

# Logiweb codex of logik rapport

## Up Help

$S'$ ,  $A1'$ ,  $A2'$ ,  $A3'$ ,  $A4'$ ,  $A5'$ ,  $S1'$ ,  $S2'$ ,  $S3'$ ,  $S4'$ ,  $S5'$ ,  $S6'$ ,  $S7'$ ,  $S8'$ ,  $S9'$ ,  $MP'$ ,  $Gen'$ ,  
logik rapport,  $A2'^*$ ,  $A1'^*$ ,  $DoubleHypothesis$ ,  $C1.10a$ ,  $C1.10(b)$ ,  $L1.8$ ,  $L3.2(b)'$ ,  
 $L3.2(c)'$ ,  $L3.2(d)'$ ,  $L3.2(f)'$ ,  $L3.2(f)'_{BASE}$ ,  $L3.2(f)'_{HYP}$ ,  $L3.2(g)'$ ,  $L3.2(g)'_{BASE}$ ,  
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$S'$

$[S' \xrightarrow{stmt} x]$

$A1'$

$[A1' \xrightarrow{proof} \text{Rule tactic}]$

$[A1' \xrightarrow{stmt} S' \vdash \forall \underline{a}: \forall \underline{b}: [ [ \underline{a} \Rightarrow \underline{b} ] \Rightarrow \underline{a} ] ]$

$A2'$

$[A2' \xrightarrow{proof} \text{Rule tactic}]$

$[A2' \xrightarrow{stmt} S' \vdash \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: [ [ [ [ [ \underline{a} \Rightarrow \underline{b} ] \Rightarrow \underline{c} ] \Rightarrow [ \underline{a} \Rightarrow \underline{b} ] ] \Rightarrow \underline{a} ] \Rightarrow \underline{c} ] ] ]$

$A3'$

$[A3' \xrightarrow{proof} \text{Rule tactic}]$

$[A3' \xrightarrow{stmt} S' \vdash \forall \underline{a}: \forall \underline{b}: [ [ [ [ [ \neg \underline{b} ] \Rightarrow \neg \underline{a} ] \Rightarrow [ [ \neg \underline{b} ] \Rightarrow \underline{a} ] ] \Rightarrow \underline{b} ] ] ]$

$A4'$

$[A4' \xrightarrow{proof} \text{Rule tactic}]$

$[A4' \xrightarrow{stmt} S' \vdash \forall \underline{c}: \forall \underline{a}: \forall \underline{x}: \forall \underline{b}: [ [ \underline{a} ] \equiv [ \underline{b} ] \mid [ \underline{x} ] := [ \underline{c} ] ] \# [ [ \forall \underline{x}: \underline{b} ] \Rightarrow \underline{a} ] ] ]$

A5'

[A5'  $\xrightarrow{\text{proof}}$  Rule tactic]

[A5'  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{x}: \forall \underline{a}: \forall \underline{b}: [ \text{nonfree}([\underline{x}], [\underline{a}]) \vdash [ [ [ \forall \underline{x}: [ \underline{a} \Rightarrow \underline{b} ] ] \Rightarrow \underline{a} ] \Rightarrow \forall \underline{x}: \underline{b} ] ] ]$ ]

S1'

[S1'  $\xrightarrow{\text{proof}}$  Rule tactic]

[S1'  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: [ [ [ \underline{a} \stackrel{P}{=} \underline{b} ] \Rightarrow [ \underline{a} \stackrel{P}{=} \underline{c} ] ] \Rightarrow [ \underline{b} \stackrel{P}{=} \underline{c} ] ] ]$ ]

S2'

[S2'  $\xrightarrow{\text{proof}}$  Rule tactic]

[S2'  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{a}: \forall \underline{b}: [ [ \underline{a} \stackrel{P}{=} \underline{b} ] \Rightarrow [ \underline{a}' \stackrel{P}{=} [ \underline{b}' ] ] ] ]$ ]

S3'

[S3'  $\xrightarrow{\text{proof}}$  Rule tactic]

[S3'  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{a}: \neg [ \dot{0} \stackrel{P}{=} [ \underline{a}' ] ] ]$ ]

S4'

[S4'  $\xrightarrow{\text{proof}}$  Rule tactic]

[S4'  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{a}: \forall \underline{b}: [ [ \underline{a}' \stackrel{P}{=} [ \underline{b}' ] ] \Rightarrow [ \underline{a} \stackrel{P}{=} \underline{b} ] ] ]$ ]

S5'

[S5'  $\xrightarrow{\text{proof}}$  Rule tactic]

[S5'  $\xrightarrow{\text{stmt}}$   $S' \vdash \forall \underline{a}: [ [ \underline{a} \dot{+} \dot{0} ] \stackrel{P}{=} \underline{a} ] ]$ ]

S6'

[S6'  $\xrightarrow{\text{proof}}$  Rule tactic]

$[S6' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{a}: \forall \underline{b}: [ [ \underline{a} \dot{+} [ \underline{b}' ] ] \stackrel{p}{=} [ [ \underline{a} \dot{+} \underline{b} ]' ] ] ]$

S7'

$[S7' \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[S7' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{a}: [ [ \underline{a} \dot{:} \dot{0} ] \stackrel{p}{=} \dot{0} ] ]$

S8'

$[S8' \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[S8' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{a}: \forall \underline{b}: [ [ \underline{a} \dot{:} [ \underline{b}' ] ] \stackrel{p}{=} [ [ \underline{a} \dot{:} \underline{b} ] \dot{+} \underline{a} ] ] ]$

S9'

$[S9' \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[S9' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{a}: \forall \underline{b}: \forall \underline{c}: \forall \underline{x}: [ \underline{b} \equiv \langle \underline{a} | \underline{x} := \dot{0} \rangle \Vdash [ \underline{c} \equiv \langle \underline{a} | \underline{x} := \underline{x}' \rangle \Vdash [ [ \underline{b} \dot{\Rightarrow} \dot{\forall} \underline{x}: [ \underline{a} \dot{\Rightarrow} \underline{c} ] ] \dot{\Rightarrow} \dot{\forall} \underline{x}: \underline{a} ] ] ] ] ]$

MP'

$[MP' \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[MP' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{a}: \forall \underline{b}: [ [ \underline{a} \dot{\Rightarrow} \underline{b} ] \vdash [ \underline{a} \vdash \underline{b} ] ] ]$

Gen'

$[Gen' \xrightarrow{\text{proof}} \text{Rule tactic}]$

$[Gen' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{x}: \forall \underline{a}: [ \underline{a} \vdash \dot{\forall} \underline{x}: \underline{a} ] ]$

**logik rapport**

$[\text{logik rapport} \xrightarrow{\text{pyk}} \text{"logik rapport"}]$

## A2'\*

$$[A2'^* \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash \forall h: \forall a: \forall b: [ [ h \Rightarrow [ a \Rightarrow b ] ] ] \vdash [ [ A2' \gg [ [ h \Rightarrow [ a \Rightarrow b ] ] ] \Rightarrow [ [ h \Rightarrow a ] \Rightarrow [ h \Rightarrow b ] ] ] ]]; [ [ [ MP' \triangleright [ [ h \Rightarrow [ a \Rightarrow b ] ] ] ] \Rightarrow [ [ h \Rightarrow a ] \Rightarrow [ h \Rightarrow b ] ] ] ] ] \triangleright [ h \Rightarrow [ a \Rightarrow b ] ] \gg [ [ h \Rightarrow a ] \Rightarrow [ h \Rightarrow b ] ] ]], p_0, c)]$$

$$[A2'^* \xrightarrow{\text{stmt}} S' \vdash \forall h: \forall a: \forall b: [ [ h \Rightarrow [ a \Rightarrow b ] ] ] \vdash [ [ h \Rightarrow a ] \Rightarrow [ h \Rightarrow b ] ] ] ]]$$

$$[A2'^* \xrightarrow{\text{tex}} \text{"\{A2'\}^*"}]$$

$$[A2'^* \xrightarrow{\text{pyk}} \text{"lemma prime a two star"}]$$

## A1'\*

$$[A1'^* \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash \forall a: \forall h: [ a \vdash [ [ A1' \gg [ a \Rightarrow [ h \Rightarrow a ] ] ] ] ]]; [ [ [ MP' \triangleright [ a \Rightarrow [ h \Rightarrow a ] ] ] ] \triangleright a ] \gg [ h \Rightarrow a ] ] ] ]], p_0, c)]$$

$$[A1'^* \xrightarrow{\text{stmt}} S' \vdash \forall a: \forall h: [ a \vdash [ h \Rightarrow a ] ] ]]$$

$$[A1'^* \xrightarrow{\text{tex}} \text{"\{A1'\}^*"}]$$

$$[A1'^* \xrightarrow{\text{pyk}} \text{"lemma prime a one star"}]$$

## DoubleHypothesis

$$[\text{DoubleHypothesis} \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash \forall a: \forall b: \forall h: [ [ a \Rightarrow b ] ] \vdash [ [ [ A1'^* \triangleright [ a \Rightarrow b ] ] ] \gg [ h \Rightarrow [ a \Rightarrow b ] ] ] ]]; [ [ A2'^* \triangleright [ h \Rightarrow [ a \Rightarrow b ] ] ] ] \gg [ [ h \Rightarrow a ] \Rightarrow [ h \Rightarrow b ] ] ] ]], p_0, c)]$$

$$[\text{DoubleHypothesis} \xrightarrow{\text{stmt}} S' \vdash \forall a: \forall b: \forall h: [ [ a \Rightarrow b ] ] \vdash [ [ h \Rightarrow a ] \Rightarrow [ h \Rightarrow b ] ] ] ]]$$

$$[\text{DoubleHypothesis} \xrightarrow{\text{tex}} \text{"Double Hypothesis"}]$$

$$[\text{DoubleHypothesis} \xrightarrow{\text{pyk}} \text{"lemma double hyp"}]$$

## C1.10a

$$[C1.10a \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash \forall b: \forall c: \forall d: [ [ b \Rightarrow c ] ] \vdash [ [ c \Rightarrow d ] ] \vdash [ [ A1' \gg [ [ c \Rightarrow d ] ] \Rightarrow [ b \Rightarrow [ c \Rightarrow d ] ] ] ] ]]; [ [ [ [ MP' \triangleright [ [ c \Rightarrow d ] ] \Rightarrow [ b \Rightarrow [ c \Rightarrow d ] ] ] ] ] \triangleright [ c \Rightarrow d ] ] \gg [ b \Rightarrow [ c \Rightarrow d ] ] ]]; [ [ A2' \gg [ [ b \Rightarrow [ c \Rightarrow d ] ] ] \Rightarrow [ [ b \Rightarrow c ] \Rightarrow [ b \Rightarrow d ] ] ] ]]; [ [ [ [ MP' \triangleright [ [ b \Rightarrow [ c \Rightarrow d ] ] ] ] ] \Rightarrow [ [ b \Rightarrow c ] \Rightarrow [ b \Rightarrow d ] ] ] ] ] \triangleright [ b \Rightarrow [ c \Rightarrow d ] ] ] \gg [ [ b \Rightarrow c ] ] ]]$$



$\text{]}, p_0, c]$

$[\text{L3.2(b)}' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{t}: \forall \underline{r}: [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{t} ] ] ]$

$[\text{L3.2(b)}' \xrightarrow{\text{tex}} \text{“L3.2(b)”}]$

$[\text{L3.2(b)}' \xrightarrow{\text{pyk}} \text{“lemma prime 1 three two b”}]$

**L3.2(c)'**

$[\text{L3.2(c)}' \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash \forall \underline{t}: \forall \underline{r}: \forall \underline{s}: [ [ S1' \gg [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] ] ; [ [ \text{L3.2(b)}' \gg [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{t} ] ] ] ] ; [ [ [ \text{C1.10a} \triangleright [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{t} ] ] ] \triangleright [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] ] \gg [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] ] ], p_0, c)]$

$[\text{L3.2(c)}' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{t}: \forall \underline{r}: \forall \underline{s}: [ [ \underline{t} \stackrel{P}{=} \underline{r} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ]$

$[\text{L3.2(c)}' \xrightarrow{\text{tex}} \text{“L3.2(c)”}]$

$[\text{L3.2(c)}' \xrightarrow{\text{pyk}} \text{“lemma prime 1 three two c”}]$

**L3.2(d)'**

$[\text{L3.2(d)}' \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash \forall \underline{t}: \forall \underline{r}: \forall \underline{s}: [ [ \text{L3.2(c)}' \gg [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{t} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] ; [ [ [ \text{Tautology1} \triangleright [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{t} \stackrel{P}{=} \underline{s} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] \gg [ [ \underline{t} \stackrel{P}{=} \underline{s} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] ; [ [ \text{L3.2(b)}' \gg [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] ; [ [ [ [ \text{C1.10a} \triangleright [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{t} \stackrel{P}{=} \underline{s} ] ] ] ] \triangleright [ [ \underline{t} \stackrel{P}{=} \underline{s} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] \gg [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] ; [ [ \text{Tautology1} \triangleright [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] \gg [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ] ] ] ], p_0, c)]$

$[\text{L3.2(d)}' \xrightarrow{\text{stmt}} S' \vdash \forall \underline{t}: \forall \underline{r}: \forall \underline{s}: [ [ \underline{r} \stackrel{P}{=} \underline{t} ] \Rightarrow [ [ \underline{s} \stackrel{P}{=} \underline{t} ] \Rightarrow [ \underline{r} \stackrel{P}{=} \underline{s} ] ] ] ]$

$[\text{L3.2(d)}' \xrightarrow{\text{tex}} \text{“L3.2(d)”}]$

$[\text{L3.2(d)}' \xrightarrow{\text{pyk}} \text{“lemma prime 1 three two d”}]$

**L3.2(f)'**

$[\text{L3.2(f)}' \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash [ [ \text{L3.2(f)}'_{\text{BASE}} \gg [ \dot{0} \stackrel{P}{=} [ \dot{0} \dot{+} \dot{0} ] ] ] ] ; [ [ \text{L3.2(f)}'_{\text{HYP}} \gg \dot{\forall} \underline{t}: [ [ \underline{t} \stackrel{P}{=} [ \dot{0} \dot{+} [\underline{t}] ] ] ] \Rightarrow [ \underline{t}' \stackrel{P}{=} [ \dot{0} \dot{+} [\underline{t}'] ] ] ] ] ] ] ; [ [ S9' \gg [ [ \dot{0} \stackrel{P}{=} [ \dot{0} \dot{+} \dot{0} ] ] ] \Rightarrow [ [ \dot{\forall} \underline{t}: [ [ \underline{t} \stackrel{P}{=} [ \dot{0} \dot{+} [\underline{t}] ] ] ] \Rightarrow [ \underline{t}' \stackrel{P}{=} [ \dot{0} \dot{+} [\underline{t}'] ] ] ] ] ] ] ] \Rightarrow \dot{\forall} \underline{t}: [ \underline{t} \stackrel{P}{=} [ \dot{0} \dot{+} [\underline{t}] ] ] ] ] ] ; [ [ [ [ \text{MP}' \triangleright [ [ \dot{0} \stackrel{P}{=} [ \dot{0} \dot{+} \dot{0} ] ] ] ] ] ] ] ] ] ] ], p_0, c)]$

$$\begin{aligned} & ] \Rightarrow [ [\dot{\forall}t: [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] ] \Rightarrow [t' \stackrel{P}{=} [\dot{0} \dot{+} [t']] ] ] ] ] \Rightarrow \dot{\forall}t: [t \stackrel{P}{=} [ \\ & \dot{0} \dot{+} [t] ] ] ] ] \triangleright [ \dot{0} \stackrel{P}{=} [\dot{0} \dot{+} \dot{0}] ] ] \gg [ [\dot{\forall}t: [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] ] \Rightarrow \\ & [t' \stackrel{P}{=} [\dot{0} \dot{+} [t']] ] ] ] \Rightarrow \dot{\forall}t: [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] ] ]; [ [ [MP' \triangleright [ [\dot{\forall}t: \\ & [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [t' \stackrel{P}{=} [\dot{0} \dot{+} [t']] ] ] ] ] \Rightarrow \dot{\forall}t: [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] ] \\ & ] ] \triangleright \dot{\forall}t: [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [t' \stackrel{P}{=} [\dot{0} \dot{+} [t']] ] ] ] ] \gg \dot{\forall}t: [t \stackrel{P}{=} [ \\ & \dot{0} \dot{+} [t] ] ] ] ] ] ], p_0, c) \end{aligned}$$

$$[L3.2(f)' \xrightarrow{\text{stmt}} S' \vdash \dot{\forall}t: [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] ]$$

$$[L3.2(f)' \xrightarrow{\text{tex}} \text{“L3.2(f)”}]$$

$$[L3.2(f)' \xrightarrow{\text{pyk}} \text{“lemma prime 1 three two f”}]$$

### L3.2(f)'<sub>BASE</sub>

$$\begin{aligned} & [L3.2(f)'_{\text{BASE}} \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash [ [S5' \gg [ [\dot{0} \dot{+} \dot{0}] \stackrel{P}{=} \dot{0}] ] ]; [ [L3.2(b)' \gg \\ & [ [ [\dot{0} \dot{+} \dot{0}] \stackrel{P}{=} \dot{0}] \Rightarrow [\dot{0} \stackrel{P}{=} [\dot{0} \dot{+} \dot{0}]] ] ] ]; [ [ [MP' \triangleright [ [ [ [\dot{0} \dot{+} \dot{0}] \stackrel{P}{=} \dot{0}] \Rightarrow \\ & [\dot{0} \stackrel{P}{=} [\dot{0} \dot{+} \dot{0}]] ] ] ] \triangleright [ [\dot{0} \dot{+} \dot{0}] \stackrel{P}{=} \dot{0}] ] \gg [ \dot{0} \stackrel{P}{=} [\dot{0} \dot{+} \dot{0}] ] ] ] ], p_0, c) \end{aligned}$$

$$[L3.2(f)'_{\text{BASE}} \xrightarrow{\text{stmt}} S' \vdash [\dot{0} \stackrel{P}{=} [\dot{0} \dot{+} \dot{0}]] ]$$

$$[L3.2(f)'_{\text{BASE}} \xrightarrow{\text{tex}} \text{“}\{L3.2(f)\}\text{-}\{BASE\}\text{”}]$$

$$[L3.2(f)'_{\text{BASE}} \xrightarrow{\text{pyk}} \text{“lemma prime 1 three two f base”}]$$

### L3.2(f)'<sub>HYP</sub>

$$\begin{aligned} & [L3.2(f)'_{\text{HYP}} \xrightarrow{\text{proof}} \lambda c. \lambda x. \mathcal{P}([S' \vdash [ [L1.8 \gg [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [t \stackrel{P}{=} [ \\ & \dot{0} \dot{+} [t] ] ] ] ] ]; [ [S6' \gg [ [ [\dot{0} \dot{+} [t']] ] \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ]; [ [ \\ & A1' \gg [ [ [ [\dot{0} \dot{+} [t']] ] \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] \Rightarrow [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [ \\ & [\dot{0} \dot{+} [t']] ] \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ] ]; [ [ [ [MP' \triangleright [ [ [\dot{0} \dot{+} [t']] ] \stackrel{P}{=} \\ & [ [\dot{0} \dot{+} [t]] ]' ] ] \Rightarrow [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [ [\dot{0} \dot{+} [t']] ] \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] \\ & ]' ] ] ] ] \triangleright [ [\dot{0} \dot{+} [t']] ] \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] \gg [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \\ & ] \Rightarrow [ [\dot{0} \dot{+} [t']] ] \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ]; [ [S2' \gg [ [t \stackrel{P}{=} [\dot{0} \dot{+} [ \\ & \dot{t}] ] \Rightarrow [t' \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ]; [ [A1' \gg [ [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \\ & ] \Rightarrow [t' \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] \Rightarrow [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] \\ & ] ] \Rightarrow [t' \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ] ]; [ [ [ [MP' \triangleright [ [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] \\ & ] ] \Rightarrow [t' \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] \Rightarrow [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [ [t \stackrel{P}{=} [ \\ & \dot{0} \dot{+} [t]] ] \Rightarrow [t' \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ] ] \triangleright [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \\ & ] \Rightarrow [t' \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ] \gg [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [ [t \stackrel{P}{=} [\dot{0} \dot{+} [ \\ & \dot{t}] ] \Rightarrow [t' \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ] ]; [ [ [A2* \triangleright [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \\ & ] \Rightarrow [ [t \stackrel{P}{=} [\dot{0} \dot{+} [t]] ] \Rightarrow [t' \stackrel{P}{=} [ [\dot{0} \dot{+} [t]] ]' ] ] ] ] \gg [ [ [t \stackrel{P}{=} [ \end{aligned}$$

