fys)"]$

$[(crs1) \stackrel{\text{tex}}{=} "(crs1)"]$

$[(f1) \stackrel{\text{tex}}{=} "(f1)"]$

$[(f2) \stackrel{\text{tex}}{=} "(f2)"]$

$[(f3) \stackrel{\text{tex}}{=} "(f3)"]$

$[(f4) \stackrel{\text{tex}}{=} "(f4)"]$

$[(op1) \stackrel{\text{tex}}{=} "(op1)"]$

$[(op2) \stackrel{\text{tex}}{=} "(op2)"]$

$[(r1) \stackrel{\text{tex}}{=} "(r1)"]$

$[(s1) \stackrel{\text{tex}}{=} "(s1)"]$

$[(s2) \stackrel{\text{tex}}{=} "(s2)"]$

$[X_1 \stackrel{\text{tex}}{=} "X_{\{1\}}"]$

$[X_2 \stackrel{\text{tex}}{=} "X_{\{2\}}"]$

$[Y_1 \stackrel{\text{tex}}{=} "Y_{\{1\}}"]$

$[Y_2 \stackrel{\text{tex}}{=} "Y_{\{2\}}"]$

$[V_1 \stackrel{\text{tex}}{=} "V_{\{1\}}"]$

$[V_2 \stackrel{\text{tex}}{=} "V_{\{2\}}"]$

$[V_3 \stackrel{\text{tex}}{=} "V_{\{3\}}"]$

$[V_4 \stackrel{\text{tex}}{=} "V_{\{4\}}"]$

$[V_{2n} \stackrel{\text{tex}}{=} "V_{\{2n\}}"]$

$[\epsilon \stackrel{\text{tex}}{=} "\epsilon"]$

[M<sub>1</sub> <sup>tex</sup> ≡ “M\_{1}”]

[M<sub>2</sub> <sup>tex</sup> ≡ “M\_{2}”]

[N<sub>1</sub> <sup>tex</sup> ≡ “N\_{1} ”]

[N<sub>2</sub> <sup>tex</sup> ≡ “N\_{2} ”]

[N<sub>3</sub> <sup>tex</sup> ≡ “N\_{3} ”]

[ε<sub>1</sub> <sup>tex</sup> ≡ “\epsilon 1”]

[ε<sub>2</sub> <sup>tex</sup> ≡ “\epsilon 2”]

[FX <sup>tex</sup> ≡ “FX”]

[FY <sup>tex</sup> ≡ “FY”]

[FZ <sup>tex</sup> ≡ “FZ”]

[FU <sup>tex</sup> ≡ “FU”]

[FV <sup>tex</sup> ≡ “FV”]

[FW <sup>tex</sup> ≡ “FW”]

[FEP <sup>tex</sup> ≡ “FEP”]

[RX <sup>tex</sup> ≡ “RX”]

[RY <sup>tex</sup> ≡ “RY”]

[RZ <sup>tex</sup> ≡ “RZ”]

[RU <sup>tex</sup> ≡ “RU”]

[(SX) <sup>tex</sup> ≡ “(SX)”]

[(SX1) <sup>tex</sup> ≡ “(SX1)”]

[(SY) <sup>tex</sup> ≡ “(SY)”]

[(SY1) <sup>tex</sup> ≡ “(SY1)”]

[(SZ) <sup>tex</sup> ≡ “(SZ)”]

[(SZ1) <sup>tex</sup> ≡ “(SZ1)”]

[(SU) <sup>tex</sup> ≡ “(SU)”]

[(SU1)<sup>tex</sup> ≡ “(SU1)”]

[FXS<sup>tex</sup> ≡ “FXS”]

[FYS<sup>tex</sup> ≡ “FYS”]

[(F1)<sup>tex</sup> ≡ “(F1)”]

[(F2)<sup>tex</sup> ≡ “(F2)”]

[(F3)<sup>tex</sup> ≡ “(F3)”]

[(F4)<sup>tex</sup> ≡ “(F4)”]

[(OP1)<sup>tex</sup> ≡ “(OP1)”]

[(OP2)<sup>tex</sup> ≡ “(OP2)”]

[(R1)<sup>tex</sup> ≡ “(R1)”]

[(S1)<sup>tex</sup> ≡ “(S1)”]

[(S2)<sup>tex</sup> ≡ “(S2)”]

[(EPob)<sup>tex</sup> ≡ “(EPob)”]

[(CRS1ob)<sup>tex</sup> ≡ “(CRS1ob)”]

[(F1ob)<sup>tex</sup> ≡ “(F1ob)”]

[(F2ob)<sup>tex</sup> ≡ “(F2ob)”]

[(F3ob)<sup>tex</sup> ≡ “(F3ob)”]

[(F4ob)<sup>tex</sup> ≡ “(F4ob)”]

[(N1ob)<sup>tex</sup> ≡ “(N1ob)”]

[(N2ob)<sup>tex</sup> ≡ “(N2ob)”]

[(OP1ob)<sup>tex</sup> ≡ “(OP1ob)”]

[(OP2ob)<sup>tex</sup> ≡ “(OP2ob)”]

[(R1ob)<sup>tex</sup> ≡ “(R1ob)”]

[(S1ob)<sup>tex</sup> ≡ “(S1ob)”]

[(S2ob)<sup>tex</sup> ≡ “(S2ob)”]

[Ex3  $\stackrel{\text{tex}}{=} \text{“Ex3”}$ ]

[NAT  $\stackrel{\text{tex}}{=} \text{“NAT”}$ ]

[RATIONALSERIES  $\stackrel{\text{tex}}{=} \text{“RATIONAL\_SERIES”}$ ]

[SERIES  $\stackrel{\text{tex}}{=} \text{“SERIES”}$ ]

[SetOfReals  $\stackrel{\text{tex}}{=} \text{“SetOfReals”}$ ]

[SetOfFxs  $\stackrel{\text{tex}}{=} \text{“SetOfFxs”}$ ]

[N  $\stackrel{\text{tex}}{=} \text{“N”}$ ]

[Q  $\stackrel{\text{tex}}{=} \text{“Q”}$ ]

[X  $\stackrel{\text{tex}}{=} \text{“X”}$ ]

[xs  $\stackrel{\text{tex}}{=} \text{“xs”}$ ]

[xaF  $\stackrel{\text{tex}}{=} \text{“xaF”}$ ]

[ysF  $\stackrel{\text{tex}}{=} \text{“ysF”}$ ]

[us  $\stackrel{\text{tex}}{=} \text{“us”}$ ]

[usFoelge  $\stackrel{\text{tex}}{=} \text{“usFoelge”}$ ]

[0  $\stackrel{\text{tex}}{=} \text{“0”}$ ]

[1  $\stackrel{\text{tex}}{=} \text{“1”}$ ]

[(-1)  $\stackrel{\text{tex}}{=} \text{“(-1)”}$ ]

[2  $\stackrel{\text{tex}}{=} \text{“2”}$ ]

[3  $\stackrel{\text{tex}}{=} \text{“3”}$ ]

[1/2  $\stackrel{\text{tex}}{=} \text{“1/2”}$ ]

[1/3  $\stackrel{\text{tex}}{=} \text{“1/3”}$ ]

[2/3  $\stackrel{\text{tex}}{=} \text{“2/3”}$ ]

[0f  $\stackrel{\text{tex}}{=} \text{“0f”}$ ]

[00  $\stackrel{\text{tex}}{=} \text{“00”}$ ]

[(- - 01)  $\stackrel{\text{tex}}{=} \text{“(-01)”}$ ]

[02 <sup>tex</sup> ≡ “02”]

[01//02 <sup>tex</sup> ≡ “01//02”]

[x = y <sup>tex</sup> ≡ “#1.  
= #2.”]

[x ≠ y <sup>tex</sup> ≡ “#1.  
\neq #2.”]

[x < y <sup>tex</sup> ≡ “#1.  
< #2.”]

[x <= y <sup>tex</sup> ≡ “#1.  
<= #2.”]

[x <<sub>f</sub> y <sup>tex</sup> ≡ “#1.  
<\_{f}#2.”]

[x ≤<sub>f</sub> y <sup>tex</sup> ≡ “#1.  
\leq\_{f}#2.”]

[SF(x,y) <sup>tex</sup> ≡ “SF(#1.  
, #2.  
)”]

[x == y <sup>tex</sup> ≡ “#1.  
== #2.”]

[x!! == y <sup>tex</sup> ≡ “#1.  
!!== #2.”]

[x << y <sup>tex</sup> ≡ “#1.  
<< #2.”]

[x <<== y <sup>tex</sup> ≡ “#1.  
<<== #2.”]

[x[y] <sup>tex</sup> ≡ “#1.  
[#2.  
]”]

[(-ux) <sup>tex</sup> ≡ “(-u#1.  
)”]

[-<sub>f</sub>x <sup>tex</sup> ≡ “-\_{f}#1.”]

$[(- - x)^{\text{tex}} \equiv (--\#1.$   
)]

$[1f/x^{\text{tex}} \equiv "1f/\#1." ]$

$[01//tempx^{\text{tex}} \equiv "01//temp\#1." ]$

$[(x + y)^{\text{tex}} \equiv "(#1.$   
+ $\#2.$   
)]

$[(x - y)^{\text{tex}} \equiv "(#1.$   
- $\#2.$   
)]

$[(fx) +_f (fy)^{\text{tex}} \equiv "\#1.$   
+\_{f}\#2." ]

$[(fx) -_f (fy)^{\text{tex}} \equiv "\#1.$   
-\_{f}\#2." ]

$[(fx) *_f (fy)^{\text{tex}} \equiv "\#1.$   
\*\_{f}\#2." ]

$[x + +y^{\text{tex}} \equiv "\#1.$   
++ $\#2." ]$

$[R((fx)) - -R((fy))^{\text{tex}} \equiv "R(\#1.$   
) -- R( $\#2.$   
)]

$[(x * y)^{\text{tex}} \equiv "(#1.$   
\* $\#2.$   
)]

$[x * *y^{\text{tex}} \equiv "\#1.$   
\*\* $\#2." ]$

$[x(\text{exp})y^{\text{tex}} \equiv "\#1.$   
( $\text{exp}$ )  $\#2." ]$

$[\text{leqReflexivity}^{\text{tex}} \equiv "\text{leqReflexivity}"]$

$[\text{recx}^{\text{tex}} \equiv "\text{rec}\#1." ]$

$[|x|^{\text{tex}} \equiv "| \#1.$   
|"]



[StateExpand(t, s, c)  $\stackrel{\text{tex}}{=}$  “StateExpand(#1.  
, #2.  
, #3.  
)”]

[extractSeries(t)  $\stackrel{\text{tex}}{=}$  “extractSeries(#1.  
)”]

[|f|x|  $\stackrel{\text{tex}}{=}$  “|f#1.  
|”]

[|r|x|  $\stackrel{\text{tex}}{=}$  “|r#1.  
|”]

[SetOfSeries(x)  $\stackrel{\text{tex}}{=}$  “SetOfSeries(#1.  
)”]

[ExpandList(x, y, z)  $\stackrel{\text{tex}}{=}$  “ExpandList(#1.  
, #2.  
, #3.  
)”]

[\* \* Macro(x)  $\stackrel{\text{tex}}{=}$  “\*\*Macro(#1.  
)”]

[+ + Macro(x)  $\stackrel{\text{tex}}{=}$  “++Macro(#1.  
)”]

[− − Macro(x)  $\stackrel{\text{tex}}{=}$  “--Macro(#1.  
)”]

[<< Macro(x)  $\stackrel{\text{tex}}{=}$  “<<Macro(#1.  
)”]

[|Macro(x)  $\stackrel{\text{tex}}{=}$  “|Macro(#1.  
)”]

[01//Macro(x)  $\stackrel{\text{tex}}{=}$  “01//Macro(#1.  
)”]

[Max(x, y)  $\stackrel{\text{tex}}{=}$  “Max(#1.  
, #2.  
)”]

[Max(x, y)  $\stackrel{\text{tex}}{=}$  “Max(#1.  
, #2.  
)”]

[Limit(x, y)  $\stackrel{\text{tex}}{=} \text{“Limit(\#1.}$   
 , #2.  
 )”]

[Union(x)  $\stackrel{\text{tex}}{=} \text{“Union(\#1.}$   
 )”]

[if(x, y, z)  $\stackrel{\text{tex}}{=} \text{“if(\#1.}$   
 , #2.  
 , #3.  
 )”]

[IsOrderedPair(x, y, z)  $\stackrel{\text{tex}}{=} \text{“IsOrderedPair(\#1.}$   
 , #2.  
 , #3.  
 )”]

[IsRelation(x, y, z)  $\stackrel{\text{tex}}{=} \text{“IsRelation(\#1.}$   
 , #2.  
 , #3.  
 )”]

[isFunction(x, y, z)  $\stackrel{\text{tex}}{=} \text{“isFunction(\#1.}$   
 , #2.  
 , #3.  
 )”]

[TypeNat(x)  $\stackrel{\text{tex}}{=} \text{“TypeNat(\#1.}$   
 )”]

[TypeNat0(x)  $\stackrel{\text{tex}}{=} \text{“TypeNat0(\#1.}$   
 )”]

[TypeRational(x)  $\stackrel{\text{tex}}{=} \text{“TypeRational(\#1.}$   
 )”]

[TypeRational0(x)  $\stackrel{\text{tex}}{=} \text{“TypeRational0(\#1.}$   
 )”]

[TypeSeries(x, y)  $\stackrel{\text{tex}}{=} \text{“TypeSeries(\#1.}$   
 , #2.  
 )”]

[Typeseries0(x, y)  $\stackrel{\text{tex}}{=} \text{“Typeseries0(\#1.}$   
 , #2.  
 )”]

[UB(x, y) <sup>tex</sup> ≡ “UB(#1.  
, #2.  
)”]

[LUB(x, y) <sup>tex</sup> ≡ “LUB(#1.  
, #2.  
)”]

[BS(x, y) <sup>tex</sup> ≡ “BS(#1.  
, #2.  
)”]

[UStelescope(x, y) <sup>tex</sup> ≡ “UStelescope(#1.  
, #2.  
)”]

[(x) <sup>tex</sup> ≡ “(#1.  
)”]

[R(x) <sup>tex</sup> ≡ “R(#1.  
)”]

[- - R(x) <sup>tex</sup> ≡ “--R(#1.  
)”]

[IsSeries(x, y) <sup>tex</sup> ≡ “IsSeries(#1.  
, #2.  
)”]

[IsNatural(xy, \*) <sup>tex</sup> ≡ “IsNatural(#1.  
, #2.  
)”]

[OrderedPair(x, y) <sup>tex</sup> ≡ “OrderedPair(#1.  
, #2.  
)”]

[leqAntisymmetryAxiom <sup>tex</sup> ≡ “leqAntisymmetryAxiom”]

[leqTransitivityAxiom <sup>tex</sup> ≡ “leqTransitivityAxiom”]

[leqTotality <sup>tex</sup> ≡ “leqTotality”]

[leqAdditionAxiom <sup>tex</sup> ≡ “leqAdditionAxiom”]

[leqMultiplicationAxiom <sup>tex</sup> ≡ “leqMultiplicationAxiom”]

[plusAssociativity <sup>tex</sup> ≡ “plusAssociativity”]

[plusCommutativity<sup>tex</sup> ≡ “plusCommutativity”]  
 [Negative<sup>tex</sup> ≡ “Negative”]  
 [plus0<sup>tex</sup> ≡ “plus0”]  
 [timesAssociativity<sup>tex</sup> ≡ “timesAssociativity”]  
 [timesCommutativity<sup>tex</sup> ≡ “timesCommutativity”]  
 [ReciprocalAxiom<sup>tex</sup> ≡ “ReciprocalAxiom”]  
 [times1<sup>tex</sup> ≡ “times1”]  
 [plusAssociativity<sup>tex</sup> ≡ “plusAssociativity”]  
 [plusCommutativity<sup>tex</sup> ≡ “plusCommutativity”]  
 [Negative<sup>tex</sup> ≡ “Negative”]  
 [Distribution<sup>tex</sup> ≡ “Distribution”]  
 [0not1<sup>tex</sup> ≡ “0not1”]  
 [A4(Axiom)<sup>tex</sup> ≡ “A4(Axiom)”]  
 [InductionAxiom<sup>tex</sup> ≡ “InductionAxiom”]  
 [EqualityAxiom<sup>tex</sup> ≡ “EqualityAxiom”]  
 [EqLeqAxiom<sup>tex</sup> ≡ “EqLeqAxiom”]  
 [EqAdditionAxiom<sup>tex</sup> ≡ “EqAdditionAxiom”]  
 [EqMultiplicationAxiom<sup>tex</sup> ≡ “EqMultiplicationAxiom”]  
 [SENC1<sup>tex</sup> ≡ “SENC1”]  
 [SENC2<sup>tex</sup> ≡ “SENC2”]  
 [Cauchy<sup>tex</sup> ≡ “Cauchy”]  
 [PlusF<sup>tex</sup> ≡ “PlusF”]  
 [ReciprocalF<sup>tex</sup> ≡ “ReciprocalF”]  
 [From ==<sup>tex</sup> ≡ “From==”]  
 [To ==<sup>tex</sup> ≡ “To==”]

[FromInR  $\stackrel{\text{tex}}{\equiv}$  "FromInR"]

[ReciprocalR(Axiom)  $\stackrel{\text{tex}}{\equiv}$  "ReciprocalR(Axiom)"]

[US0  $\stackrel{\text{tex}}{\equiv}$  "US0"]

[NextXS(UpperBound)  $\stackrel{\text{tex}}{\equiv}$  "NextXS(UpperBound)"]

[NextXS(NoUpperBound)  $\stackrel{\text{tex}}{\equiv}$  "NextXS(NoUpperBound)"]

[NextUS(UpperBound)  $\stackrel{\text{tex}}{\equiv}$  "NextUS(UpperBound)"]

[NextUS(NoUpperBound)  $\stackrel{\text{tex}}{\equiv}$  "NextUS(NoUpperBound)"]

[ExpZero  $\stackrel{\text{tex}}{\equiv}$  "ExpZero"]

[ExpPositive  $\stackrel{\text{tex}}{\equiv}$  "ExpPositive"]

[ExpZero(R)  $\stackrel{\text{tex}}{\equiv}$  "ExpZero(R)"]

[ExpPositive(R)  $\stackrel{\text{tex}}{\equiv}$  "ExpPositive(R)"]

[LessMinus1(N)  $\stackrel{\text{tex}}{\equiv}$  "LessMinus1(N)"]

[Nonnegative(N)  $\stackrel{\text{tex}}{\equiv}$  "Nonnegative(N)"]

[BSzero  $\stackrel{\text{tex}}{\equiv}$  "BSzero"]

[BSpositive  $\stackrel{\text{tex}}{\equiv}$  "BSpositive"]

[USTelescope(Zero)  $\stackrel{\text{tex}}{\equiv}$  "USTelescope(Zero)"]

[USTelescope(Positive)  $\stackrel{\text{tex}}{\equiv}$  "USTelescope(Positive)"]

[EqAddition(R)  $\stackrel{\text{tex}}{\equiv}$  "EqAddition(R)"]

[FromLimit  $\stackrel{\text{tex}}{\equiv}$  "FromLimit"]

[ToUpperBound  $\stackrel{\text{tex}}{\equiv}$  "ToUpperBound"]

[FromUpperBound  $\stackrel{\text{tex}}{\equiv}$  "FromUpperBound"]

[USisUpperBound  $\stackrel{\text{tex}}{\equiv}$  "USisUpperBound"]

[0not1(R)  $\stackrel{\text{tex}}{\equiv}$  "0not1(R)"]

[ExpUnbounded(R)  $\stackrel{\text{tex}}{\equiv}$  "ExpUnbounded(R)"]

[FromLeq(Advanced)(N)  $\stackrel{\text{tex}}{\equiv}$  "FromLeq(Advanced)(N)"]

[FromLeastUpperBound  $\stackrel{\text{tex}}{=} \text{“FromLeastUpperBound”}$ ]

[ToLeastUpperBound  $\stackrel{\text{tex}}{=} \text{“ToLeastUpperBound”}$ ]

[XSisNotUpperBound  $\stackrel{\text{tex}}{=} \text{“XSisNotUpperBound”}$ ]

[ysFGreater  $\stackrel{\text{tex}}{=} \text{“ysFGreater”}$ ]

[ysFLess  $\stackrel{\text{tex}}{=} \text{“ysFLess”}$ ]

[SmallInverse  $\stackrel{\text{tex}}{=} \text{“SmallInverse”}$ ]

[MemberOfSeries(ImPLY)  $\stackrel{\text{tex}}{=} \text{“MemberOfSeries(ImPLY)”}$ ]

[NatType  $\stackrel{\text{tex}}{=} \text{“NatType”}$ ]

[RationalType  $\stackrel{\text{tex}}{=} \text{“RationalType”}$ ]

[SeriesType  $\stackrel{\text{tex}}{=} \text{“SeriesType”}$ ]

[JoinConjuncts(2conditions)  $\stackrel{\text{tex}}{=} \text{“JoinConjuncts(2conditions)”}$ ]

[TND  $\stackrel{\text{tex}}{=} \text{“TND”}$ ]

[FromNegatedImPLY  $\stackrel{\text{tex}}{=} \text{“FromNegatedImPLY”}$ ]

[ToNegatedImPLY  $\stackrel{\text{tex}}{=} \text{“ToNegatedImPLY”}$ ]

[FromNegated(2 \* ImPLY)  $\stackrel{\text{tex}}{=} \text{“FromNegated(2*ImPLY)”}$ ]

[FromNegatedAnd  $\stackrel{\text{tex}}{=} \text{“FromNegatedAnd”}$ ]

[FromNegatedOr  $\stackrel{\text{tex}}{=} \text{“FromNegatedOr”}$ ]

[ToNegatedOr  $\stackrel{\text{tex}}{=} \text{“ToNegatedOr”}$ ]

[FromNegations  $\stackrel{\text{tex}}{=} \text{“FromNegations”}$ ]

[From3Disjuncts  $\stackrel{\text{tex}}{=} \text{“From3Disjuncts”}$ ]

[NegateDisjunct1  $\stackrel{\text{tex}}{=} \text{“NegateDisjunct1”}$ ]

[NegateDisjunct2  $\stackrel{\text{tex}}{=} \text{“NegateDisjunct2”}$ ]

[ExpandDisjuncts  $\stackrel{\text{tex}}{=} \text{“ExpandDisjuncts”}$ ]

[From2 \* 2Disjuncts  $\stackrel{\text{tex}}{=} \text{“From2*2Disjuncts”}$ ]

[PlusR(Sym)  $\stackrel{\text{tex}}{=} \text{“PlusR(Sym)”}$ ]

[LessLeq(R)  $\stackrel{\text{tex}}{=} \text{“LessLeq(R)”}$ ]

[LeqAntisymmetry(R)  $\stackrel{\text{tex}}{=} \text{“LeqAntisymmetry(R)”}$ ]

[LeqTransitivity(R)  $\stackrel{\text{tex}}{=} \text{“LeqTransitivity(R)”}$ ]

[Plus0(R)  $\stackrel{\text{tex}}{=} \text{“Plus0(R)”}$ ]

[lessAddition(R)  $\stackrel{\text{tex}}{=} \text{“lessAddition(R)”}$ ]

[leqAddition(R)  $\stackrel{\text{tex}}{=} \text{“leqAddition(R)”}$ ]

[PlusAssociativity(R)XX  $\stackrel{\text{tex}}{=} \text{“PlusAssociativity(R)XX”}$ ]

[PlusAssociativity(R)  $\stackrel{\text{tex}}{=} \text{“PlusAssociativity(R)”}$ ]

[Negative(R)  $\stackrel{\text{tex}}{=} \text{“Negative(R)”}$ ]

[PlusCommutativity(R)  $\stackrel{\text{tex}}{=} \text{“PlusCommutativity(R)”}$ ]

[Times1(R)  $\stackrel{\text{tex}}{=} \text{“Times1(R)”}$ ]

[TimesAssociativity(R)  $\stackrel{\text{tex}}{=} \text{“TimesAssociativity(R)”}$ ]

[TimesCommutativity(R)  $\stackrel{\text{tex}}{=} \text{“TimesCommutativity(R)”}$ ]

[Distribution(R)  $\stackrel{\text{tex}}{=} \text{“Distribution(R)”}$ ]

[ $\exists x: y \stackrel{\text{tex}}{=} \text{“(AARRGGHH!-exist-bug!)”}$ ]

[constantRationalSeries(x)  $\stackrel{\text{tex}}{=} \text{“constantRationalSeries(\#1. )”}$ ]

[Power(x)  $\stackrel{\text{tex}}{=} \text{“Power(\#1. )”}$ ]

[cartProd(x)  $\stackrel{\text{tex}}{=} \text{“cartProd(\#1. )”}$ ]

[binaryUnion(x, y)  $\stackrel{\text{tex}}{=} \text{“binaryUnion(\#1. , \#2. )”}$ ]

[SetOfRationalSeries  $\stackrel{\text{tex}}{=} \text{“SetOfRationalSeries”}$ ]

[MemberOfSeries  $\stackrel{\text{tex}}{=} \text{“MemberOfSeries”}$ ]

[IsSubset(x, y)  $\stackrel{\text{tex}}{=} \text{“IsSubset(\#1. \#2.)”}$ ]

[memberOfSeries(Type)  $\stackrel{\text{tex}}{=} \text{“memberOfSeries(Type)”}$ ]

[UniqueMember  $\stackrel{\text{tex}}{=} \text{“UniqueMember”}$ ]

[UniqueMember(Type)  $\stackrel{\text{tex}}{=} \text{“UniqueMember(Type)”}$ ]

[SameSeries  $\stackrel{\text{tex}}{=} \text{“SameSeries”}$ ]

[A4  $\stackrel{\text{tex}}{=} \text{“A4”}$ ]

[(sx)  $\stackrel{\text{tex}}{=} \text{“(s\#1.)”}$ ]

[(px, y)  $\stackrel{\text{tex}}{=} \text{“(p\#1. \#2.)”}$ ]

[SameMember  $\stackrel{\text{tex}}{=} \text{“SameMember”}$ ]

[Qclosed(Addition)  $\stackrel{\text{tex}}{=} \text{“Qclosed(Addition)”}$ ]

[Qclosed(Multiplication)  $\stackrel{\text{tex}}{=} \text{“Qclosed(Multiplication)”}$ ]

[FromCartProd(1)  $\stackrel{\text{tex}}{=} \text{“FromCartProd(1)”}$ ]

[FromCartProd(1)  $\stackrel{\text{tex}}{=} \text{“FromCartProd(1)”}$ ]

[Max  $\stackrel{\text{tex}}{=} \text{“Max”}$ ]

[Numerical  $\stackrel{\text{tex}}{=} \text{“Numerical”}$ ]

[NumericalF  $\stackrel{\text{tex}}{=} \text{“NumericalF”}$ ]

[Separation2formula(1)  $\stackrel{\text{tex}}{=} \text{“Separation2formula(1)”}$ ]

[Separation2formula(2)  $\stackrel{\text{tex}}{=} \text{“Separation2formula(2)”}$ ]

[QisClosed(Reciprocal)(Imply)  $\stackrel{\text{tex}}{=} \text{“QisClosed(Reciprocal)(Imply)”}$ ]

[QisClosed(Reciprocal)  $\stackrel{\text{tex}}{=} \text{“QisClosed(Reciprocal)”}$ ]

[QisClosed(Negative)(Imply)  $\stackrel{\text{tex}}{=} \text{“QisClosed(Negative)(Imply)”}$ ]

[QisClosed(Negative)  $\stackrel{\text{tex}}{=} \text{“QisClosed(Negative)”}$ ]



$[(\text{Adgic})\text{SameR} \stackrel{\text{tex}}{\equiv} “(\text{Adgic})\text{SameR}”]$